

Prof Douglas Paul

**Director: James Watt Nanofabrication Centre
University of Glasgow
U.K.**



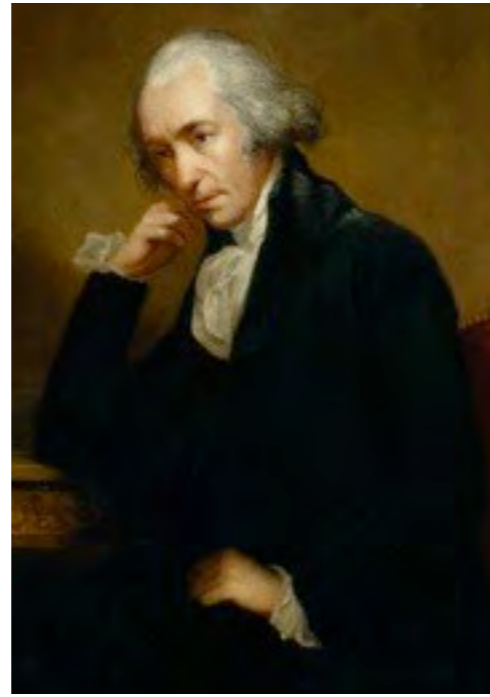
- **Established in 1451**
- **7 Nobel Laureates, 2 SI units, ultrasound, television, etc.....**
- **16,500 undergraduates, 5,000 graduates and 5,000 adult students**
- **£186M research income pa**



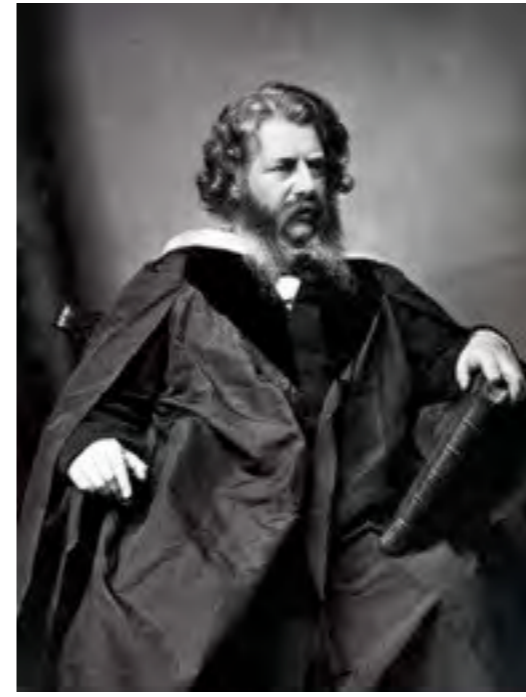
- **400 years in High Street**
- **Moved to Gilmorehill in 1870**
- **Neo-gothic buildings by Gilbert Scott**



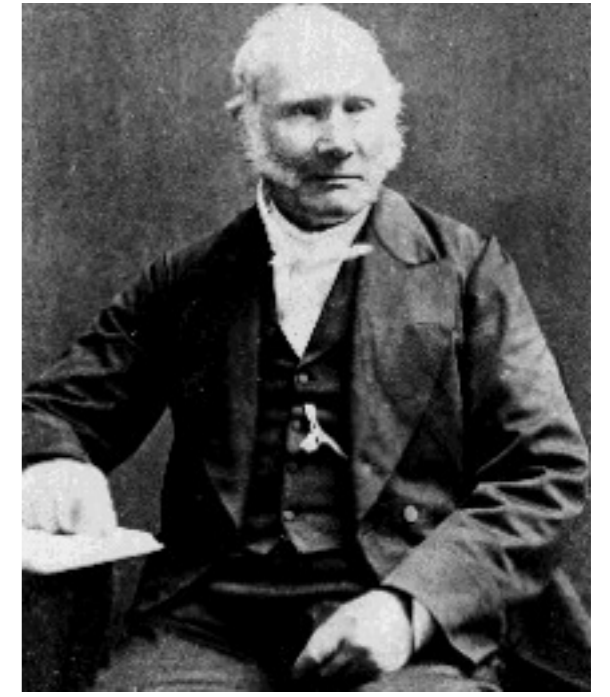
**William Thomson
(Lord Kelvin)**



James Watt



**William John
Macquorn Rankine**



Rev Robert Stirling



Rev John Kerr



Joseph Black



John Logie Baird



Adam Smith



E-beam lithography



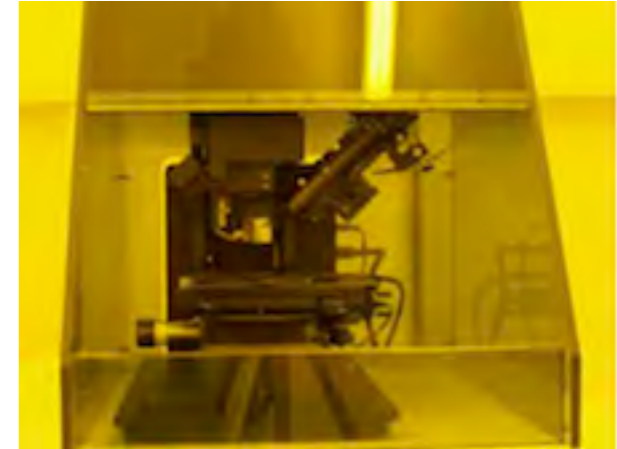
Süss MA6 optical lith

14 RIE / PECVD / ALD



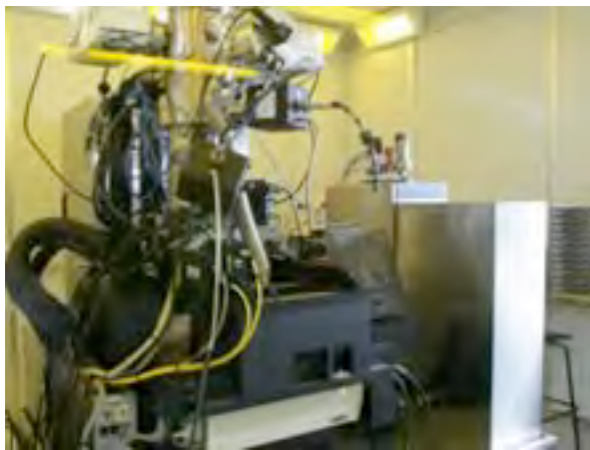
- 900 m² cleanroom - pseudo-industrial operation
- 14 technicians + 4 PhD research technologists
- Processes include: MMICs, III-V, Si/SiGe/Ge, integrated photonics, metamaterials, MEMS (microfluidics)
- Part of EPSRC III-V National Facility & STFC Kelvin-Rutherford Facility
- Commercial access through Kelvin NanoTechnology
- <http://www.jwnc.gla.ac.uk/>

6 Metal dep tools 4 SEMs: Hitachi S4700 Veeco: AFMs



**30 years
experience
of e-beam
lithography**

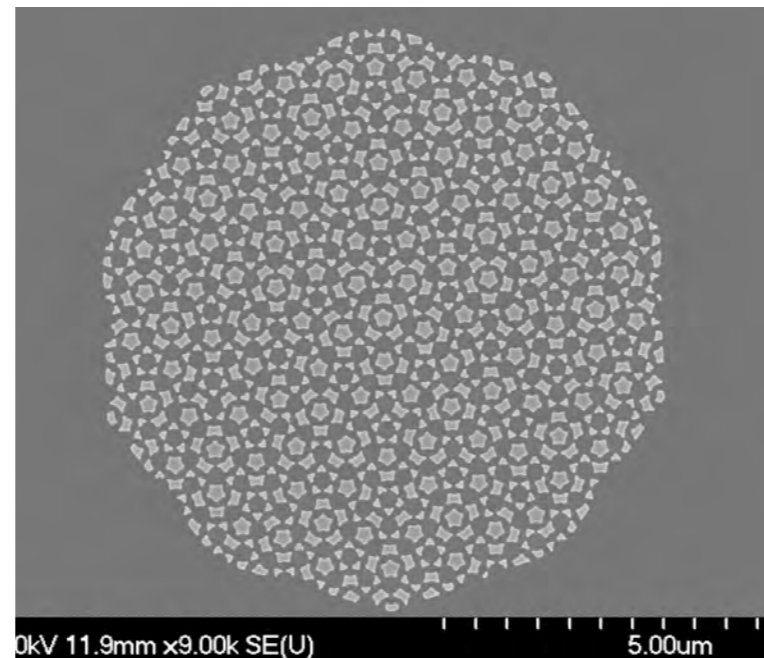
**Sub-5 nm single-line
lithography for research**



Vistec VB6

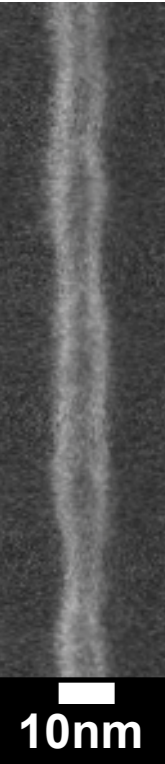
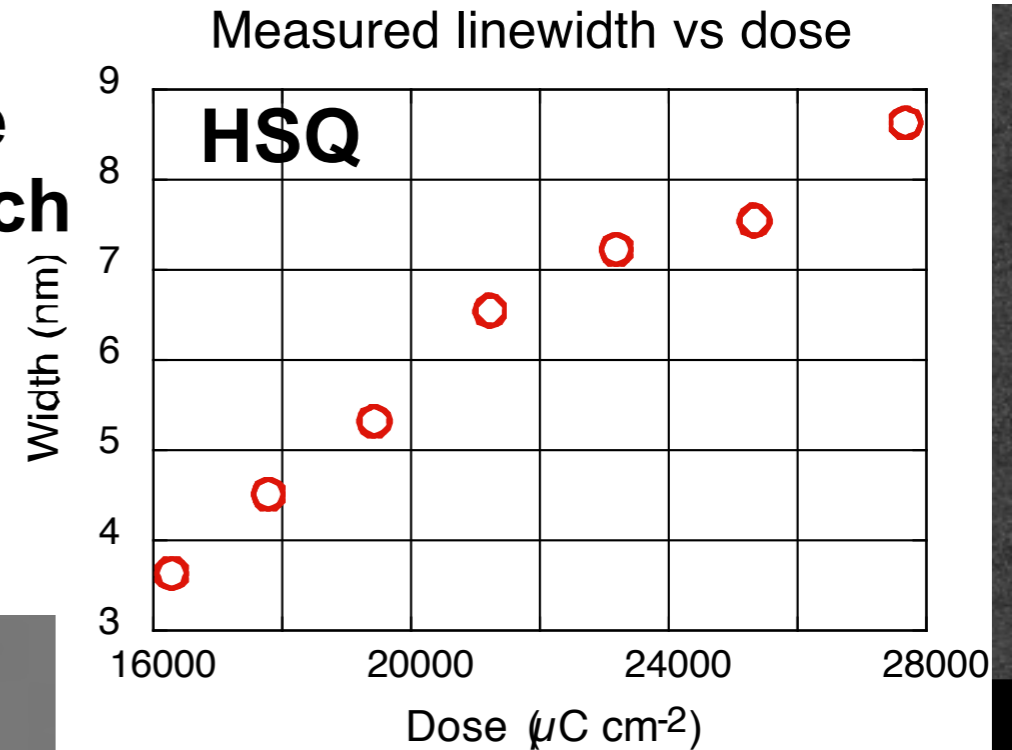


Vistec EBPG5

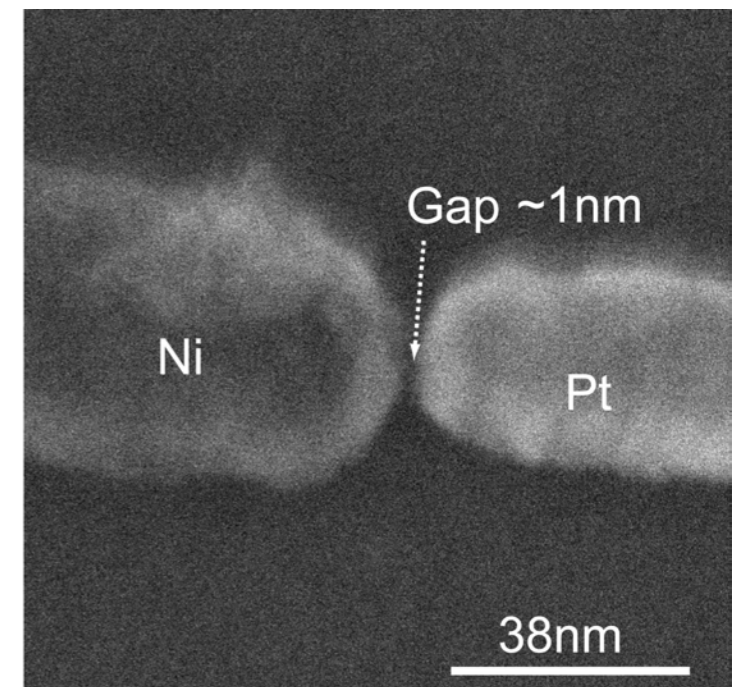


**Alignment allows 1 nm gaps
between different layers:**

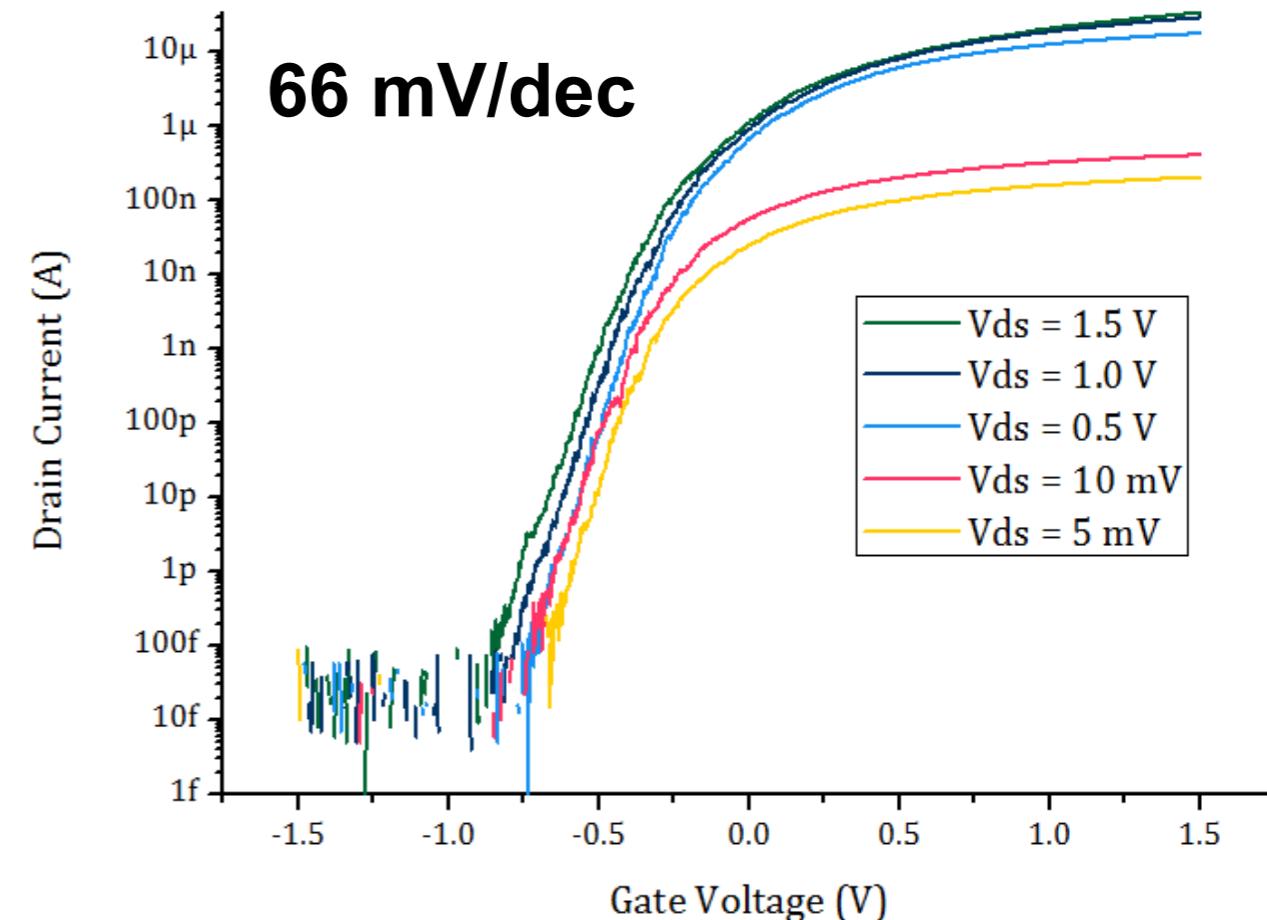
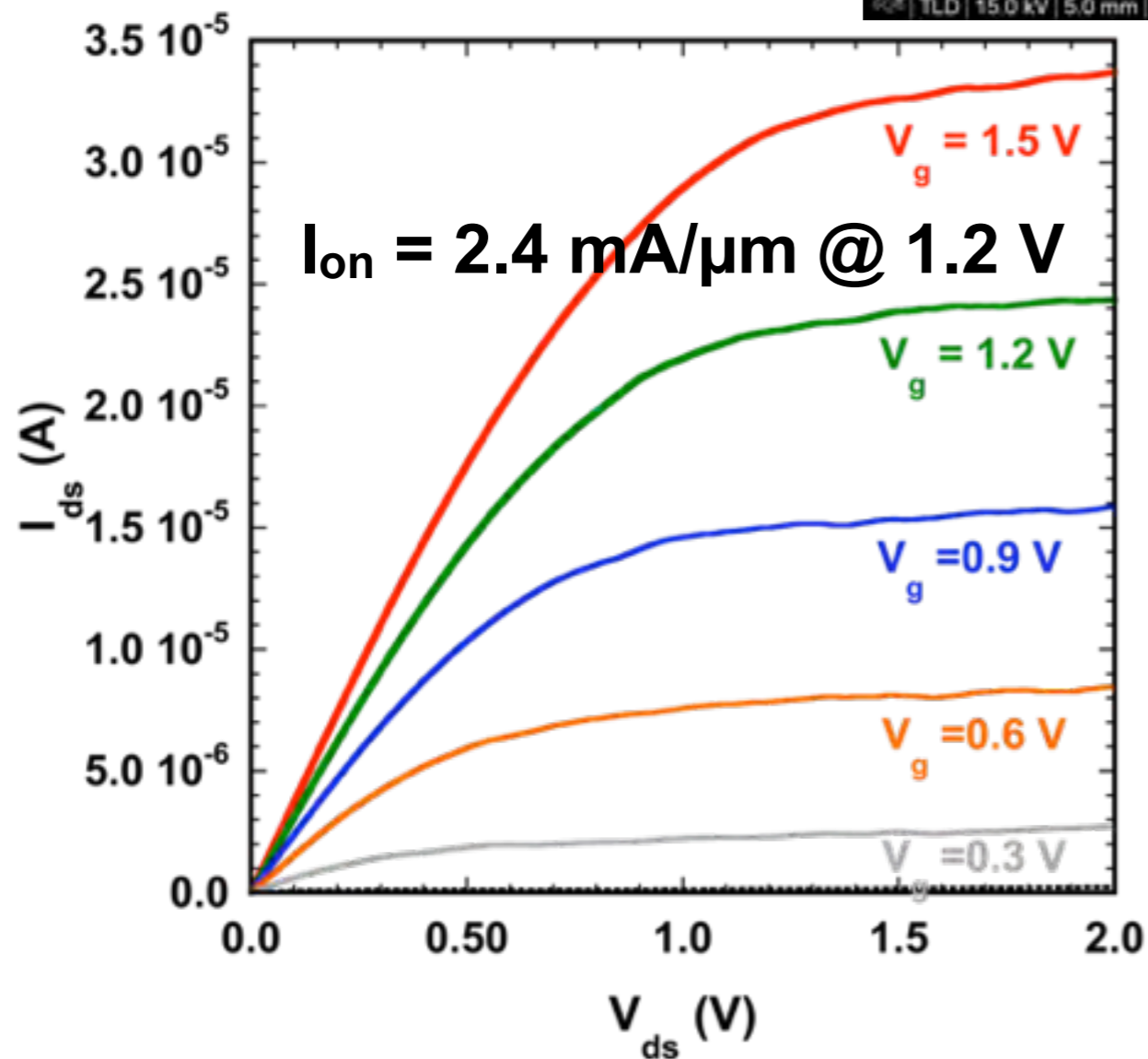
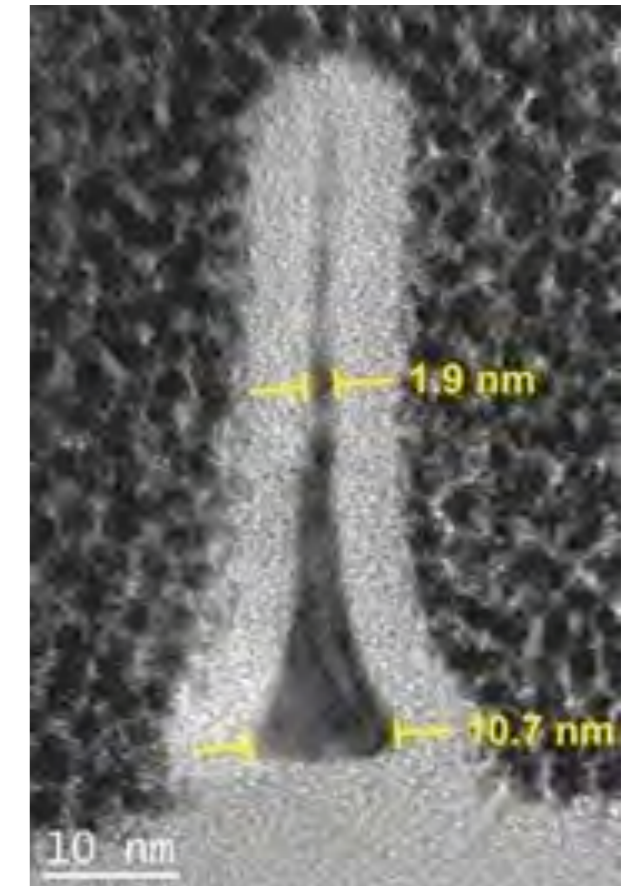
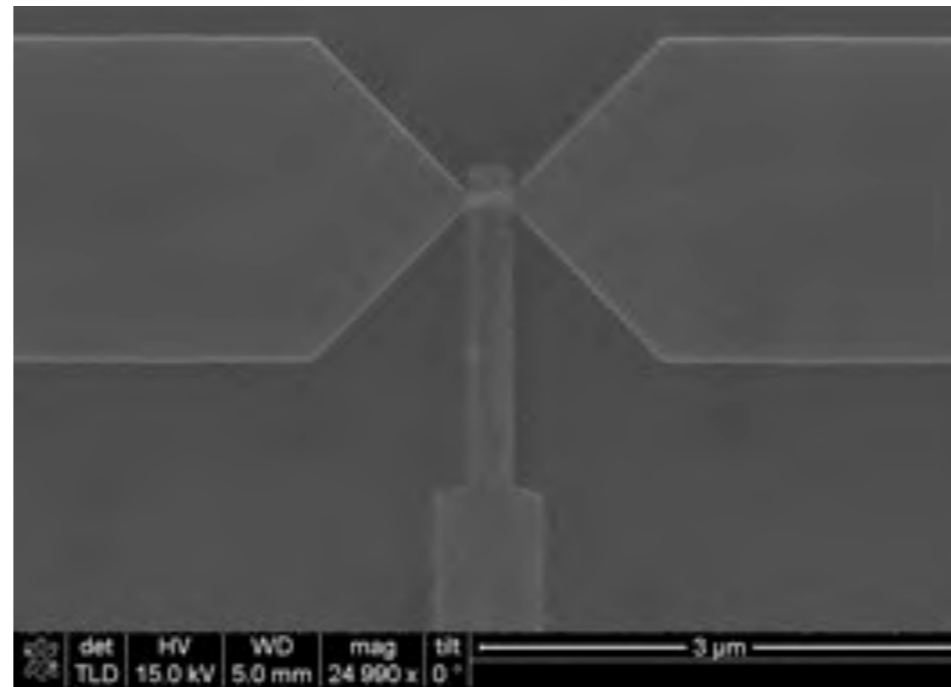
**→ nanoscience: single
molecule metrology**



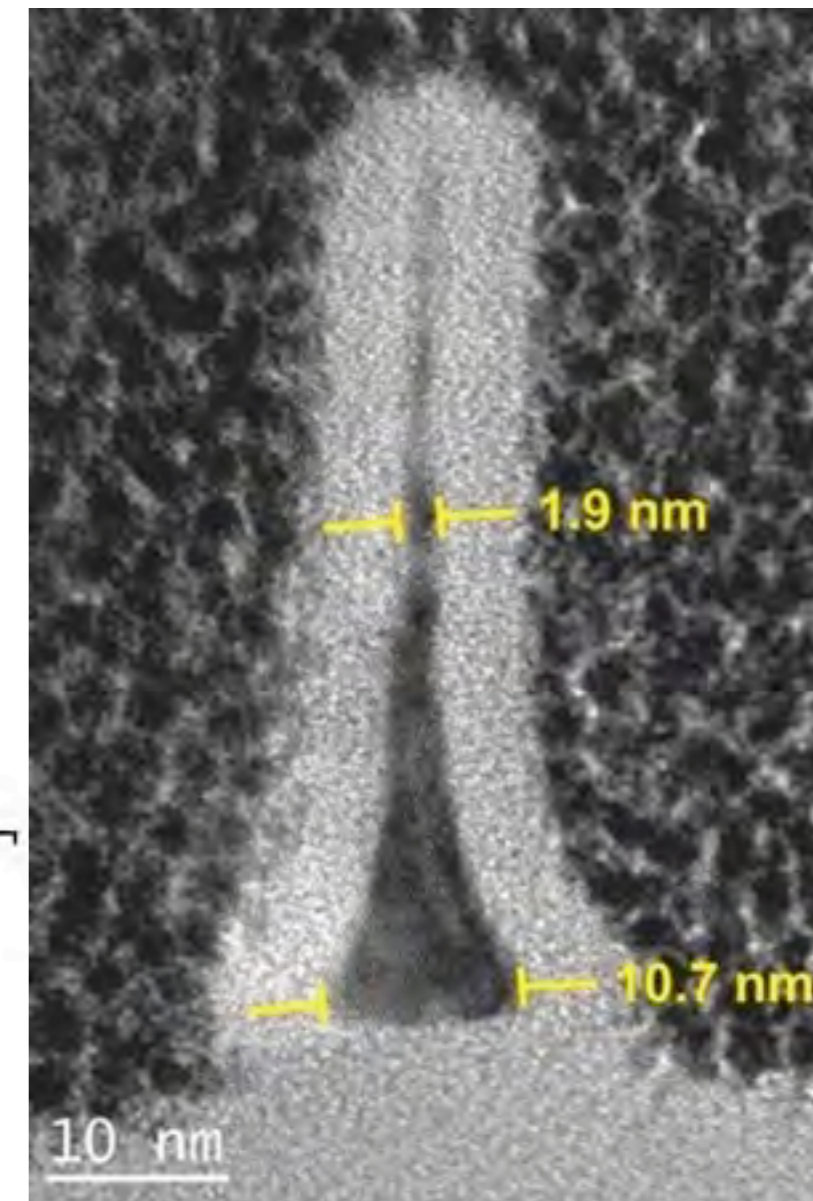
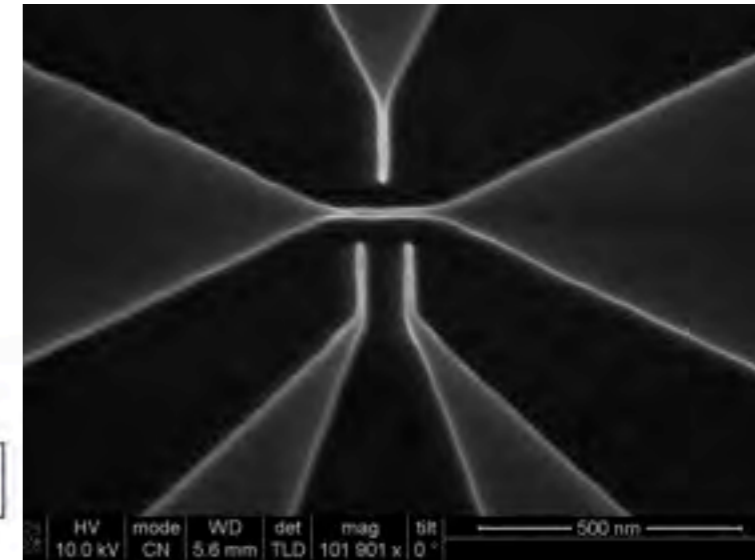
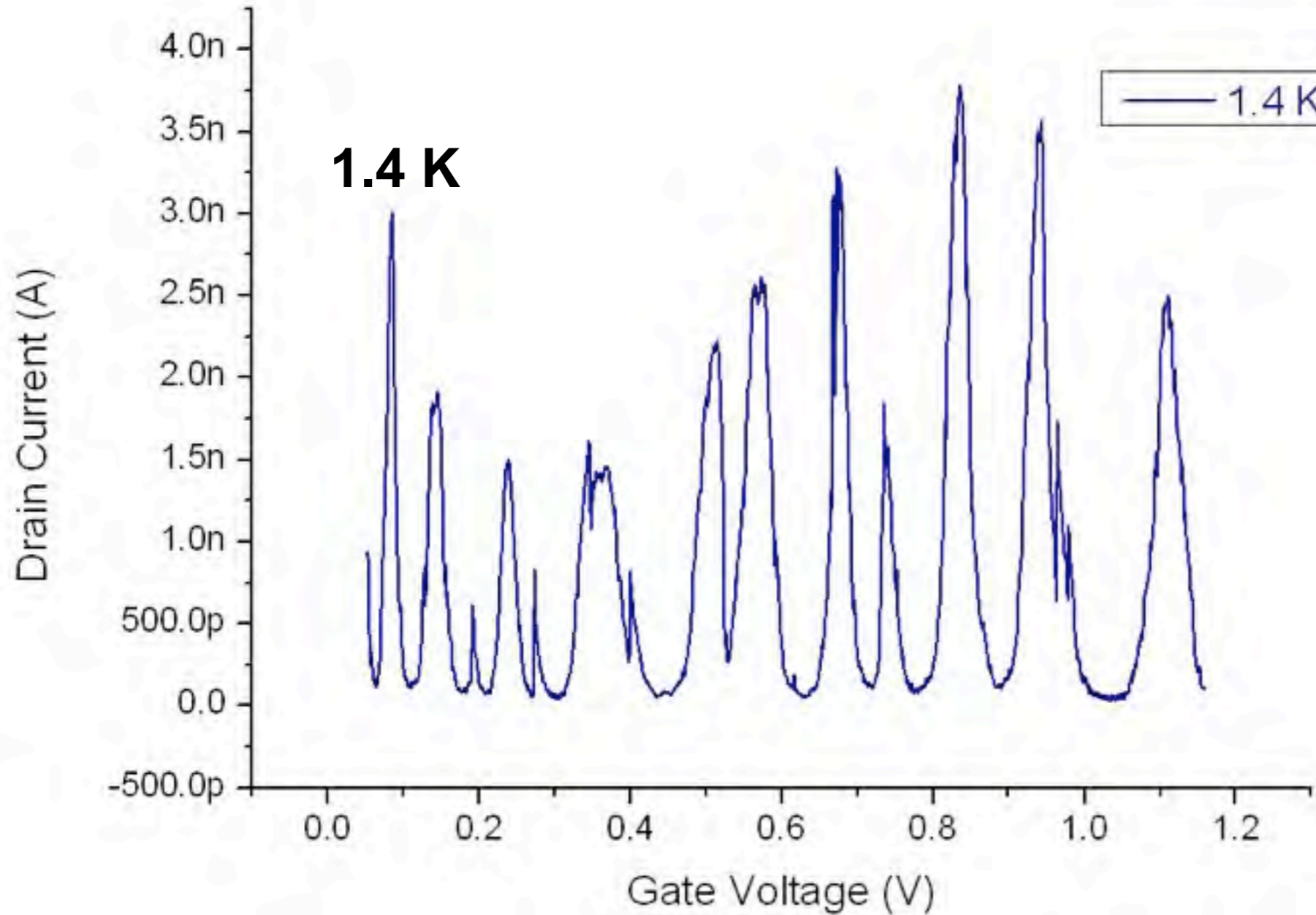
**Penrose tile: layer-to-layer
alignment 0.46 nm rms**



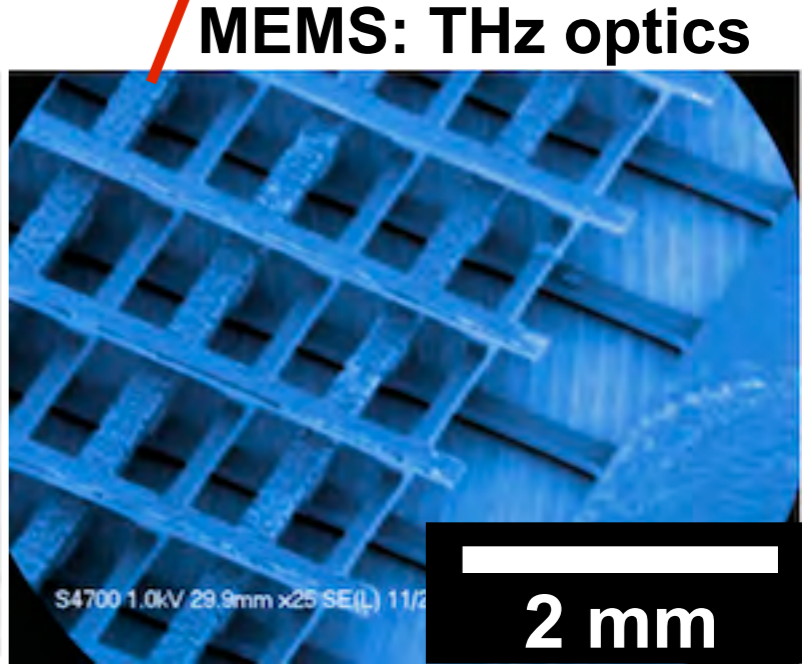
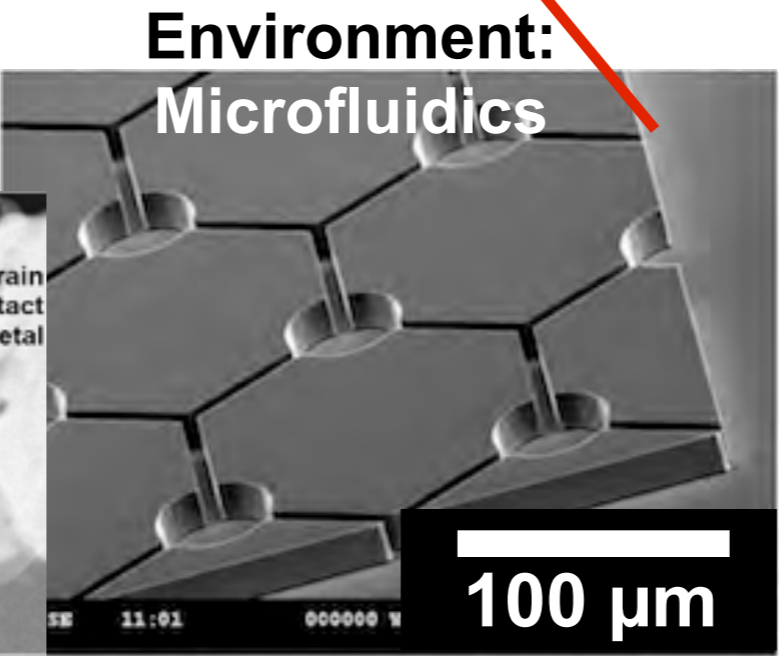
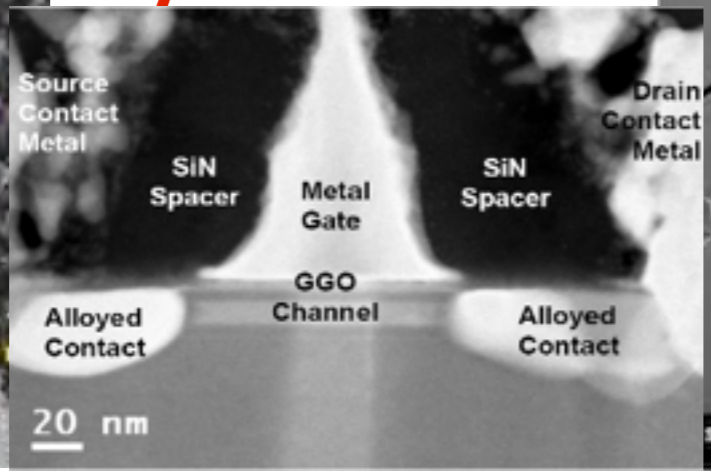
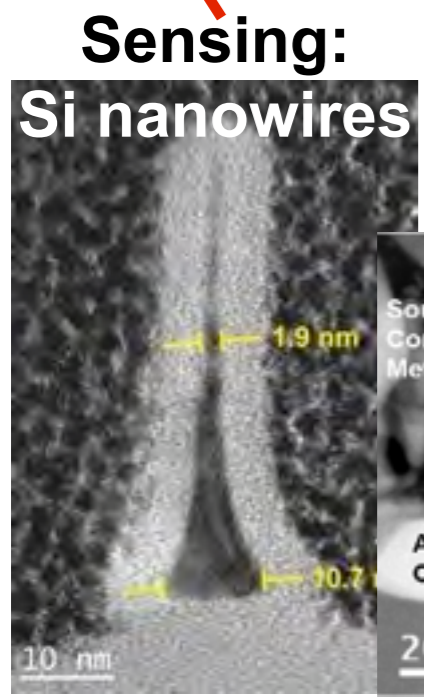
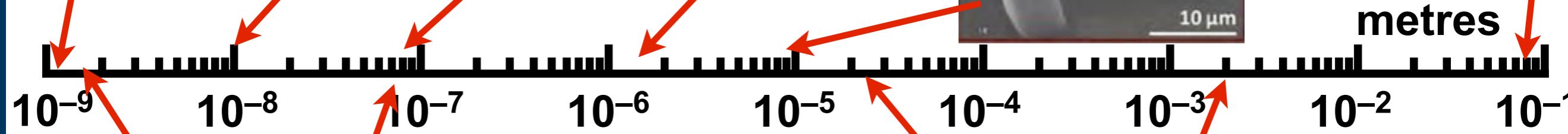
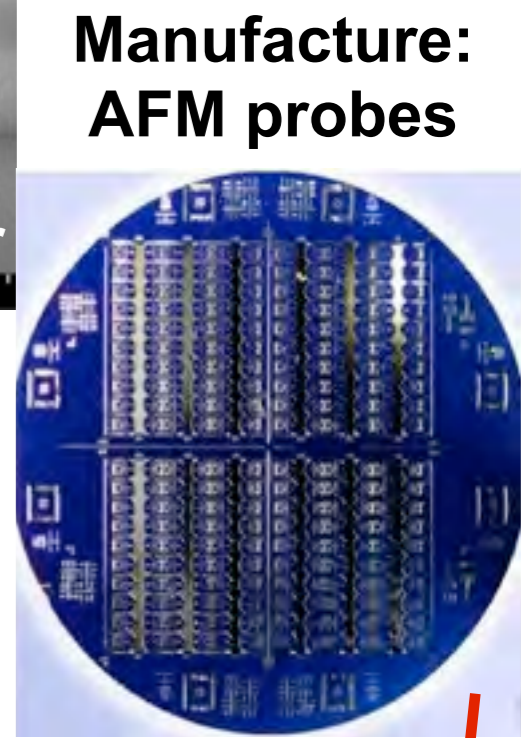
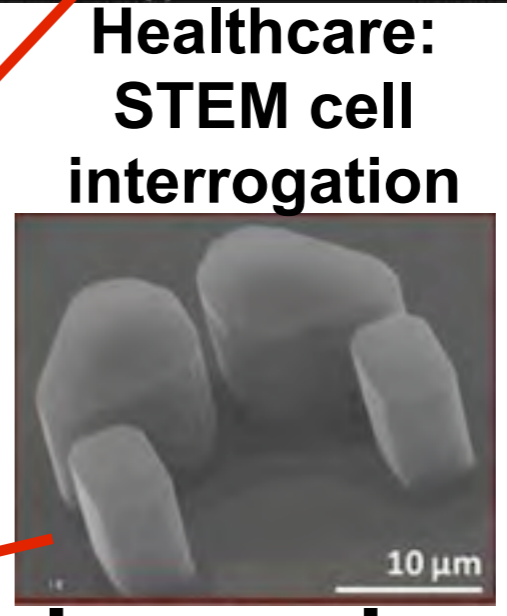
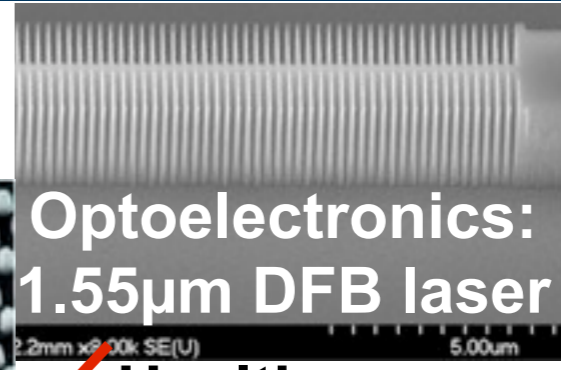
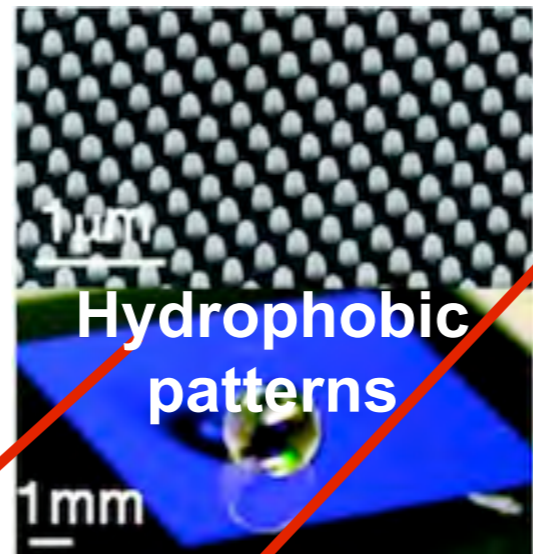
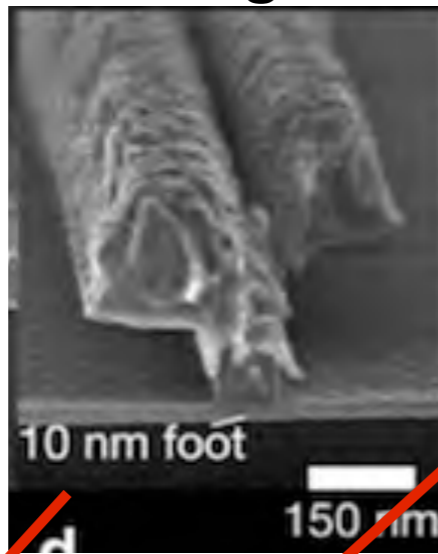
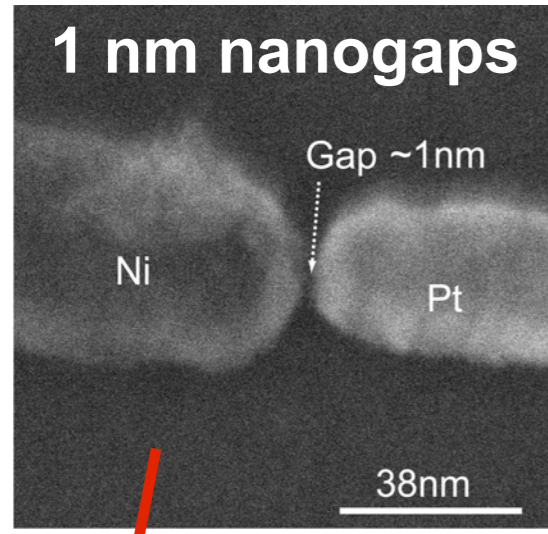
200 nm gate length
10 nm wide,
50 nm tall nanowire



Depletion mode nanowire



Nanoelectronics: 10 nm T-gate HEMT



- **History: Seebeck effect 1822**

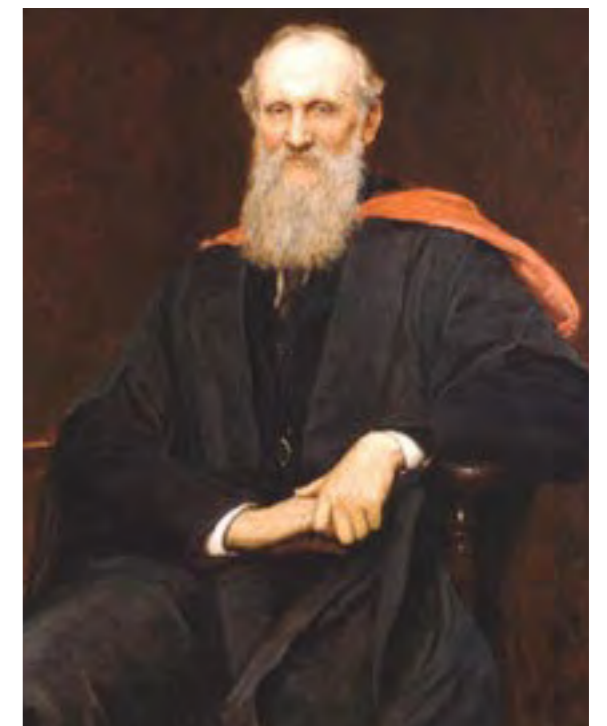


heat → electric current



- **Peltier (1834): current → cooling**

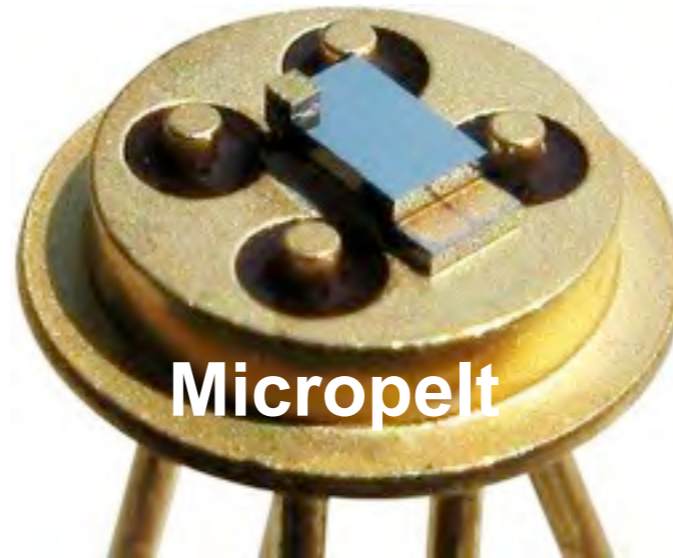
- **Thomson effect: Thomson (Lord Kelvin) 1852**



NASA Voyager I & II



Peltier cooler: telecoms lasers



Cars: replace alternator



Temperature control
for CO₂ sequestration



Buildings / industry temperature control
– autonomous sensing

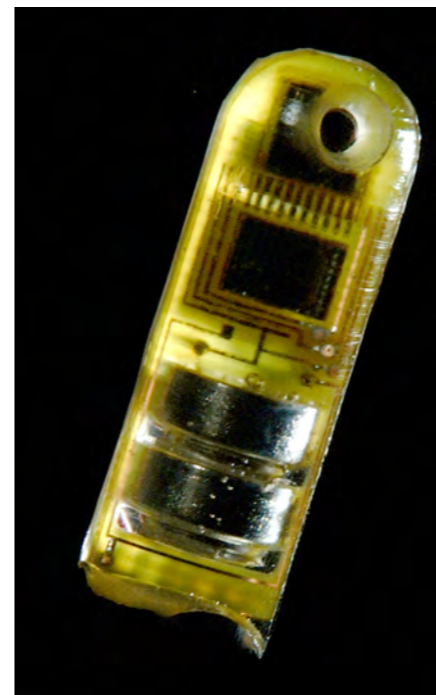
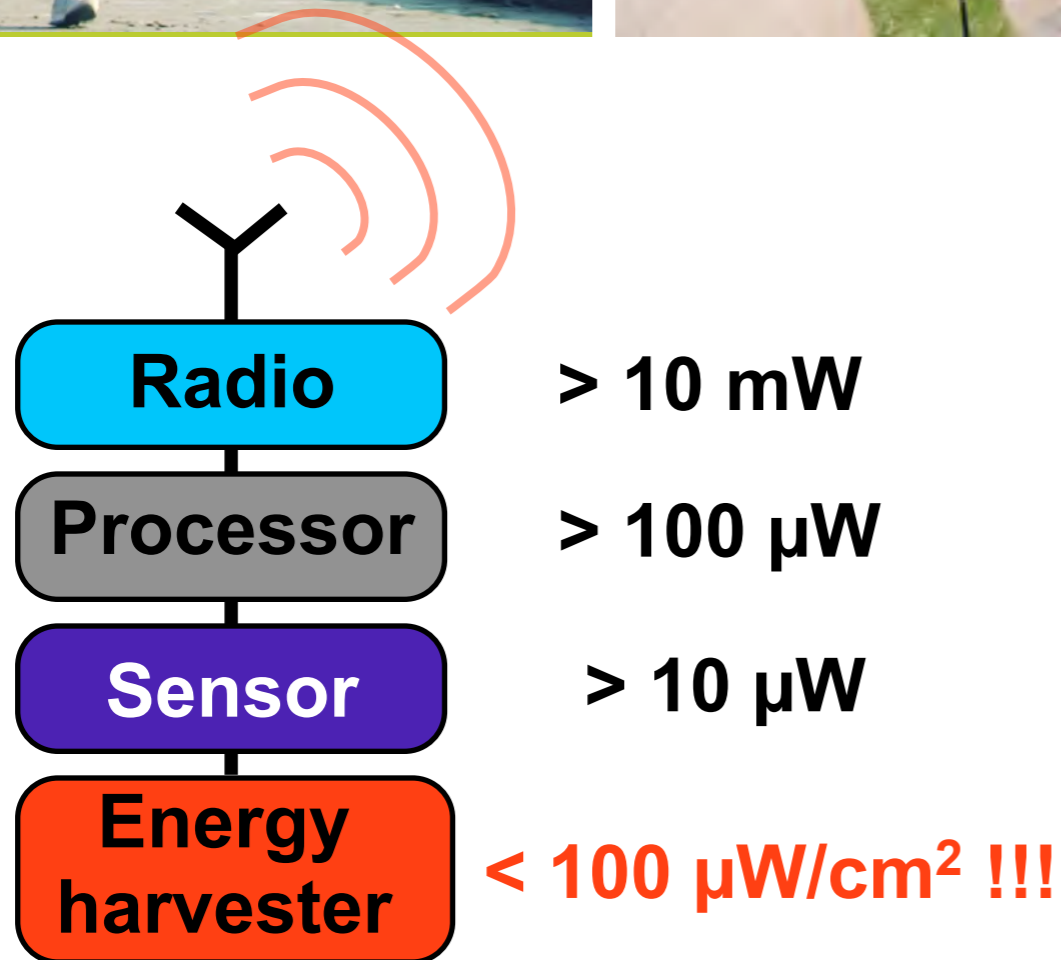
Sports performance sensors



Flood sensors



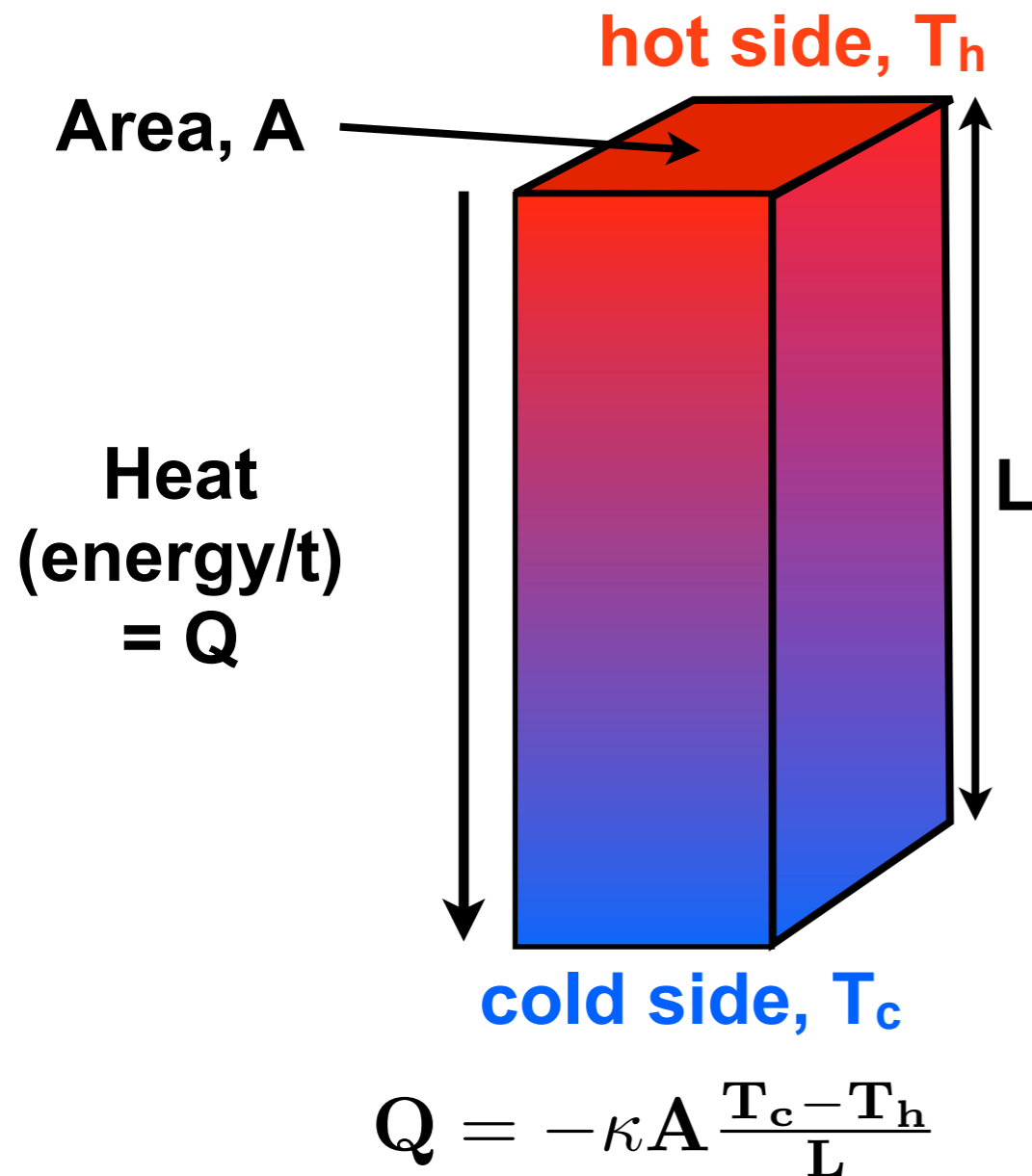
Weather monitoring



Battery free autonomous sensors: ECG, blood pressure, etc.

Fourier thermal transport

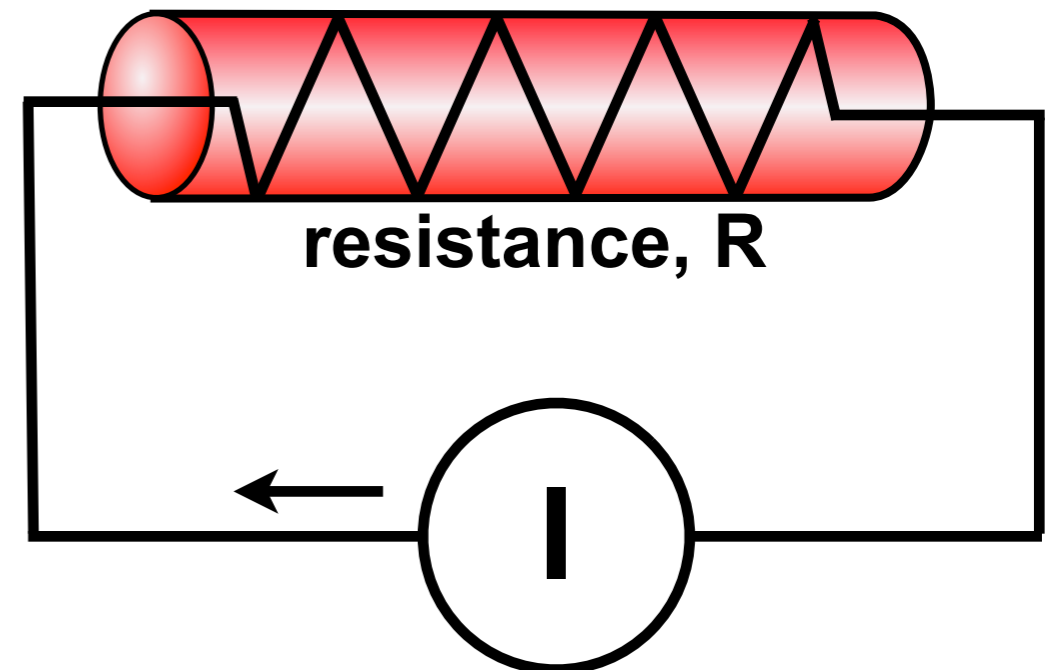
$$Q = -\kappa A \nabla T$$



Joule heating

$$Q = I^2 R$$

$Q = \text{heat (power i.e energy / time)}$



Fourier thermal transport

$$Q = -\kappa A \nabla T$$

Q = heat (power i.e energy / time)

E_F = chemical potential

V = voltage

A = area

q = electron charge

g(E) = density of states

k_B = Boltzmann's constant

Joule heating

$$Q = I^2 R$$

R = resistance

I = current (J = I/A)

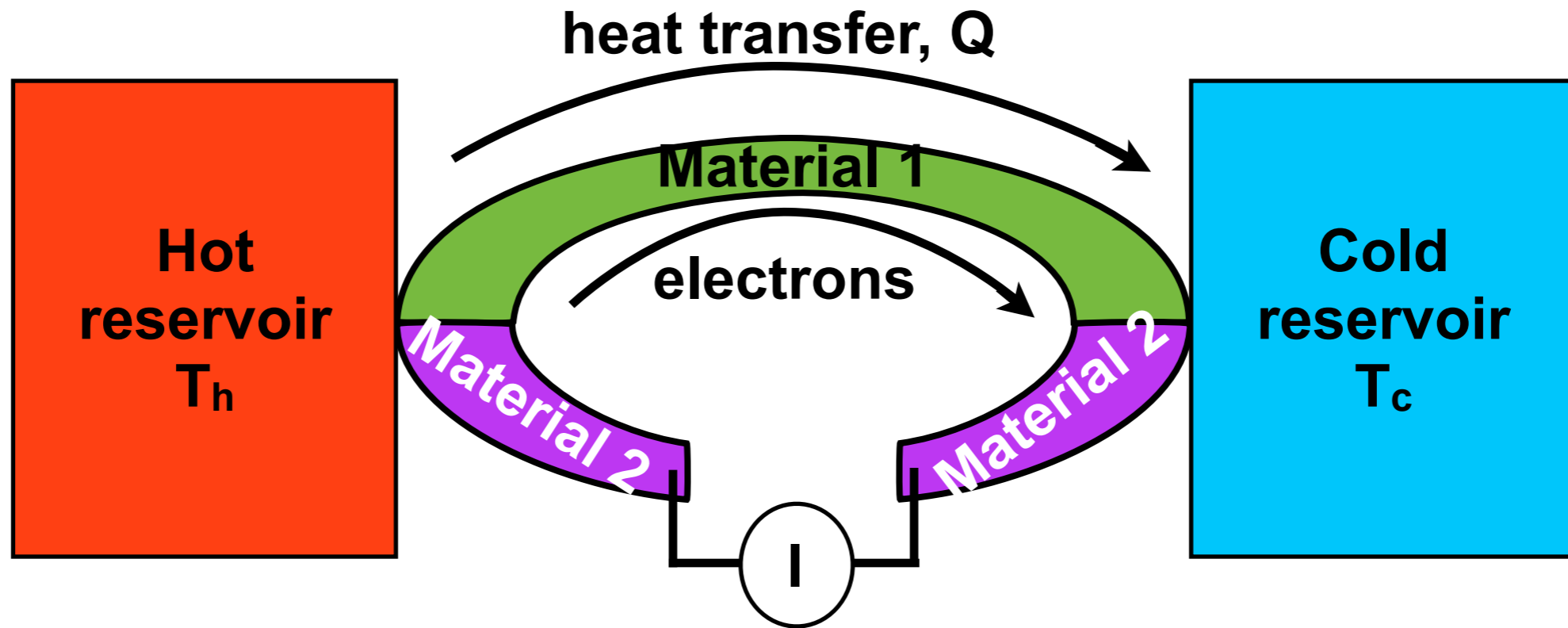
κ = thermal conductivity

σ = electrical conductivity

α = Seebeck coefficient

f(E) = Fermi function

$\mu(E)$ = mobility



Peltier coefficient, $\Pi = \frac{Q}{I}$

units: $W/A = V$



Peltier coefficient is the heat energy carried by each electron per unit charge & time

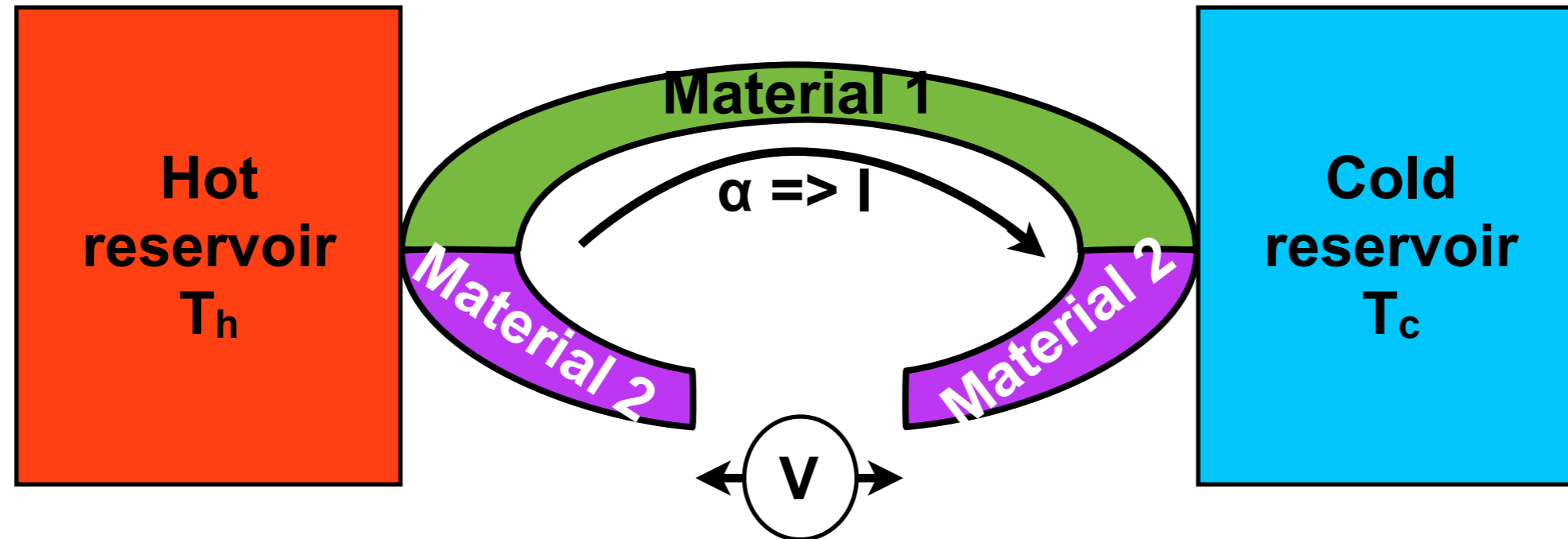
- **Full derivation uses relaxation time approximation & Boltzmann equation**

- $$\Pi = -\frac{1}{q} \int (\mathbf{E} - \mathbf{E}_F) \frac{\sigma(\mathbf{E})}{\sigma} d\mathbf{E}$$

- $$\sigma = \int \sigma(\mathbf{E}) d\mathbf{E} = q \int g(\mathbf{E}) \mu(\mathbf{E}) f(\mathbf{E}) [1 - f(\mathbf{E})] d\mathbf{E}$$

- **This derivation works well for high temperatures (> 100 K)**

- **At low temperatures phonon drag effects must be added**



- Open circuit voltage, $V = \alpha (T_h - T_c) = \alpha \Delta T$

Seebeck coefficient, $\alpha = \frac{dV}{dT}$

units: V/K

- Seebeck coefficient = $\frac{1}{q}$ x entropy $\left(\frac{Q}{T}\right)$ transported with electron

- Full derivation uses relaxation time approximation, Boltzmann equation

- $$\alpha = \frac{1}{qT} \left[\frac{\langle \mathbf{E}\tau \rangle}{\langle \tau \rangle} - E_F \right] \quad \tau = \text{momentum relaxation time}$$

- $$\alpha = -\frac{k_B}{q} \int \frac{(\mathbf{E} - E_F)}{k_B T} \frac{\sigma(\mathbf{E})}{\sigma} d\mathbf{E}$$

$$\sigma = \int \sigma(\mathbf{E}) d\mathbf{E} = q \int g(\mathbf{E}) \mu(\mathbf{E}) f(\mathbf{E}) [1 - f(\mathbf{E})] d\mathbf{E}$$

For electrons in the conduction band, E_c of a semiconductor

- $$\alpha = -\frac{k_B}{q} \left[\frac{E_c - E_F}{k_B T} + \frac{\int_0^\infty \frac{(\mathbf{E} - E_c)}{k_B T} \sigma(\mathbf{E}) d\mathbf{E}}{\int_0^\infty \sigma(\mathbf{E}) d\mathbf{E}} \right] \quad \text{for } E > E_c$$

- $f(1 - f) = -k_B T \frac{df}{dE}$

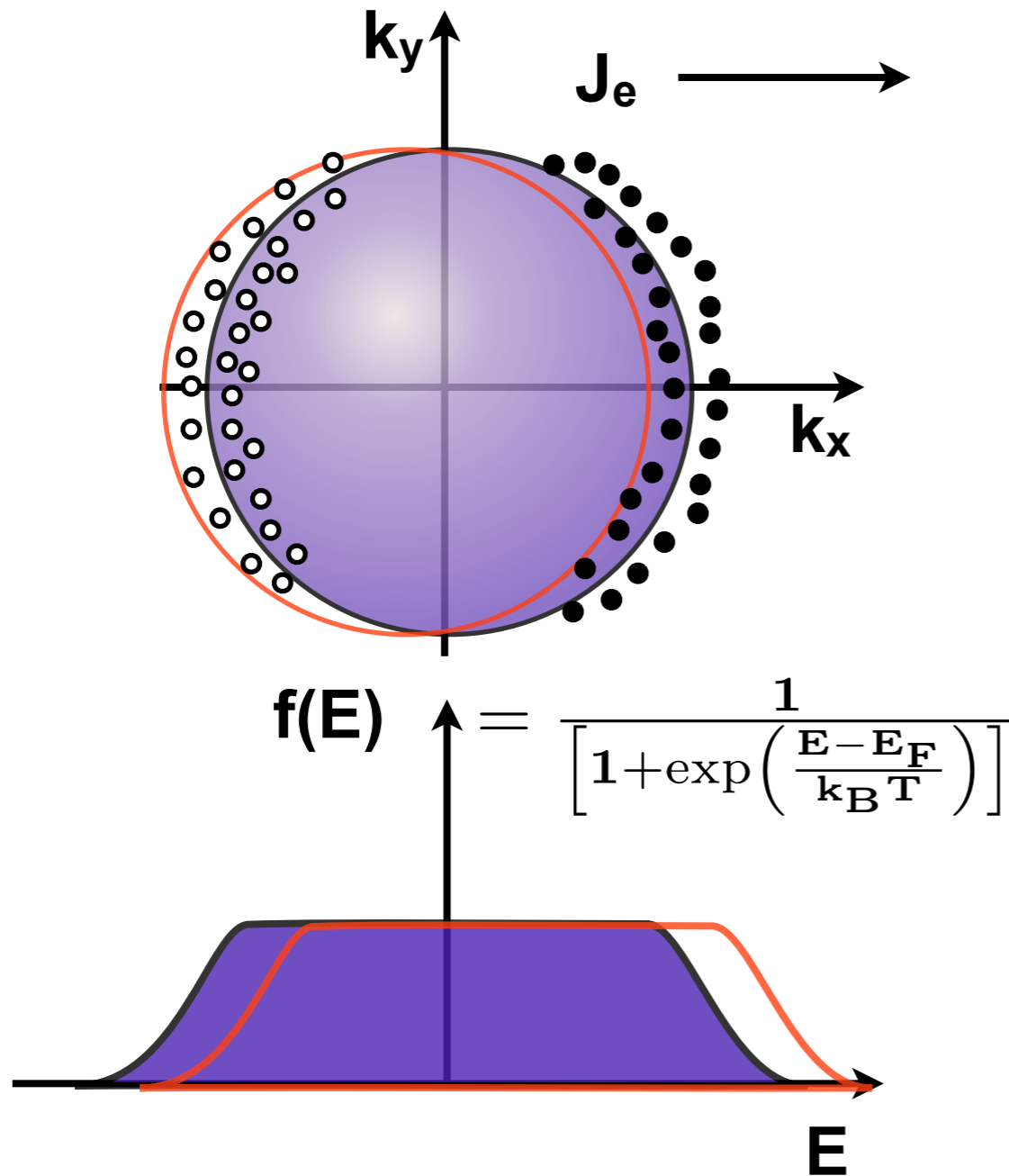
- **Expand $g(E)\mu(E)$ in Taylor's series at $E = E_F$**

- $$\alpha = -\frac{\pi^2}{3q} k_B^2 T \left[\frac{d \ln(\mu(E)g(E))}{dE} \right]_{E=E_F}$$
 (Mott's formula for metals)

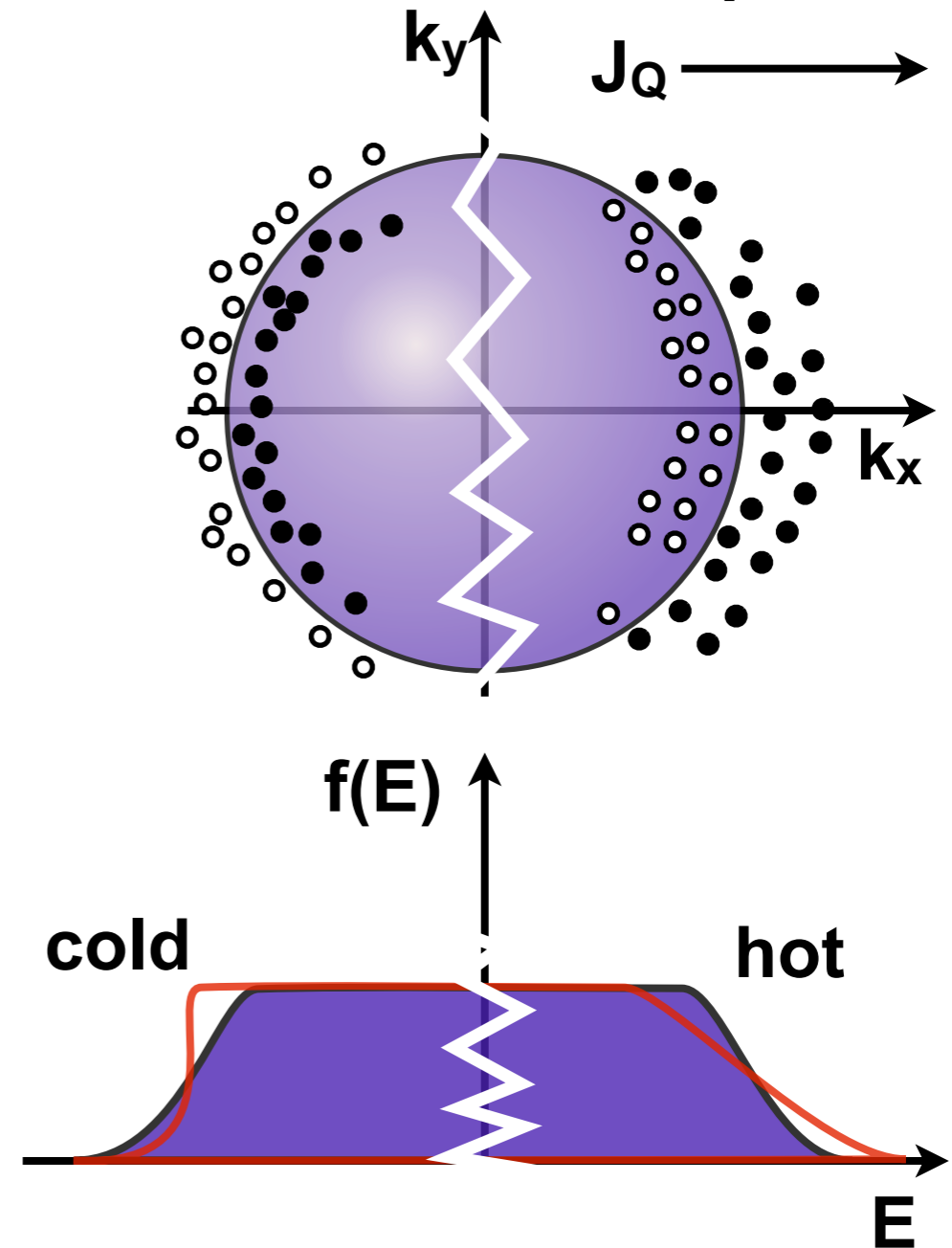
M. Cutler & N.F. Mott, Phys. Rev. 181, 1336 (1969)

- **i.e. Seebeck coefficient depends on the asymmetry of the current contributions above and below E_F**

3D electronic transport



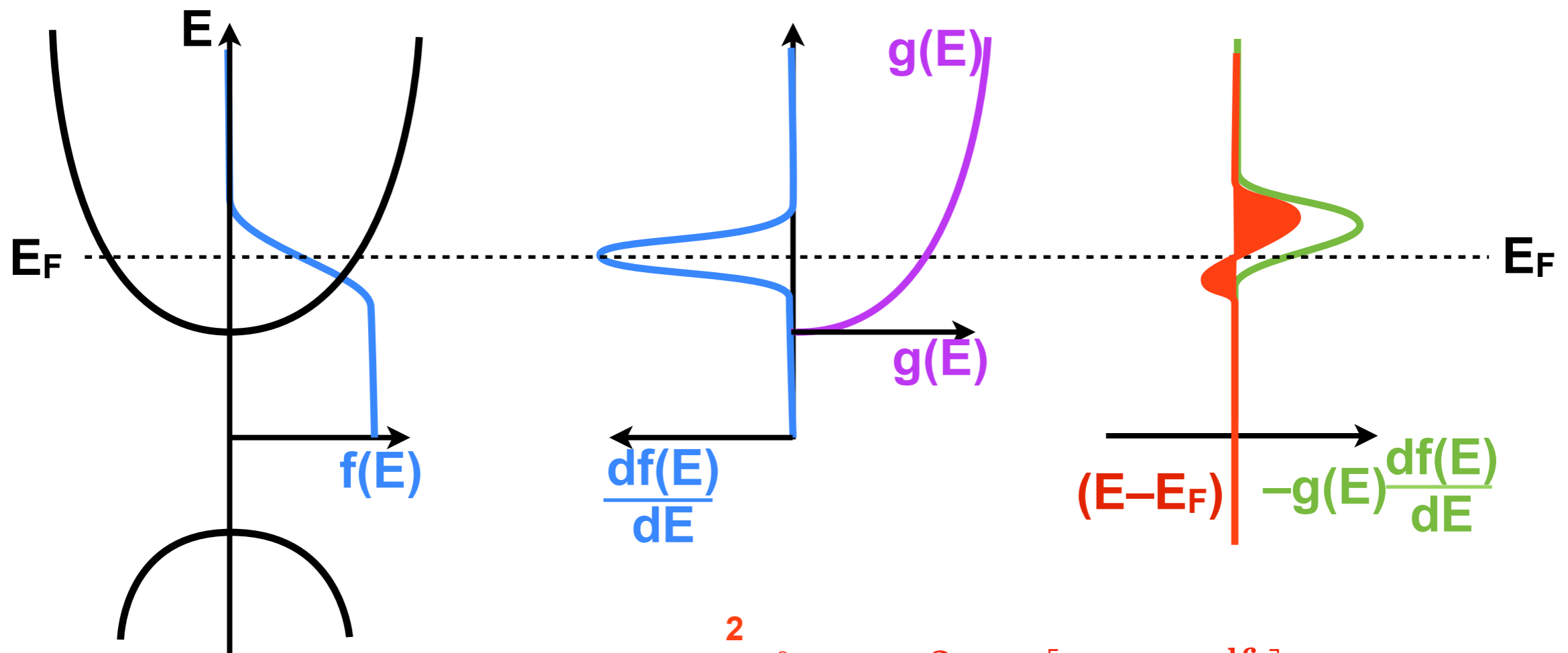
3D thermal transport





If we ignore energy dependent scattering (i.e. $\tau = \tau(E)$) then from J.M. Ziman

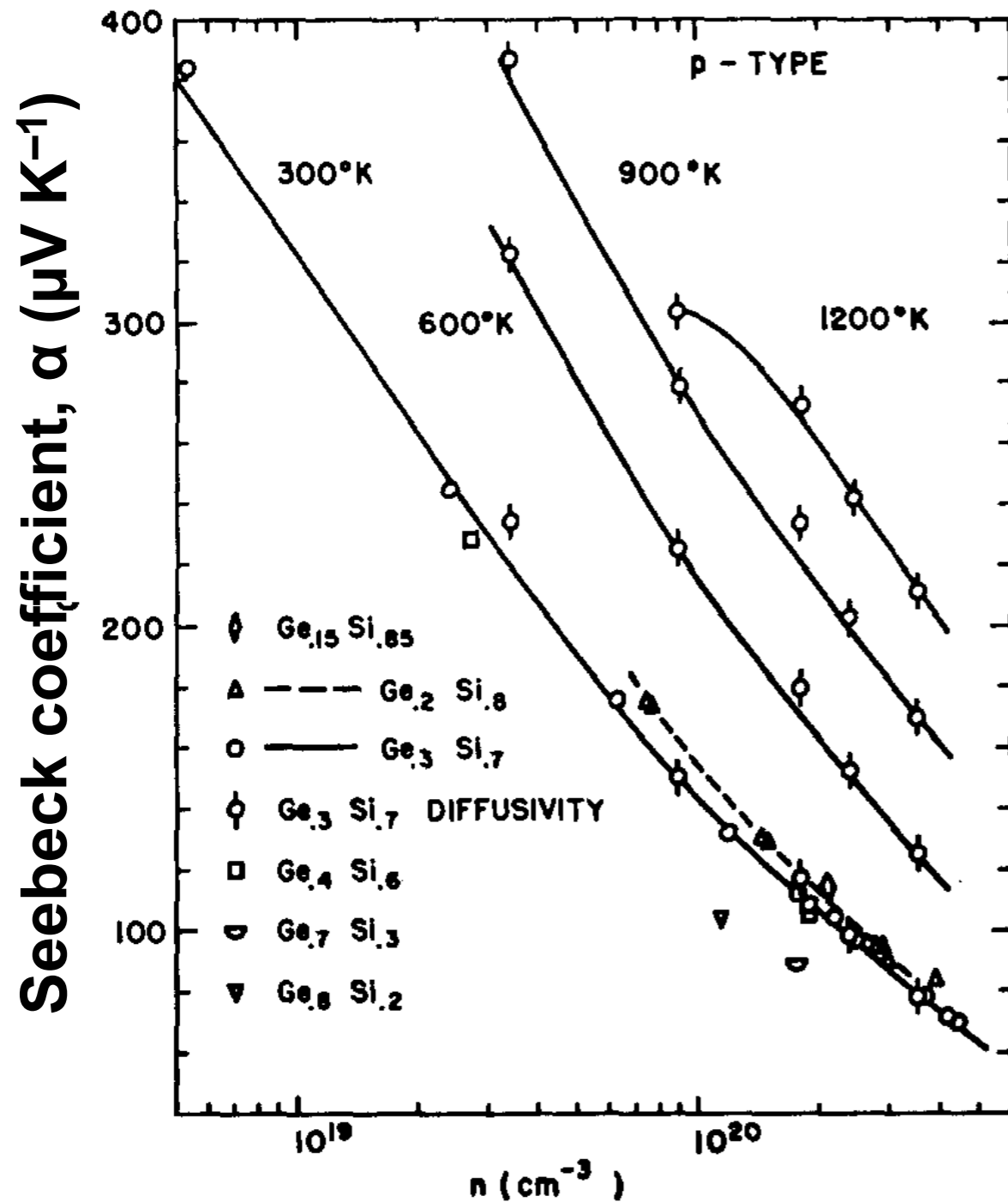
$$\sigma = \frac{q^2}{3} \int \tau(\mathbf{E}) \nu^2(\mathbf{E}) \left[-g(\mathbf{E}) \frac{df}{dE} \right] dE$$



$$\alpha = \frac{q}{3T\sigma} \int \tau(\mathbf{E}) \nu^2(\mathbf{E}) \left[-g(\mathbf{E}) \frac{df}{dE} \right] (E - E_F) dE$$



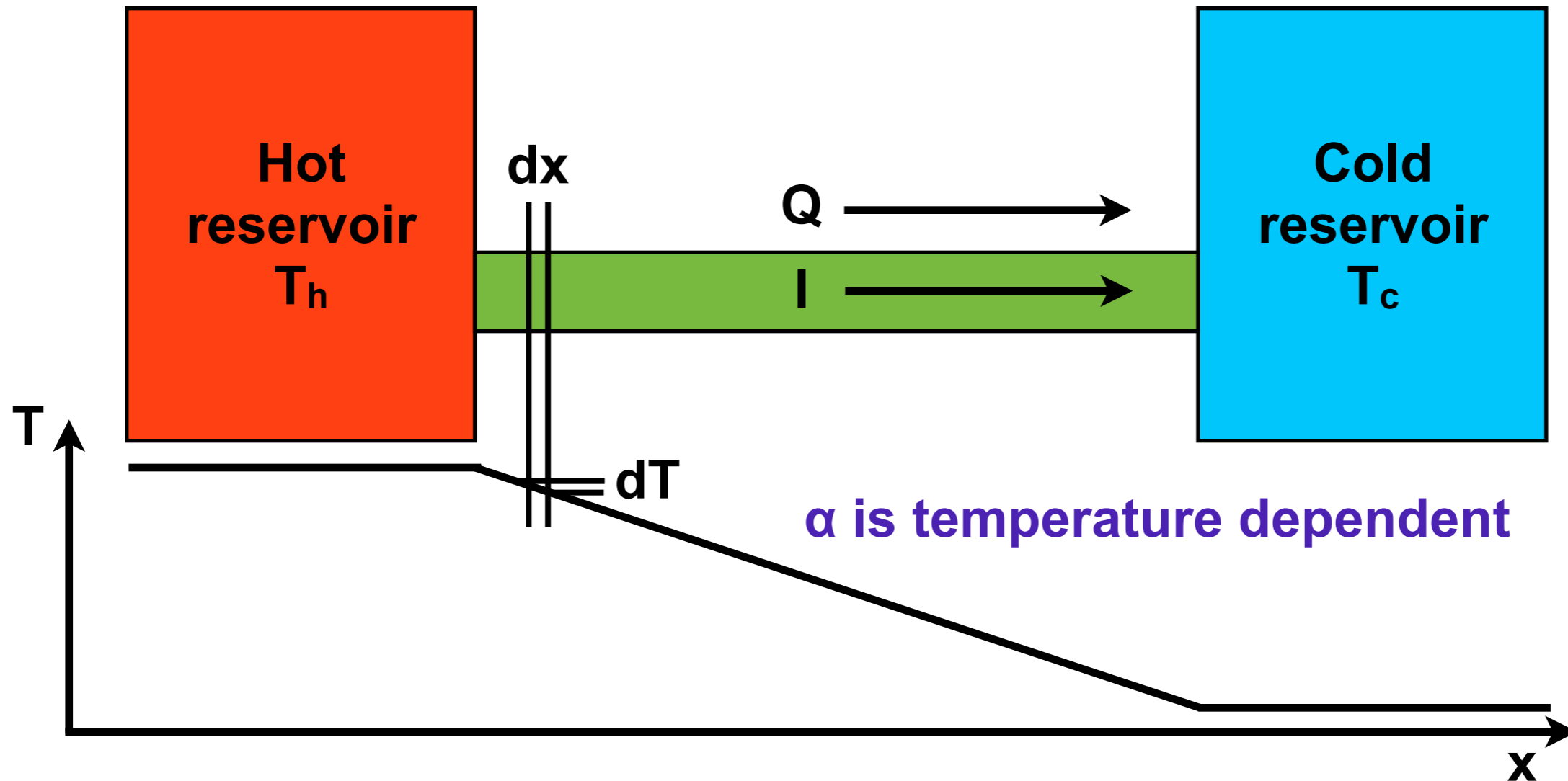
Thermoelectric power requires asymmetry in red area under curve



- Mott criteria $\sim 2 \times 10^{18} \text{ cm}^{-3}$
- Degenerately doped p- $\text{Si}_{0.7}\text{Ge}_{0.3}$
- α decreases for higher n
- For SiGe, α increases with T

$$\alpha = \frac{8\pi^2 k_B^2}{3eh^2} m^* T \left(\frac{\pi}{3n} \right)^{\frac{2}{3}}$$

The Thomson Effect



● $\frac{dQ}{dx} = \beta I \frac{dT}{dx}$

Thomson coefficient, β : $dQ = \beta I dT$

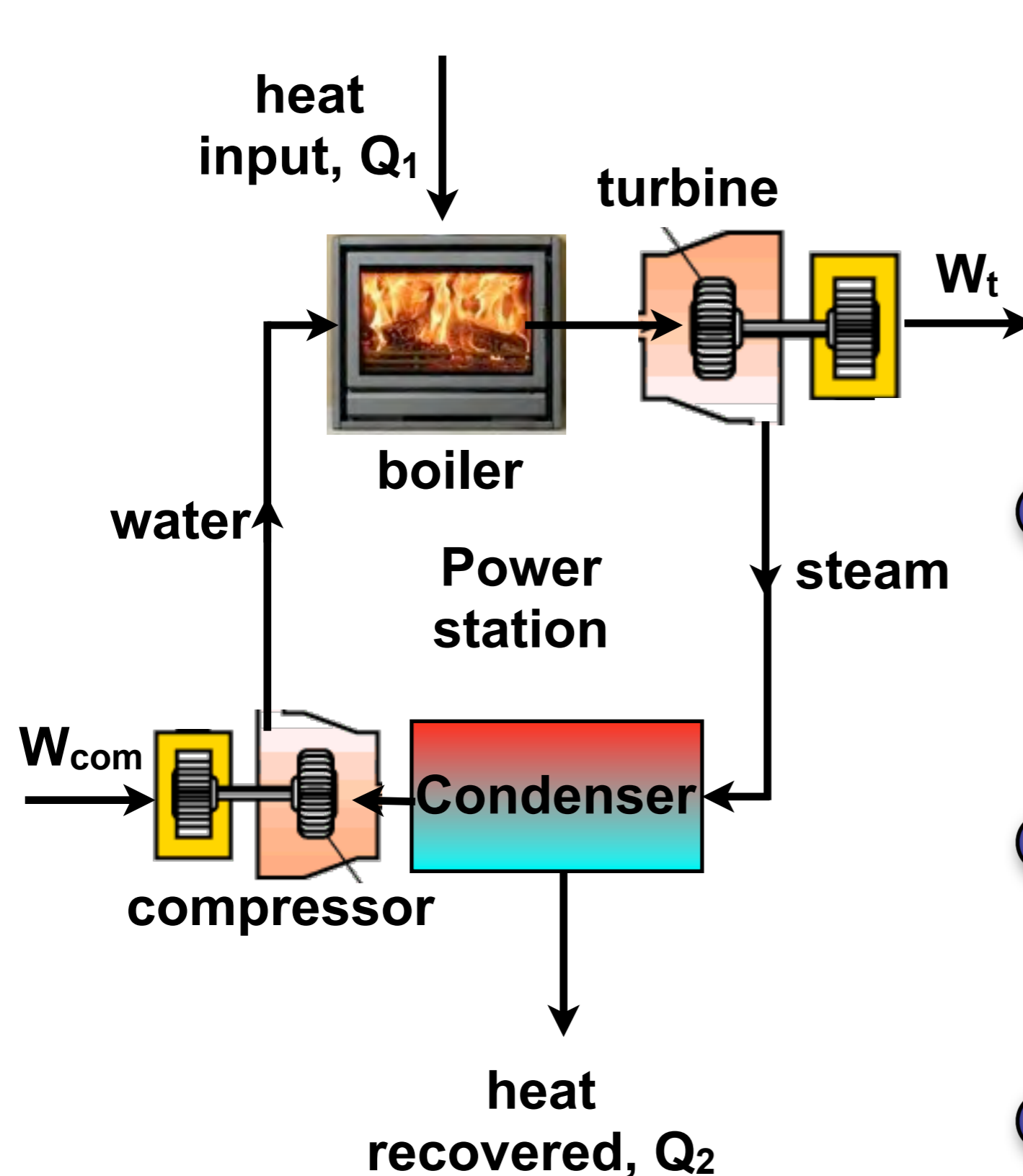
units: V/K

- Derived using irreversible thermodynamics

$$\Pi = \alpha T$$

$$\beta = T \frac{d\alpha}{dT}$$

- These relationships hold for all materials
- Seebeck, α is easy to measure experimentally
- Therefore measure α to obtain Π and β



$$\text{Efficiency} = \eta = \frac{\text{net work output}}{\text{heat input}}$$

$$= \frac{W_t - W_{com}}{Q_1}$$

● 1st law thermodynamics
 $(Q_1 - Q_2) - (W_t - W_{com}) = 0$

● $\eta = \frac{Q_1 - Q_2}{Q_1}$

● $\eta = 1 - \frac{Q_2}{Q_1}$

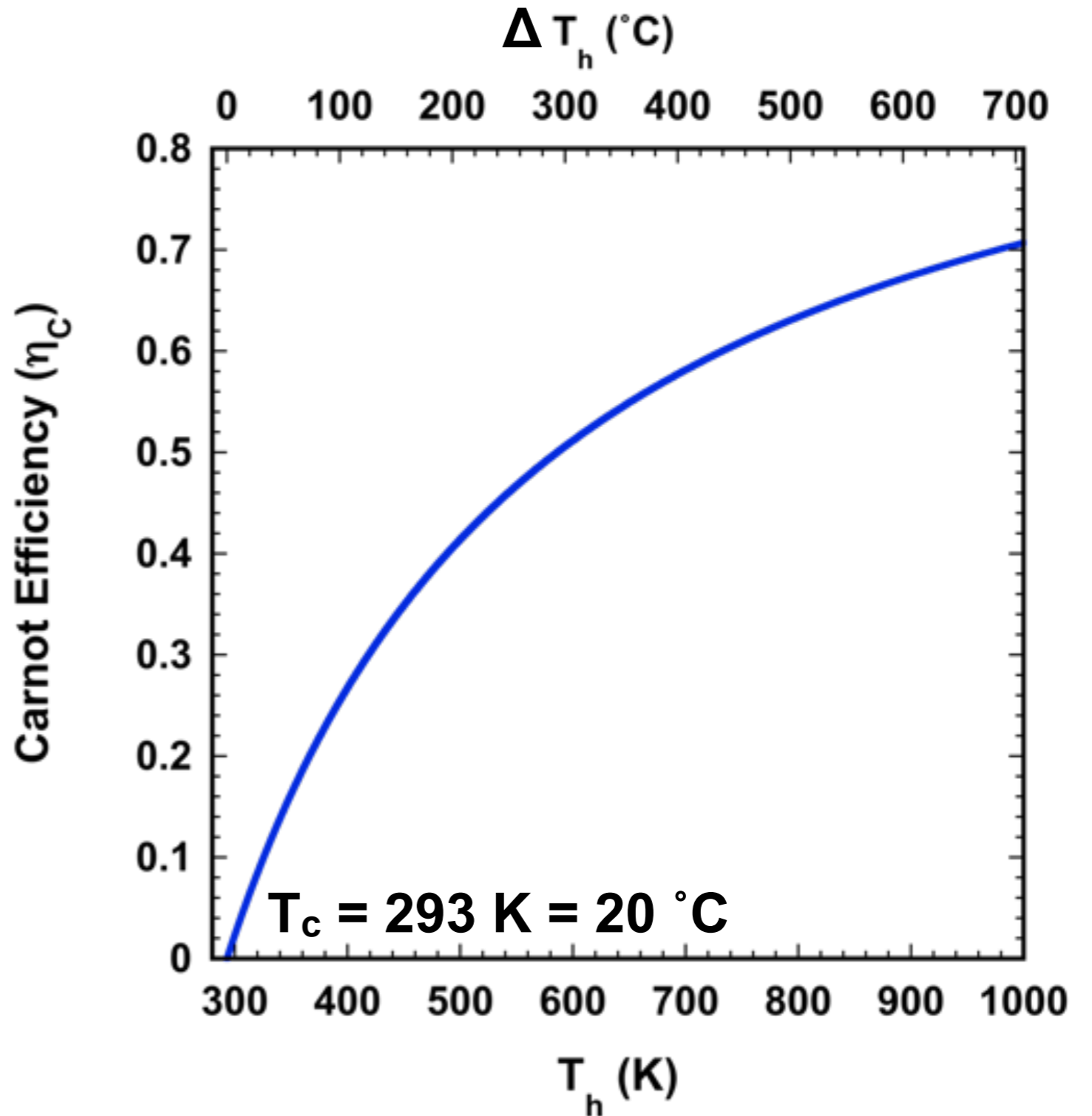
Efficiency =

$$\eta = \frac{\text{net work output}}{\text{heat input}}$$

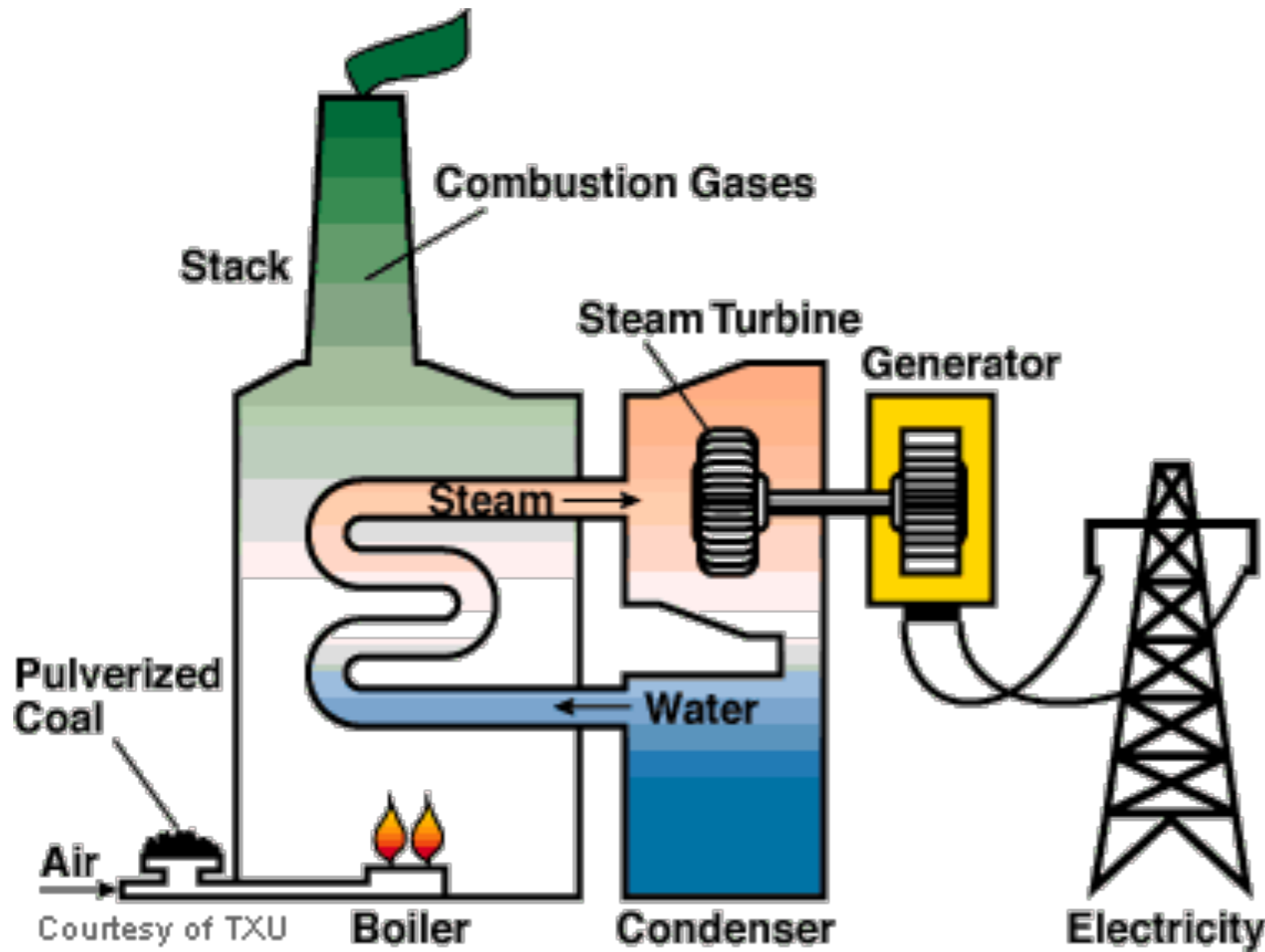
$$\eta = 1 - \frac{Q_2}{Q_1}$$

Carnot: maximum η only
depends on T_c and T_h

$$\eta_c = 1 - \frac{T_c}{T_h}$$



Higher temperatures give higher efficiencies



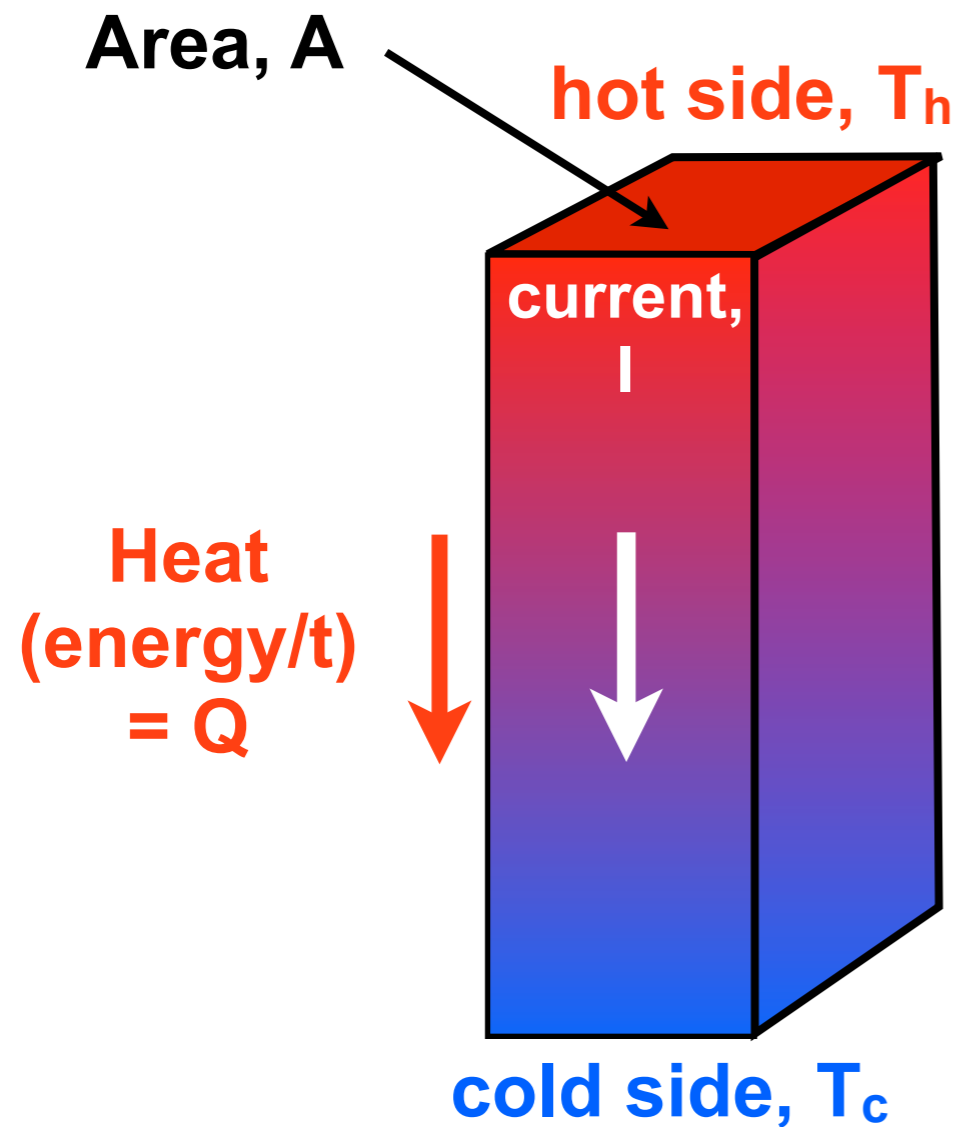
The Rankine Cycle



William John Macquorn Rankine

Energy stored in fuel → heat → kinetic energy → electric energy

- If a current of I flows through a thermoelectric material between hot and cold reservoirs:



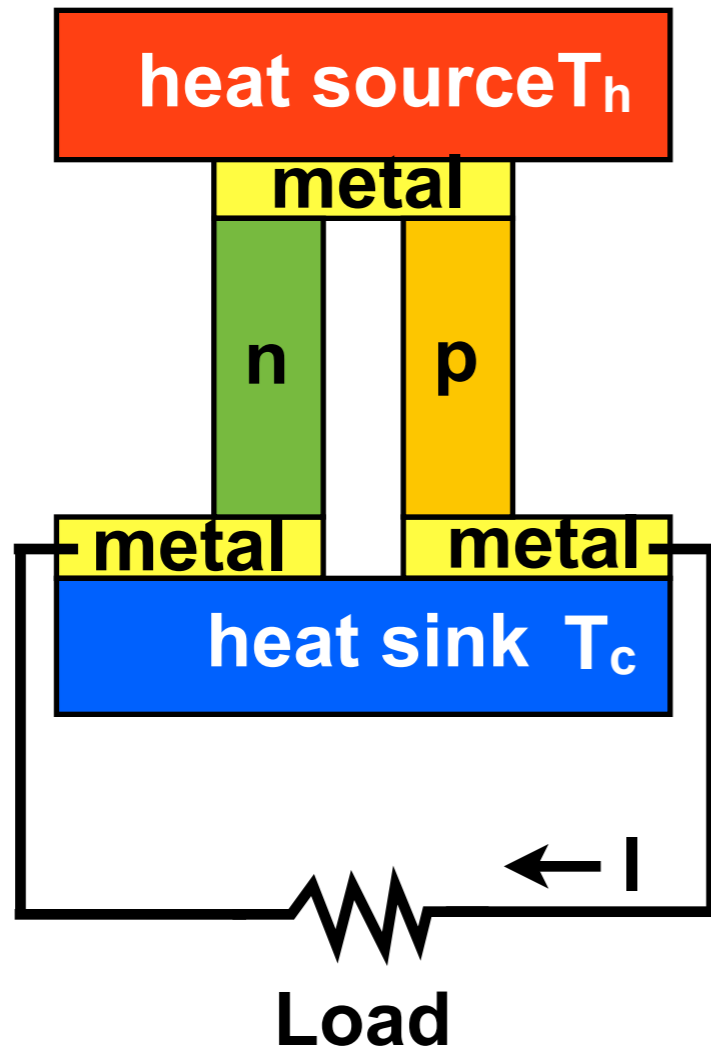
- Heat flux per unit area =
(= Peltier + Fourier)

- $$\frac{Q}{A} = \Pi J - \kappa \nabla T$$

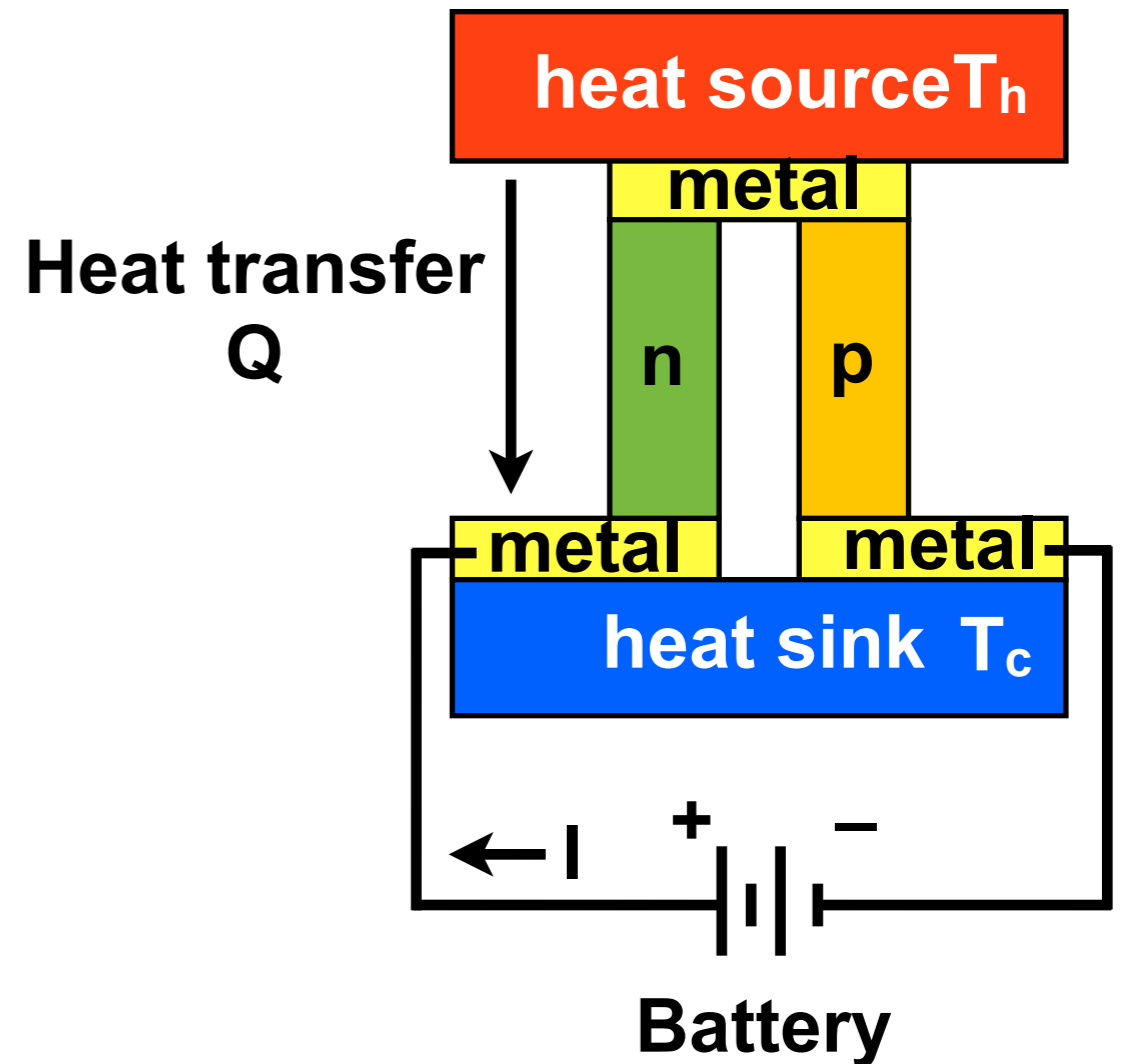
but $\Pi = \alpha T$ and $J = \frac{I}{A}$

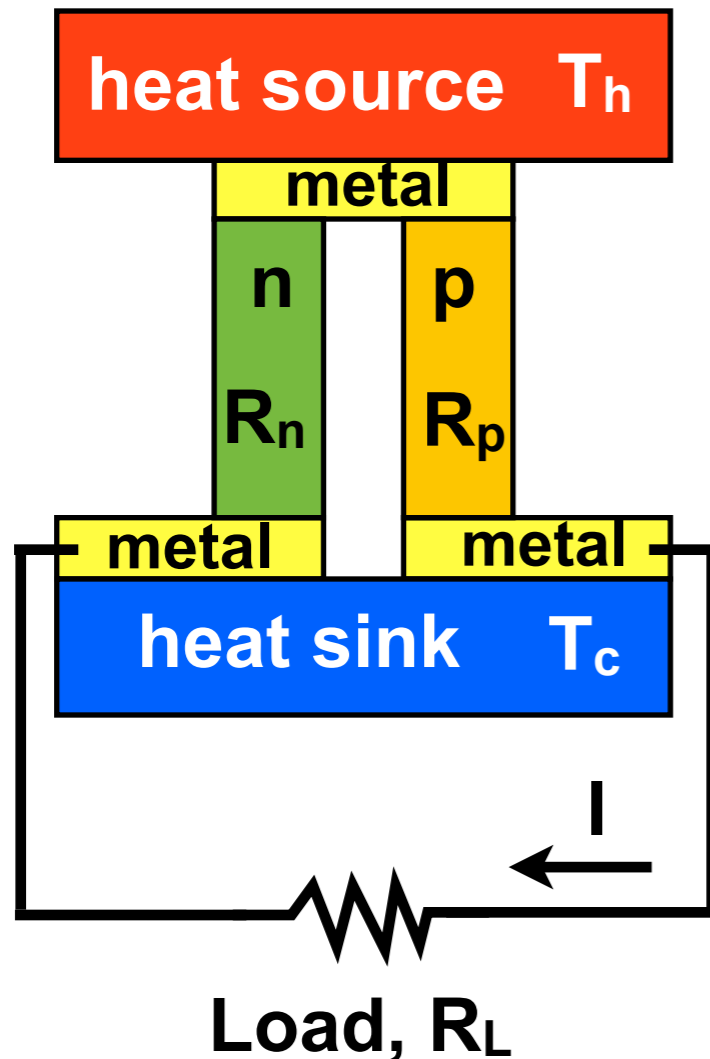
$$Q = \alpha IT - \kappa A \nabla T$$

**Seebeck effect:
electricity
generation**



**Peltier effect:
electrical cooling
i.e. heat pump**





$$R = R_n + R_p$$

- $\eta = \frac{\text{power supplied to load}}{\text{heat absorbed at hot junction}}$
- Power to load (Joule heating) = $I^2 R_L$
- Heat absorbed at hot junction = Peltier heat + heat withdrawn from hot junction
- Peltier heat = $\Pi I = \alpha I T_h$
- $I = \frac{\alpha(T_h - T_c)}{R + R_L}$ (Ohms Law)
- Heat withdrawn from hot junction
 $= \kappa A (T_h - T_c) - \frac{1}{2} I^2 R$
 ↑
 NB half Joule heat returned to hot junction

● $\eta = \frac{\text{power supplied to load}}{\text{heat absorbed at hot junction}}$

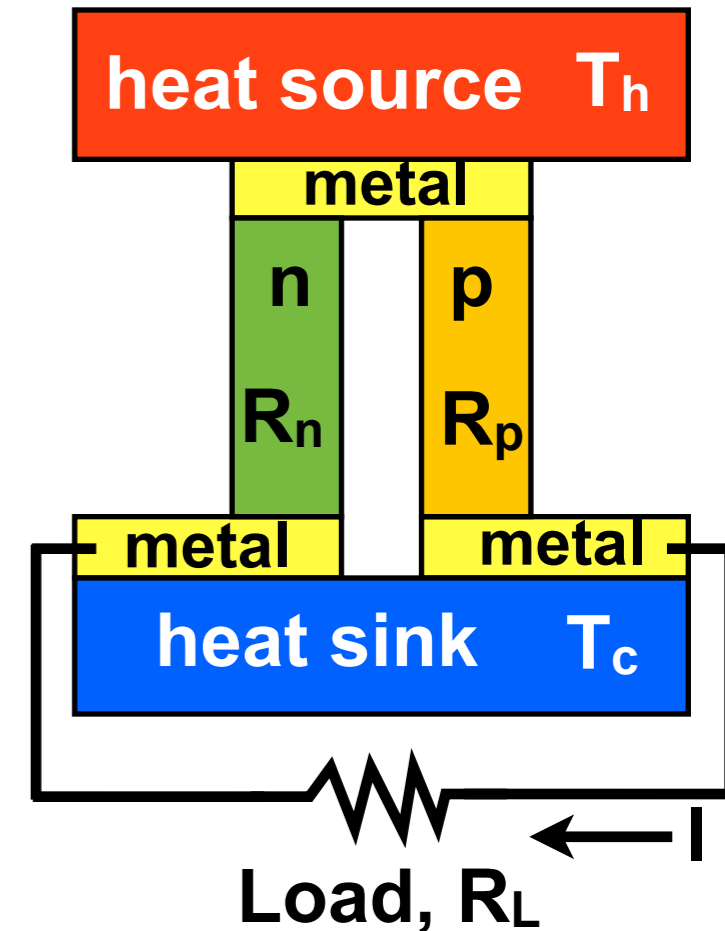
$= \frac{\text{power supplied to load}}{\text{Peltier} + \text{heat withdrawn}}$

$$\eta = \frac{I^2 R_L}{\alpha I T_h + \kappa A (T_h - T_c) - \frac{1}{2} I^2 R}$$

● For maximum value $\frac{d\eta}{d(\frac{R_L}{R})} = 0$

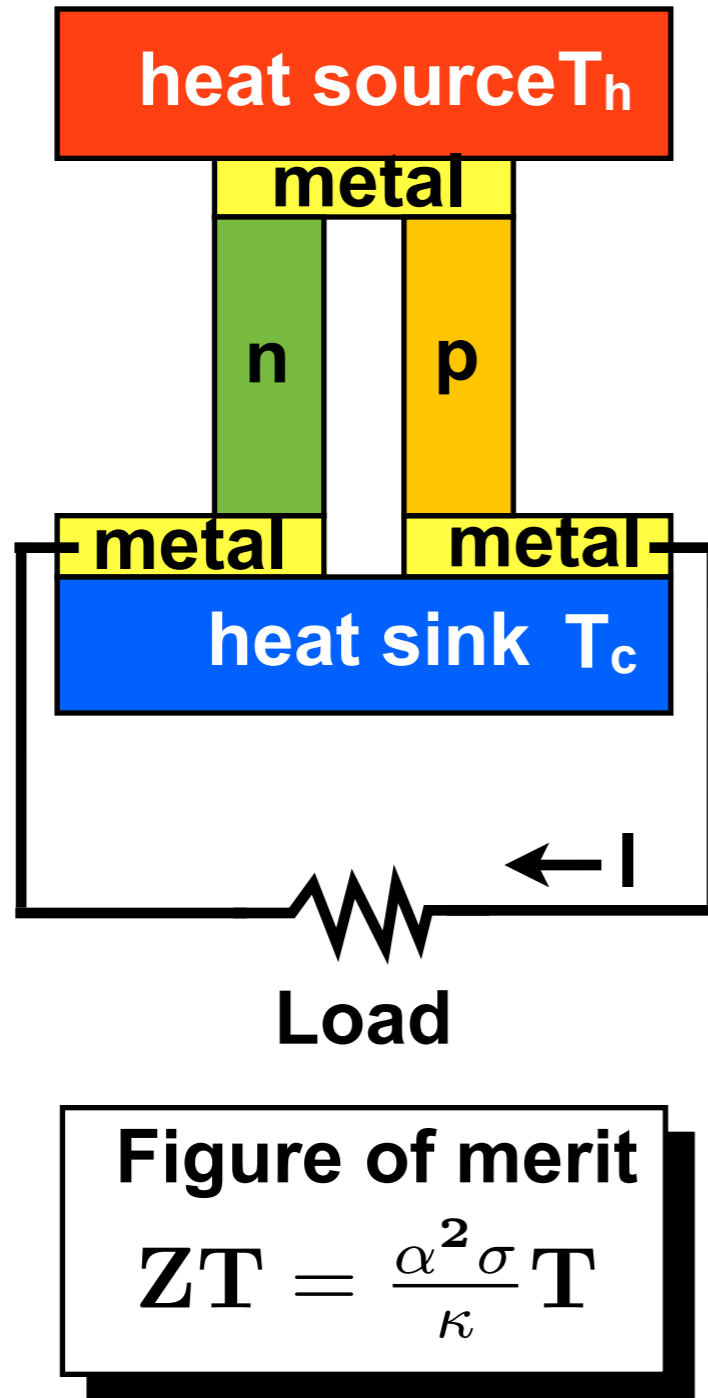
$$\eta_{\max} = \frac{T_h - T_c}{T_h} \frac{\sqrt{1 + ZT} - 1}{\sqrt{1 + ZT} + \frac{T_c}{T_h}}$$

= **Carnot** x **Joule losses and irreversible processes**



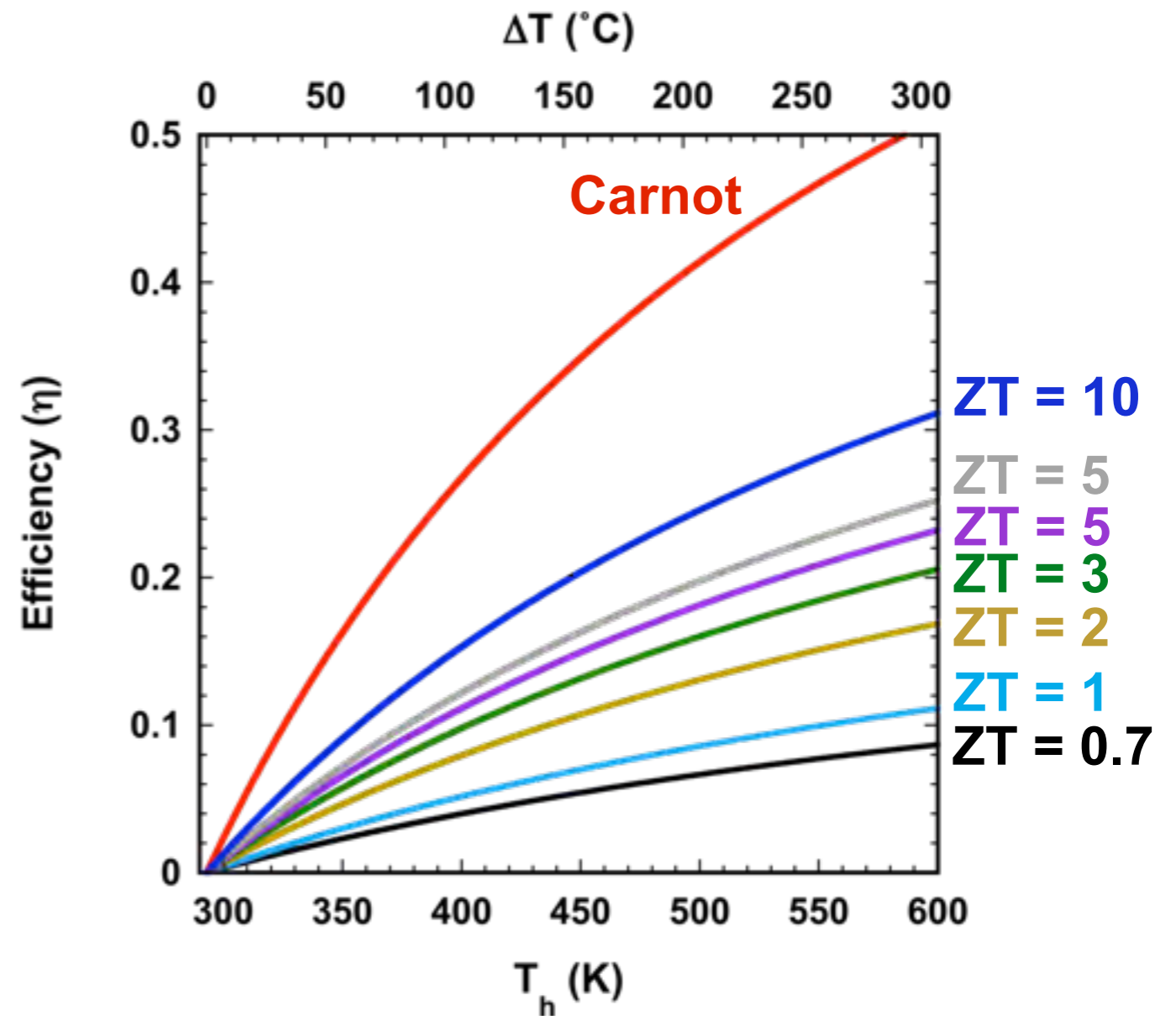
$$T = \frac{1}{2} (T_h + T_c)$$

where $Z = \frac{\alpha^2}{R\kappa A} = \frac{\alpha^2 \sigma}{\kappa}$

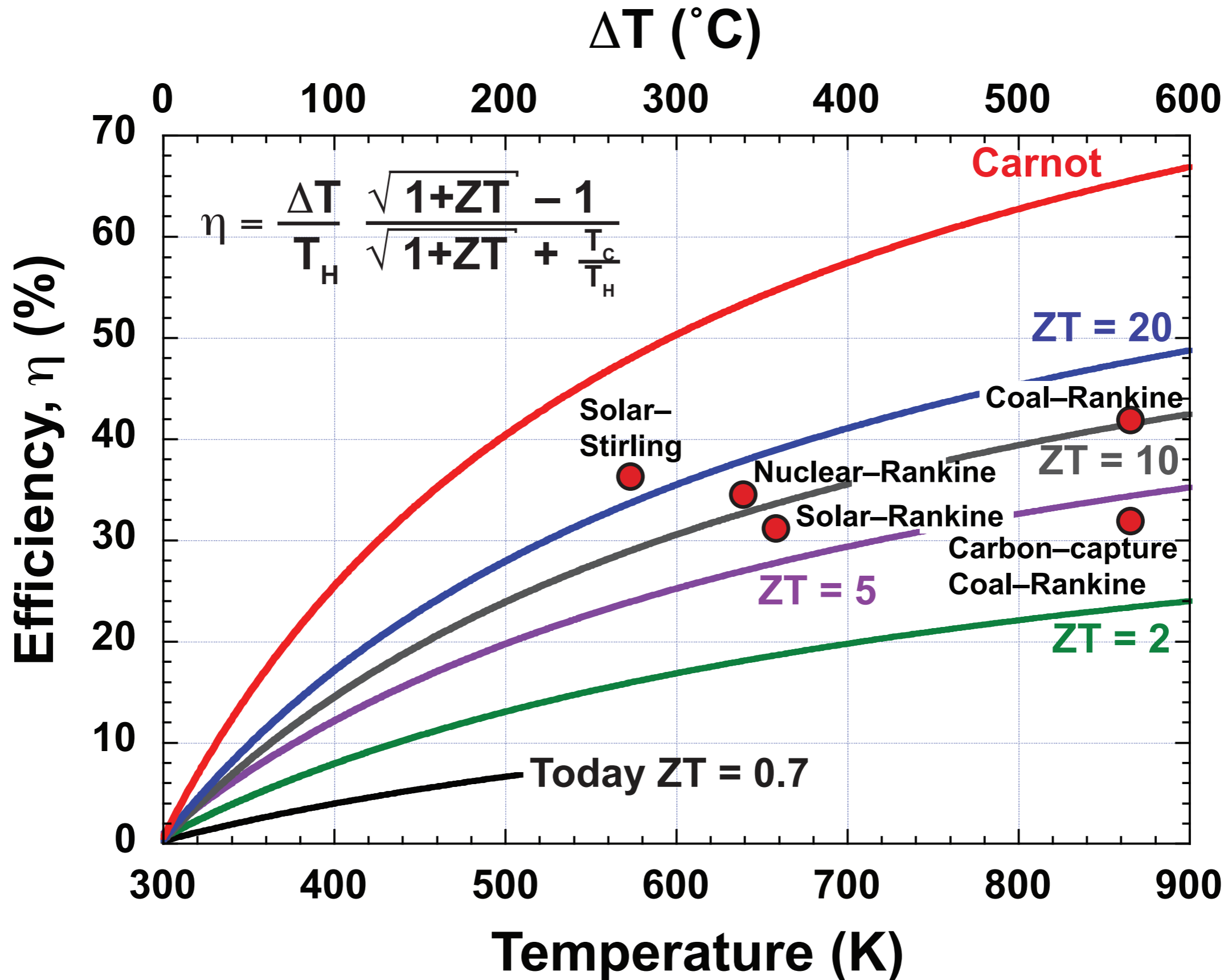


Power factor = $\alpha^2 \sigma$

$$\eta = \frac{\Delta T}{T_h} \frac{\sqrt{1 + ZT} - 1}{\sqrt{1 + ZT} + \frac{T_c}{T_h}}$$

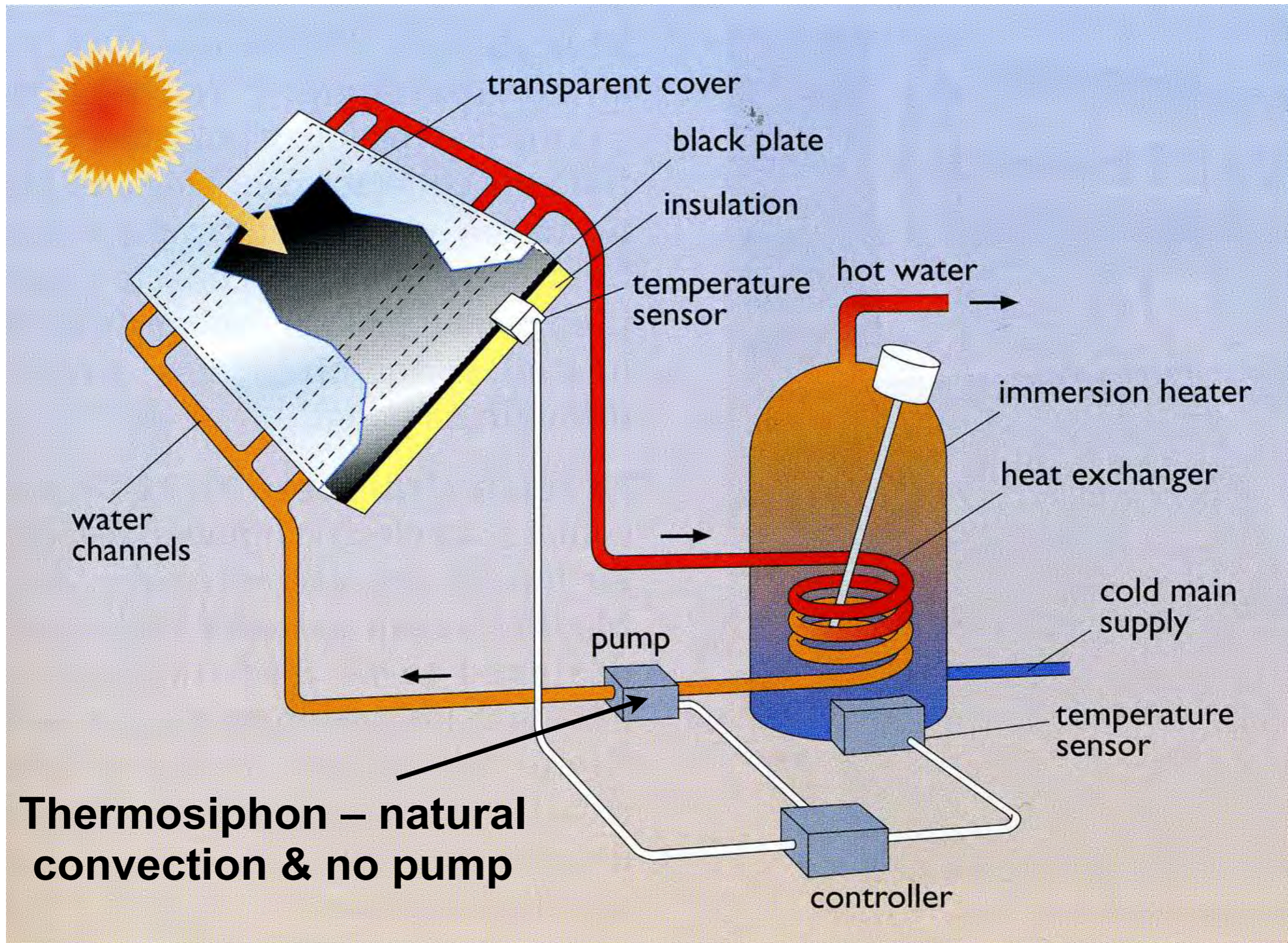


Impedance matching and maximum power point tracking are key for thermoelectrics



| |
|------------------------|
| Highest Quality |
| Electromagnetic |
| Mechanical (kinetic) |
| Photon (light) |
| Chemical |
| Heat (thermal) |
| Lowest Quality |

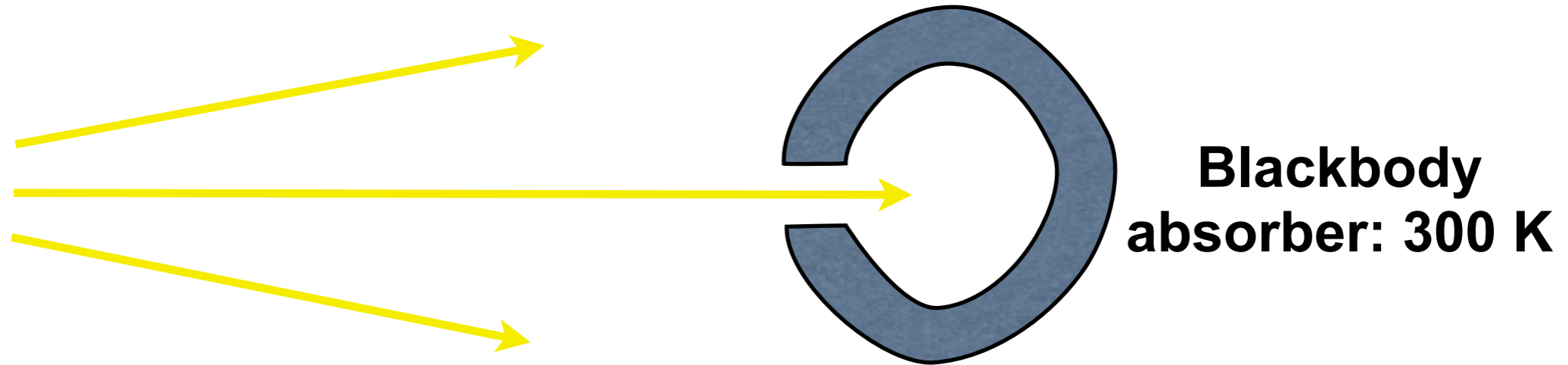
- First proposed as **availability** by Kelvin in 1851 refined by Ohta
- Energy quality describes the ease (i.e. η) with which energy can be transformed
- A transition down the table will be more efficient than moving up the table
- Therefore solar heating is more efficient than photovoltaic electrical generation
- Expanded version from chemistry developed by Odum



● 46% to 74% η for solar energy \rightarrow heat conversion are typical

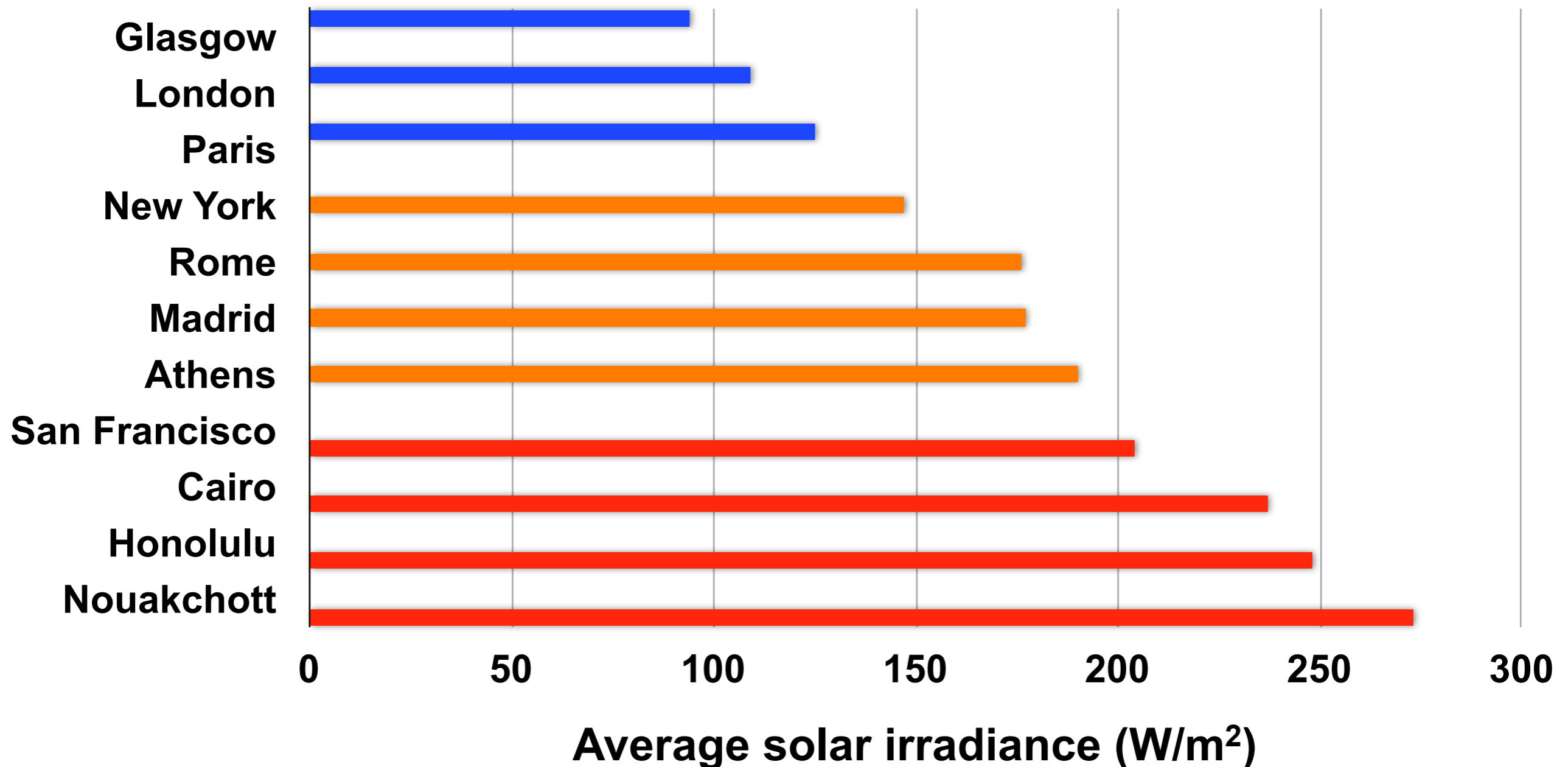
- **Thermal limit i.e. heating for the sun as a 6000 K black body emitter with a 300 K solar cell black body absorber**

Sun: 6000 K

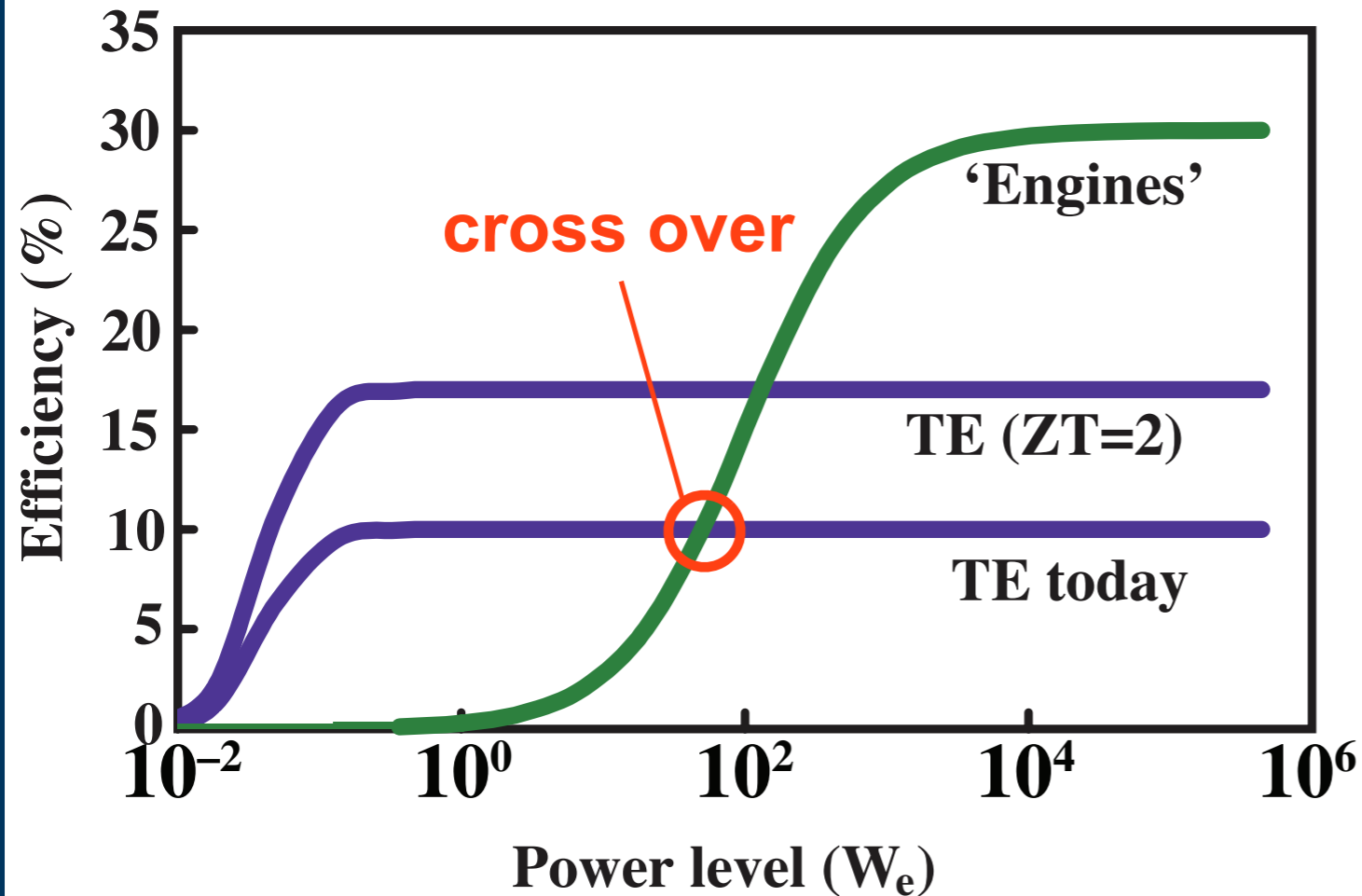


- **Maximum Carnot efficiency is 85% for absorber at 2470 K:
all photons absorbed
maximum heat from every photon
zero thermal dissipation from absorber**
- **Actual efficiencies for a room temperature absorber are $< 85\%$**

- Due to clouds, day/night & seasons, average energy \ll peak energy
- Available energy needs to be averaged over 365 days and 24 hours



Illustrative schematic diagram



At large scale, thermodynamic engines more efficient than TE

ZT average for both n and p over all temperature range

Diagram assumes high ΔT

- At the mm and μm scale with powers $\ll 1\text{W}$, thermoelectrics are more efficient than thermodynamic engines (Reynolds no. etc..)

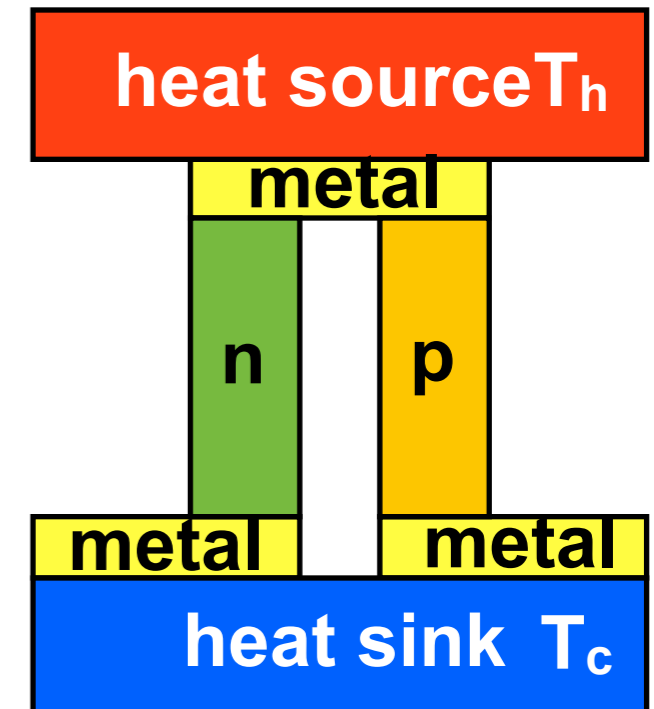
- As the system has thermal conductivity κ a maximum ΔT can be sustained across a module limited by heat transport

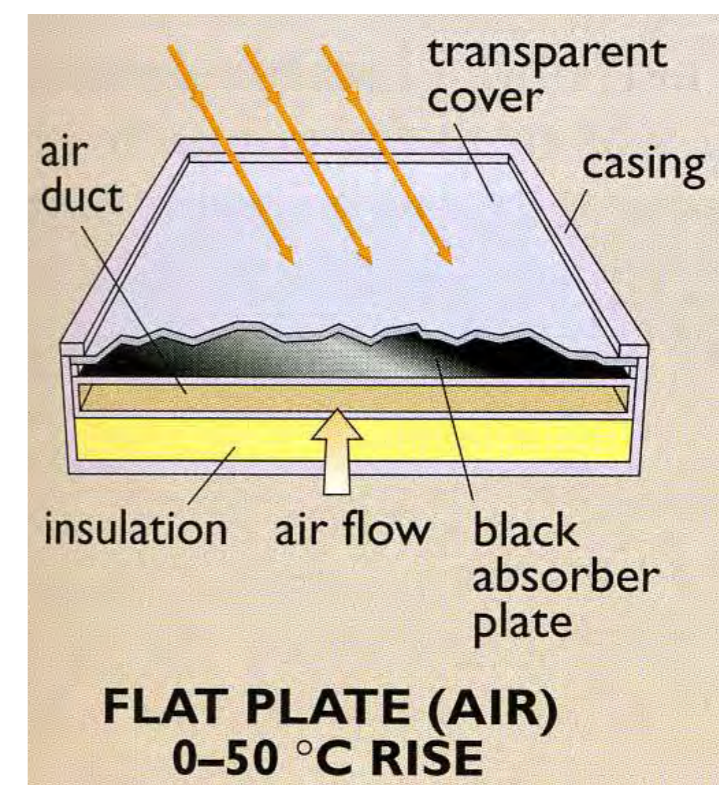
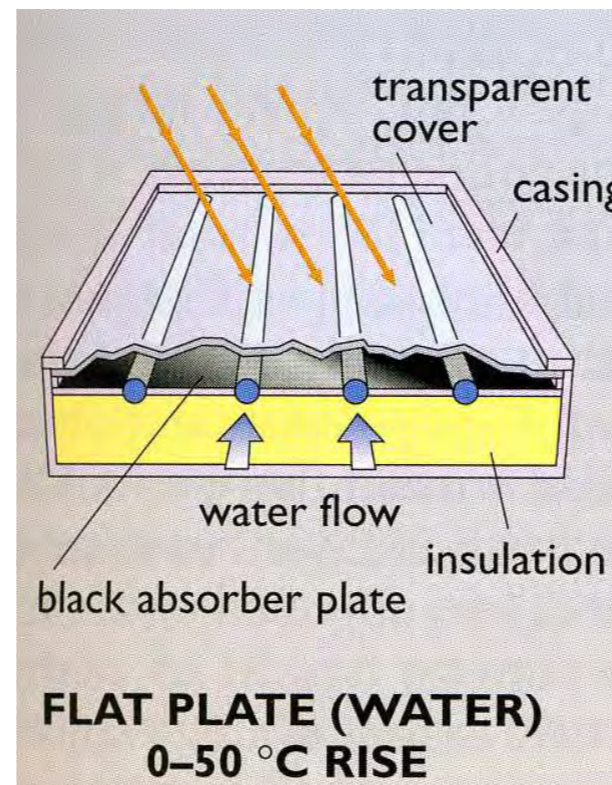
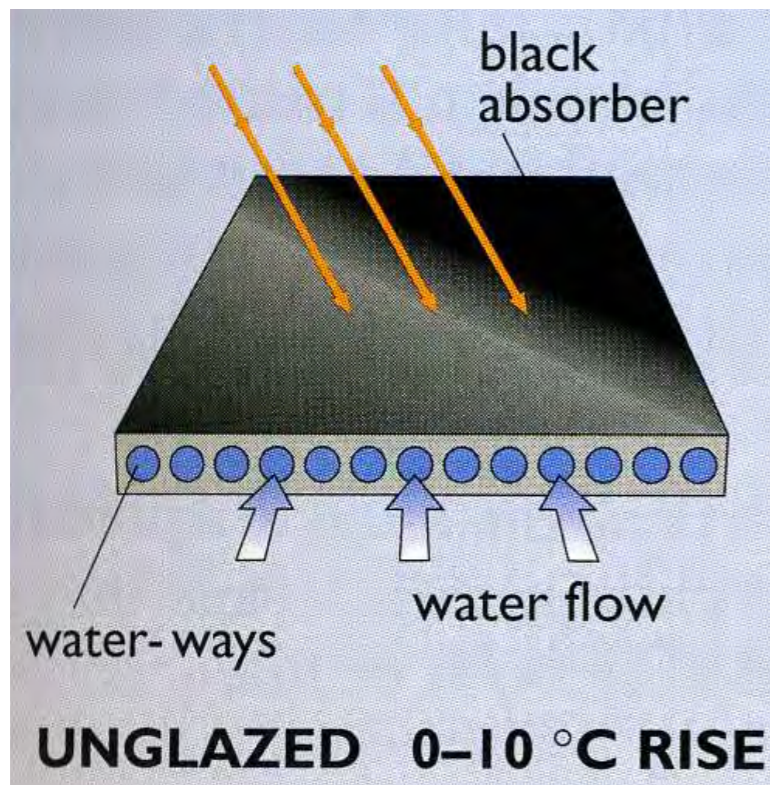
- $$\Delta T_{\max} = \frac{1}{2} Z T_c^2$$

- The efficiency cannot be increased indefinitely by increasing T_h

- The thermal conductivity also limits maximum ΔT in Peltier coolers

- Higher ΔT_{\max} requires better Z materials

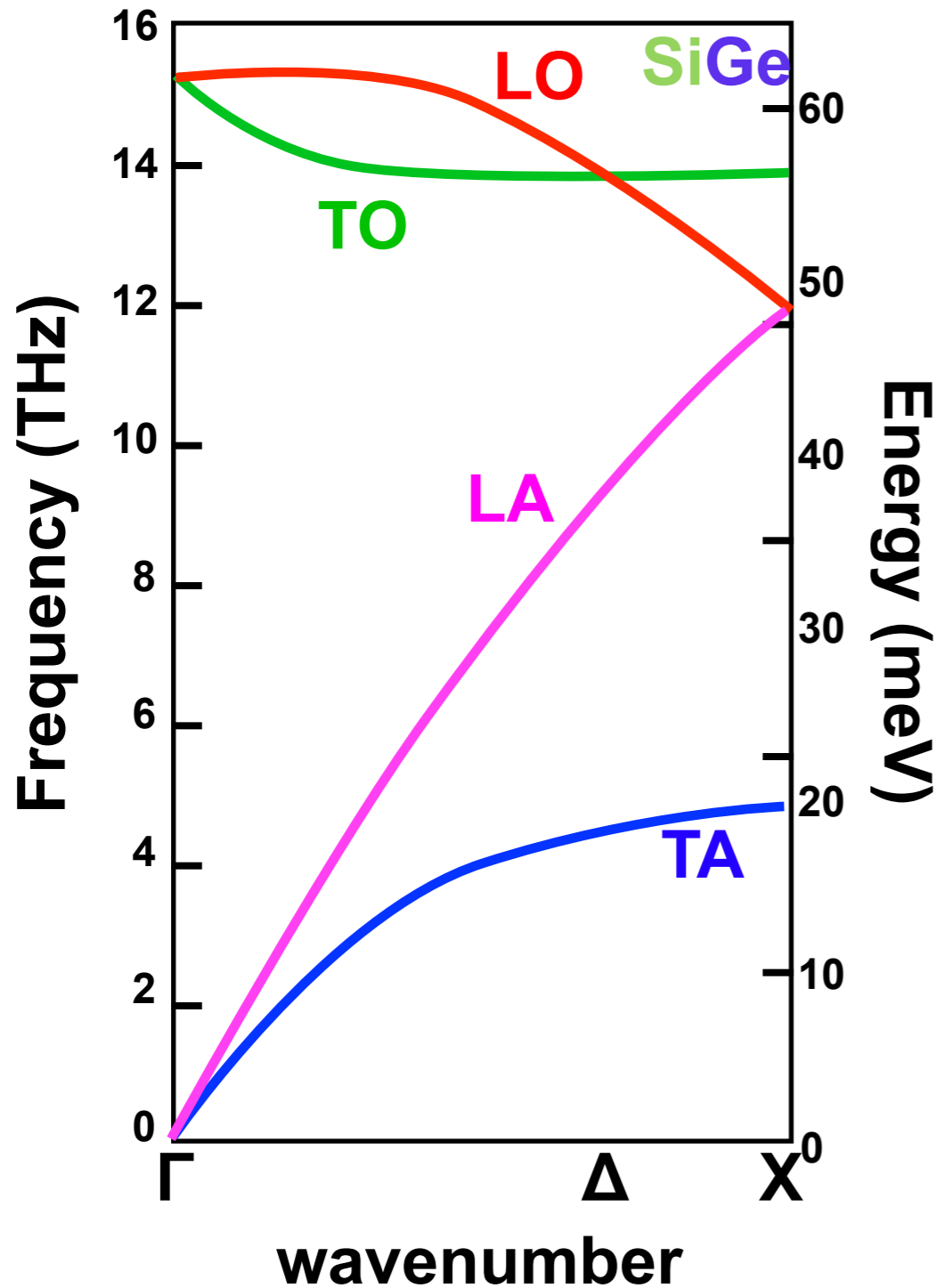




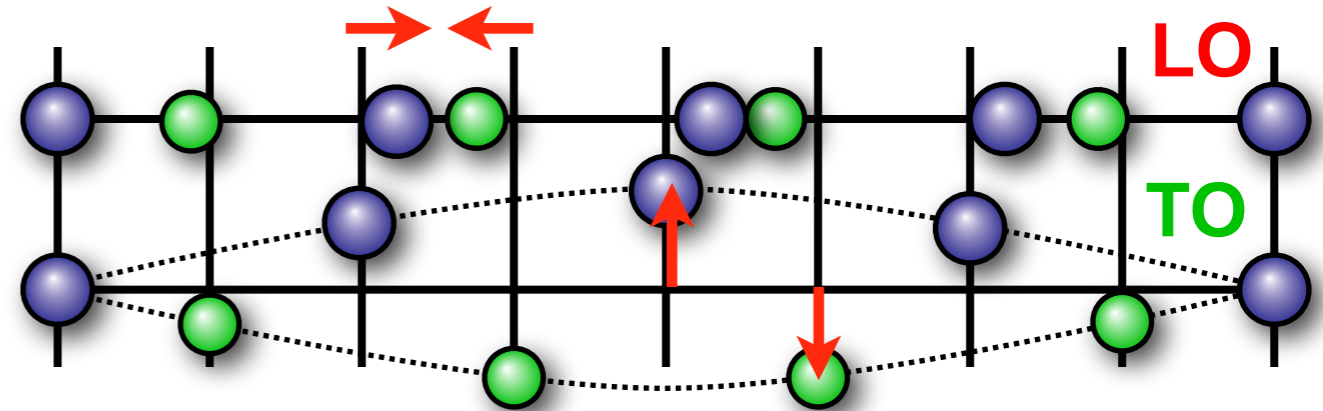
- Efficiency can be high as η is dominated by absorption of photons
- Optimisation is all about maximum photon absorption and minimum heat loss
- 46% to 74% η for solar energy \rightarrow heat conversion are typical
- η heavily dependent on amount of solar energy available and required hot water temperature


- **NASA with finite Pu fuel for RTG requires high efficiency**
- **Automotive requires high power (heat is abundant)**
- **Industrial sensing requires high power (heat is abundant)**
- **Autonomous sensing requires high power (heat is abundant)**
- **As heat is abundant the issue is how to maximise power output NOT efficiency for most applications**

$$\text{Power} \propto \alpha^2 \sigma$$

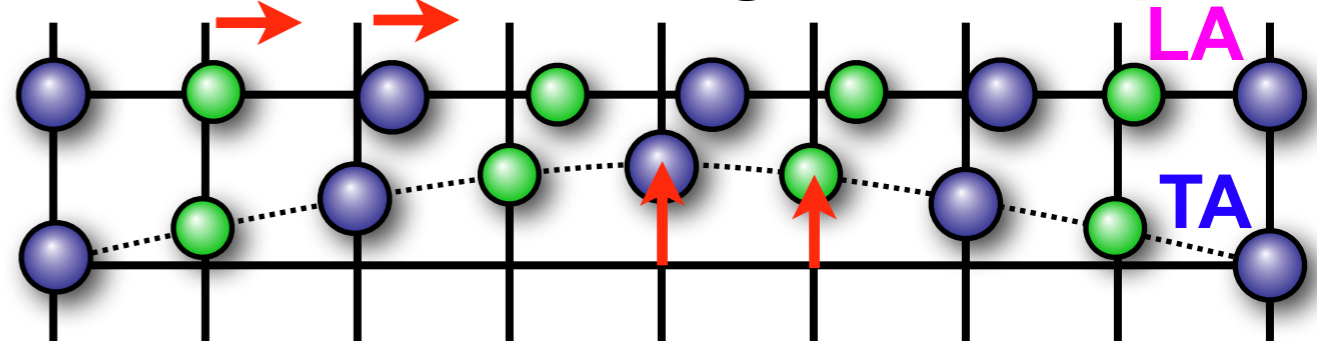


optic modes - neighbours in **antiphase**



 NB acoustic phonons transmit most thermal energy

acoustic modes - neighbours in **phase**



 The majority of heat in solids is transported by acoustic phonons

Lattice contribution:

$$\bullet \quad \kappa_{\text{ph}} = \frac{k_{\text{B}}}{2\pi^2} \left(\frac{k_{\text{B}}}{\hbar} \right)^3 T^3 \int_0^{\frac{\theta_{\text{D}}}{T}} \frac{\tau_{\text{c}}(\mathbf{x}) x^4 e^x}{v(\mathbf{x})(e^x - 1)^2} d\mathbf{x}$$

θ_{D} = Debye temperature (640 K for Si)

$$x = \frac{\hbar\omega}{k_{\text{B}}T}$$

τ_{c} = combined phonon scattering time

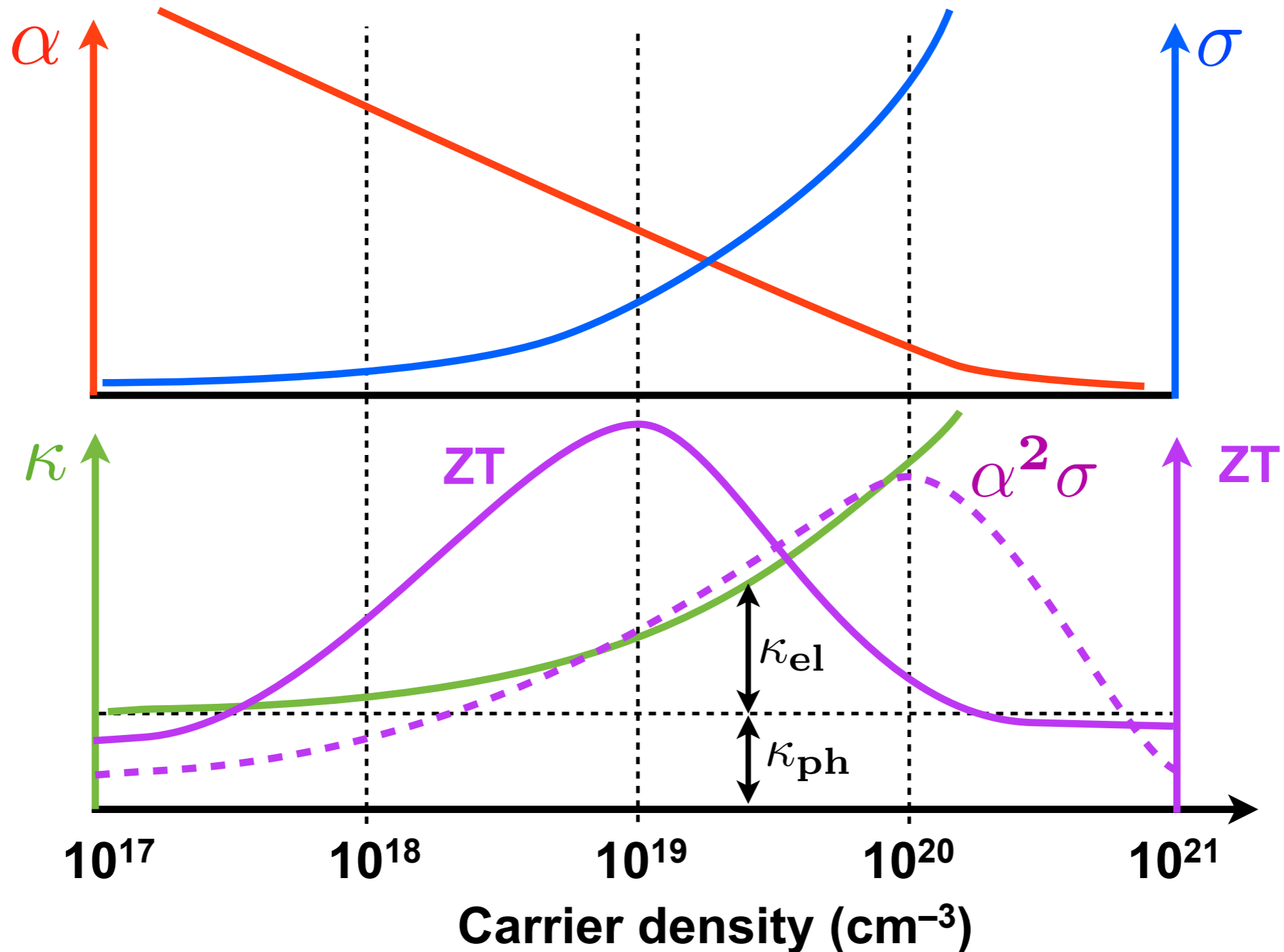
$v(\mathbf{x})$ = velocity

J. Callaway, Phys. Rev. 113, 1046 (1959)

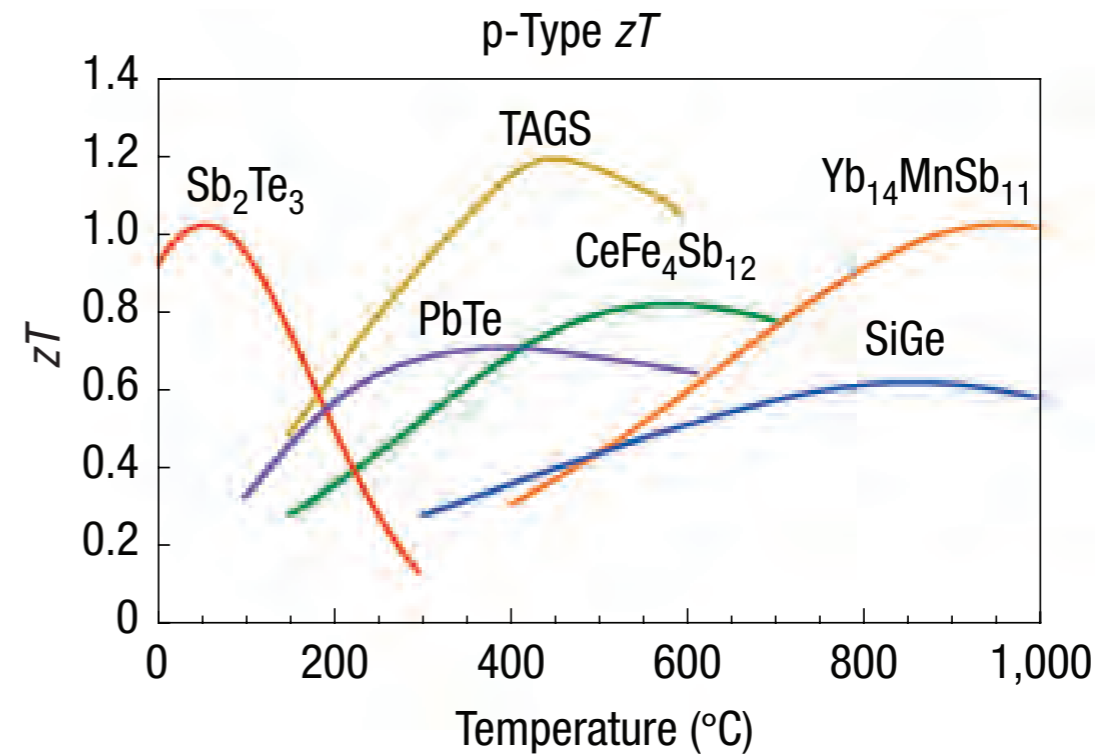
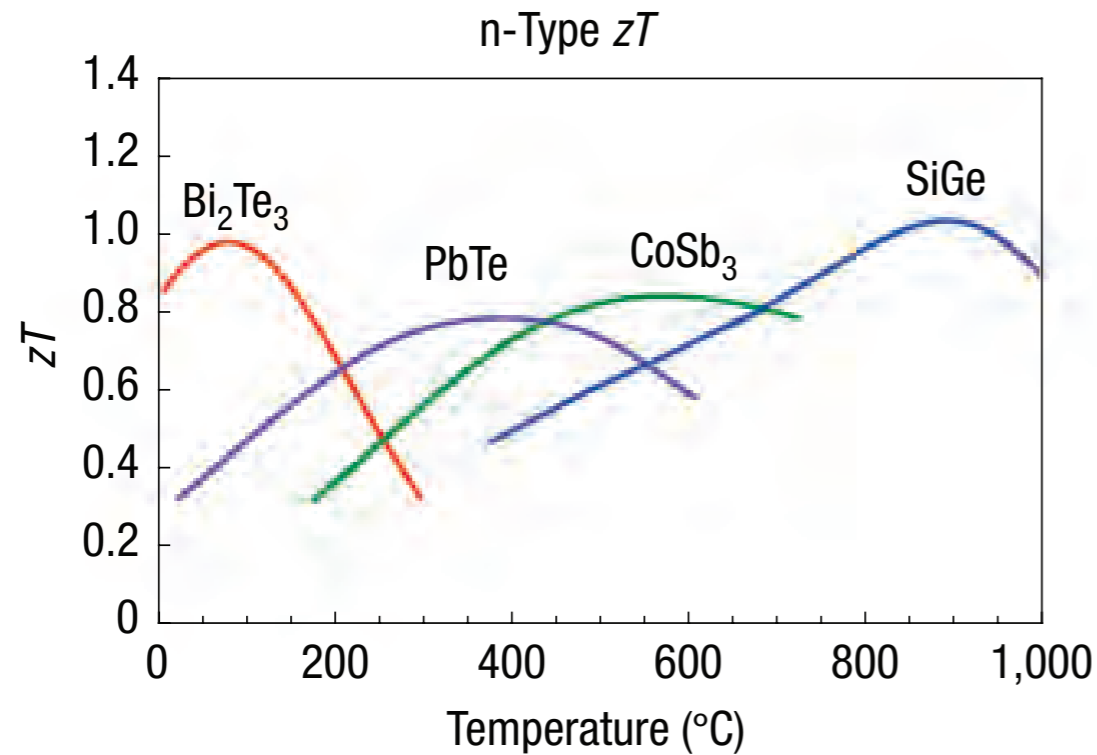
Electron (hole) contribution:

$$\bullet \quad \kappa_{\text{el}} = \frac{\sigma}{q^2 T} \left[\frac{\langle \tau \rangle \langle \mathbf{E}^2 \tau \rangle - \langle \mathbf{E} \tau \rangle^2}{\langle \tau^3 \rangle} \right]$$

$\tau(\mathbf{E})$ = total electron momentum relaxation time



- Electrical and thermal conductivities are not independent
- Wiedemann Franz rule: electrical conductivity \propto thermal conductivity at high doping



Nature Materials 7, 105 (2008)

- **Bulk n- Bi_2Te_3 and p- Sb_2Te_3 used in most commercial thermoelectrics & Peltier coolers**
- **But tellurium is 9th rarest element on earth !!!**
- **Bulk $Si_{1-x}Ge_x$ ($x \sim 0.2$ to 0.3) used for high temperature satellite applications**

Reducing thermal conductivity faster than electrical conductivity:

- e.g. skutterudite structure: filling voids with heavy atoms

Low-dimensional structures:

- Increase α by enhanced DOS $\left(\alpha = -\frac{\pi^2}{3q} k_B^2 T \left[\frac{d \ln(\mu(E)g(E))}{dE} \right]_{E=E_F} \right)$
- Make κ and σ almost independent
- Reduce κ through phonon scattering on heterointerfaces

Energy filtering:

- $$\alpha = -\frac{k_B}{q} \left[\frac{E_c - E_F}{k_B T} + \frac{\int_0^\infty \frac{(E - E_c)}{k_B T} \sigma(E) dE}{\int_0^\infty \sigma(E) dE} \right]$$

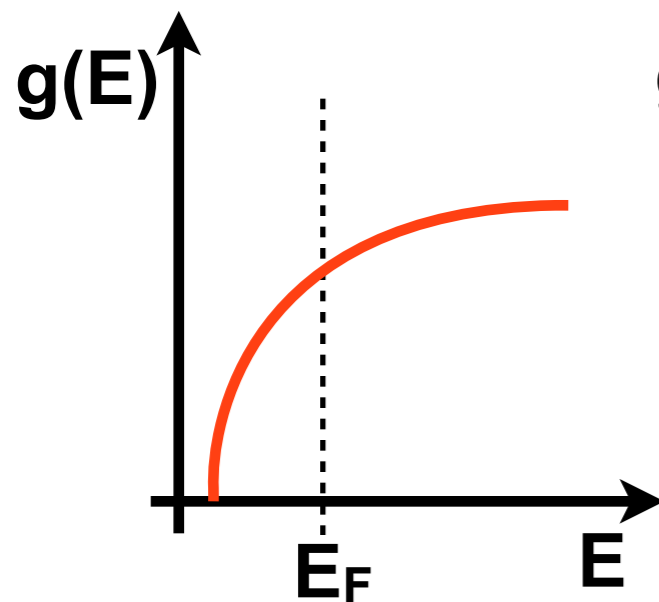
Y.I. Ravich et al., Phys. Stat. Sol. (b) 43, 453 (1971)

enhance

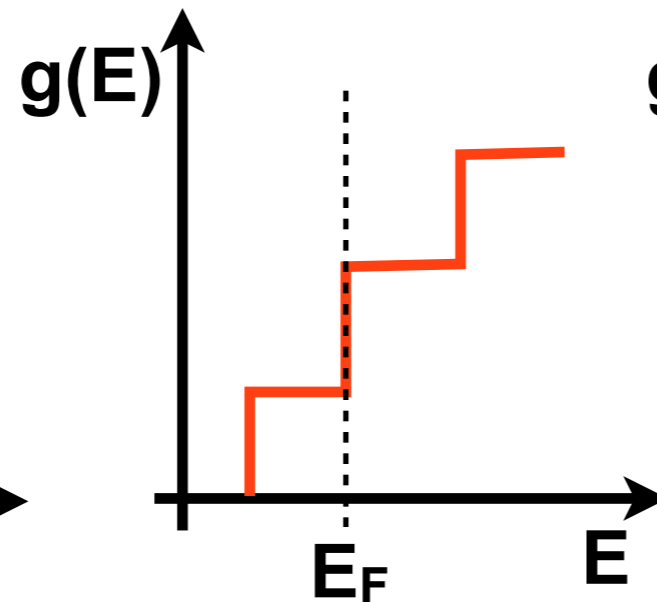
- Increase α through enhanced DOS:

$$\alpha = -\frac{\pi^2}{3q} k_B^2 T \left[\frac{d \ln(\mu(E)g(E))}{dE} \right]_{E=E_F}$$

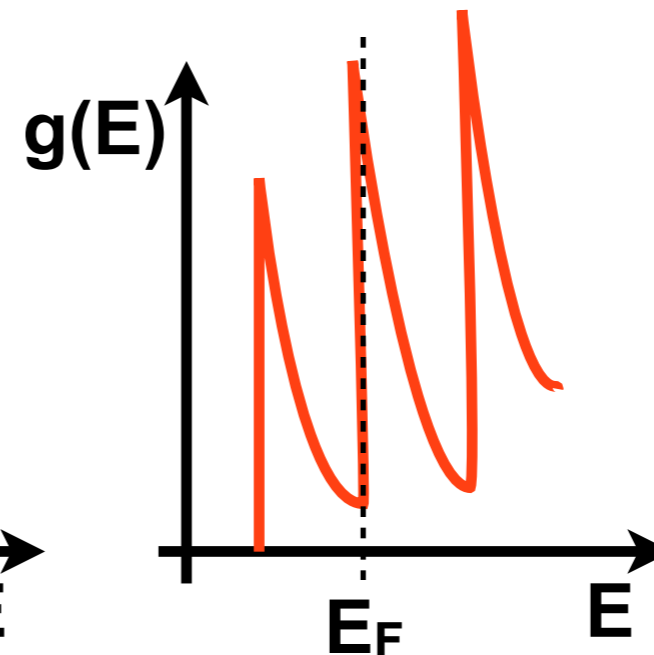
3D
bulk



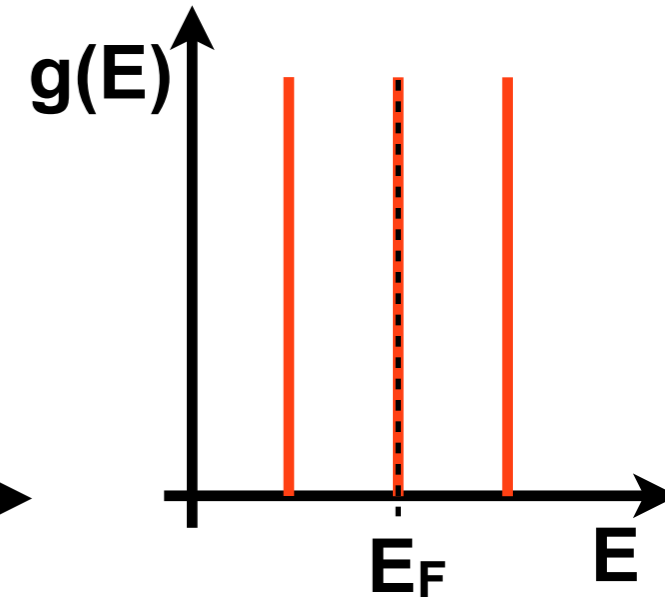
2D
quantum well



1D
quantum wire



0D
quantum dot



————— α increasing —————>

3D electron mean free path $\ell = v_F \tau_m = \frac{\hbar}{m^*} (3\pi^2 n)^{\frac{1}{3}} \frac{\mu m^*}{q}$

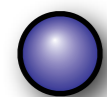
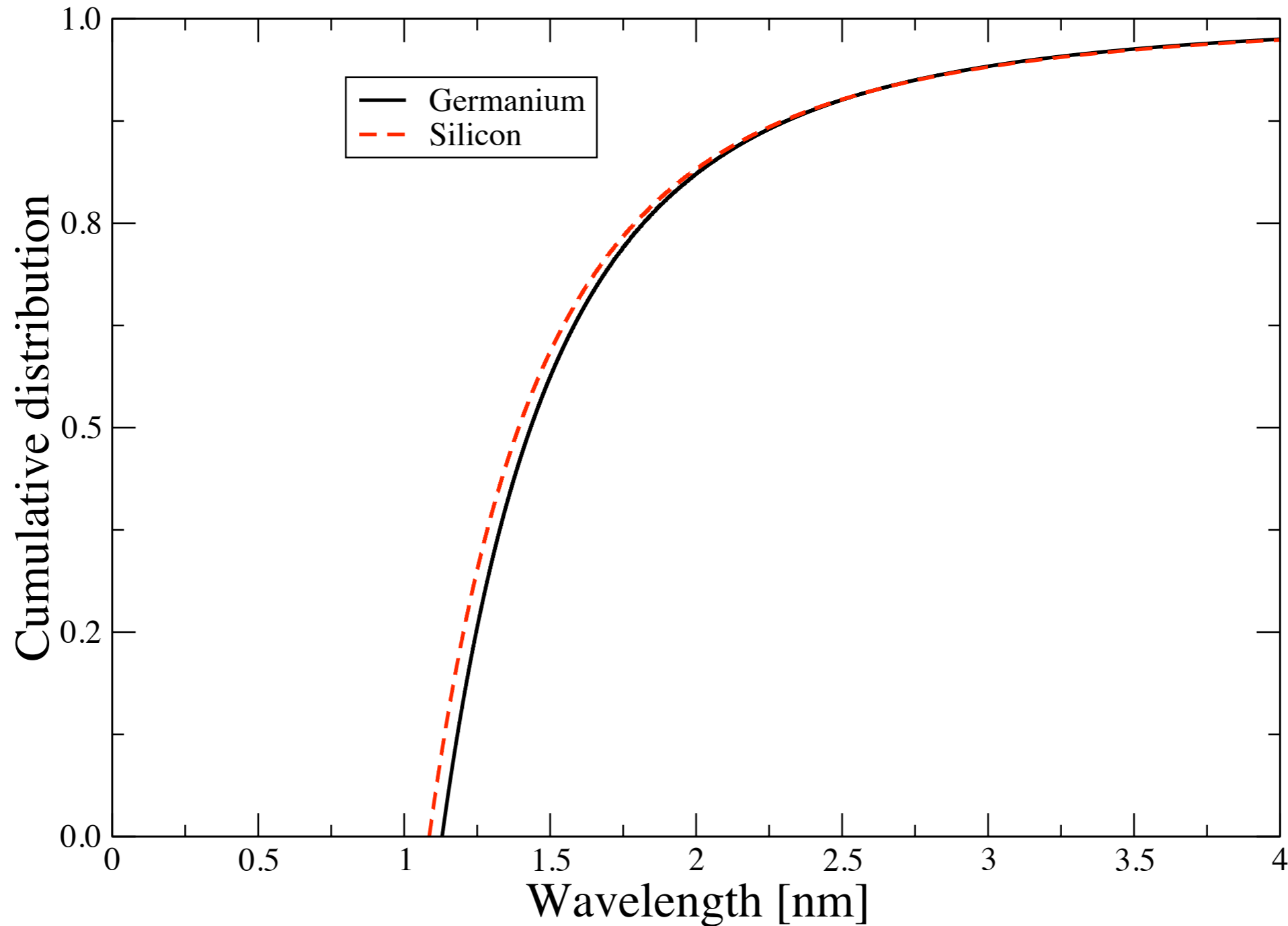
$$\ell = \frac{\hbar \mu}{q} (3\pi^2 n)^{\frac{1}{3}}$$

3D phonon mean free path

$$\Lambda_{\text{ph}} = \frac{3\kappa_{\text{ph}}}{C_v \langle v_t \rangle \rho}$$

- C_v = specific heat capacity
- $\langle v_t \rangle$ = average phonon velocity
- ρ = density of phonons
- A structure may be 2D or 3D for electrons but 1 D for phonons (or vice versa!)

| Material | Model | Specific Heat ($\times 10^6 \text{ Jm}^{-3}\text{K}^{-1}$) | Group velocity (ms^{-1}) | Phonon mean free path, Λ_{ph} (nm) |
|-----------------|-------------------|--|---|---|
| Si | Debye | 1.66 | 6400 | 40.9 |
| Si | Dispersion | 0.93 | 1804 | 260.4 |
| Ge | Debye | 1.67 | 3900 | 27.5 |
| Ge | Dispersion | 0.87 | 1042 | 198.6 |



Greater than 95% of heat conduction in Si / Ge from phonons with wavelengths between 1.2 and 3.5 nm

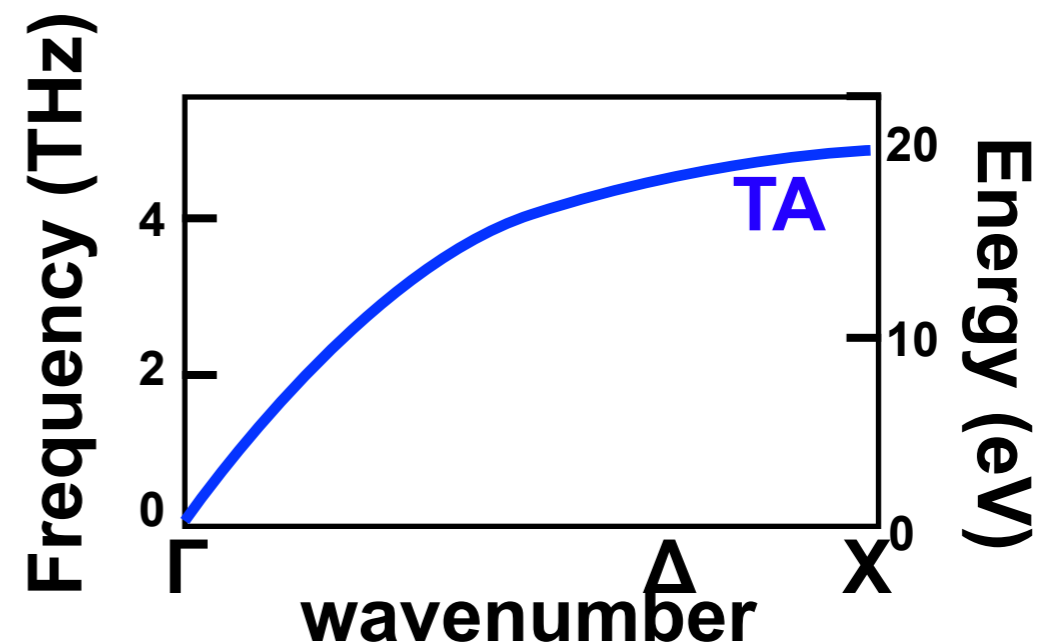
Phonon scattering:

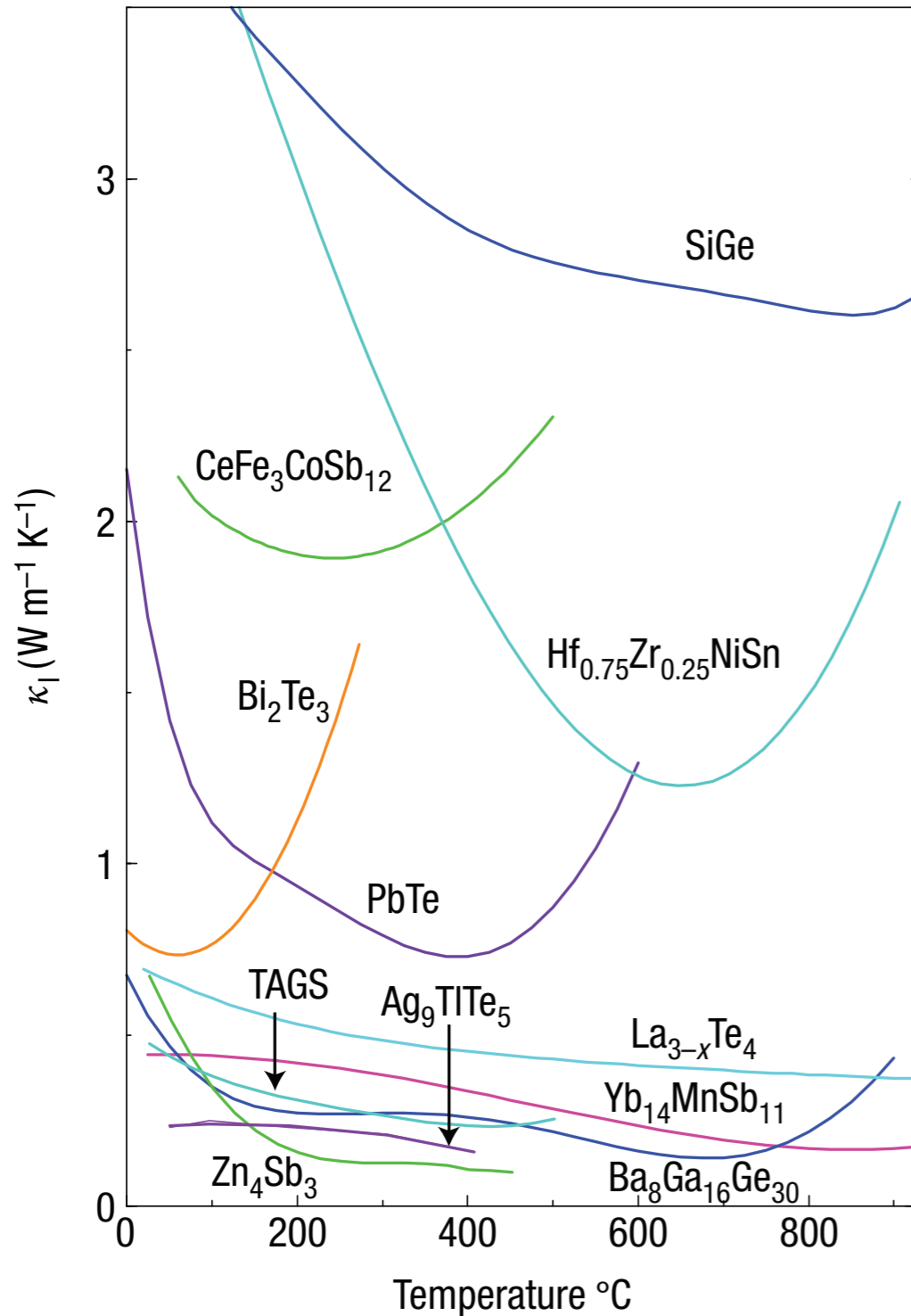
- Require structures below the phonon mean free path (10s nm)

Phonon Bandgaps:

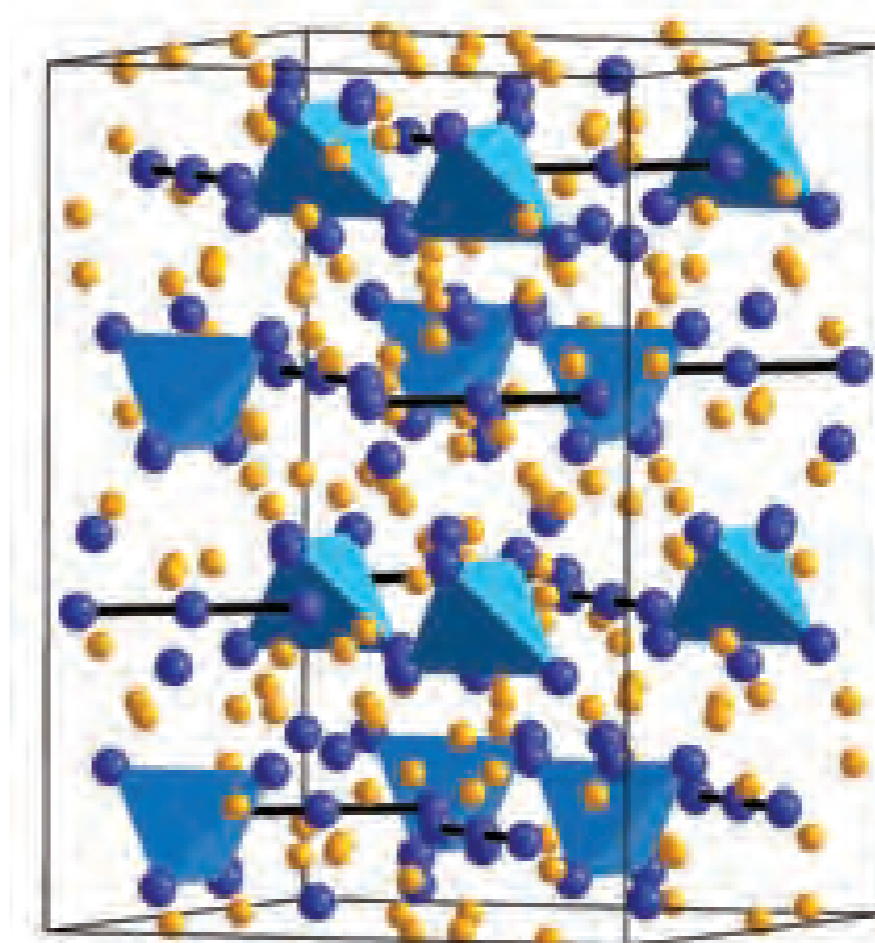
- Change the acoustic phonon dispersion → stationary phonons or bandgaps
- Require structures with features at the phonon wavelength (< 5 nm)

- Phonon group velocity $\propto \frac{dE}{dk_q}$



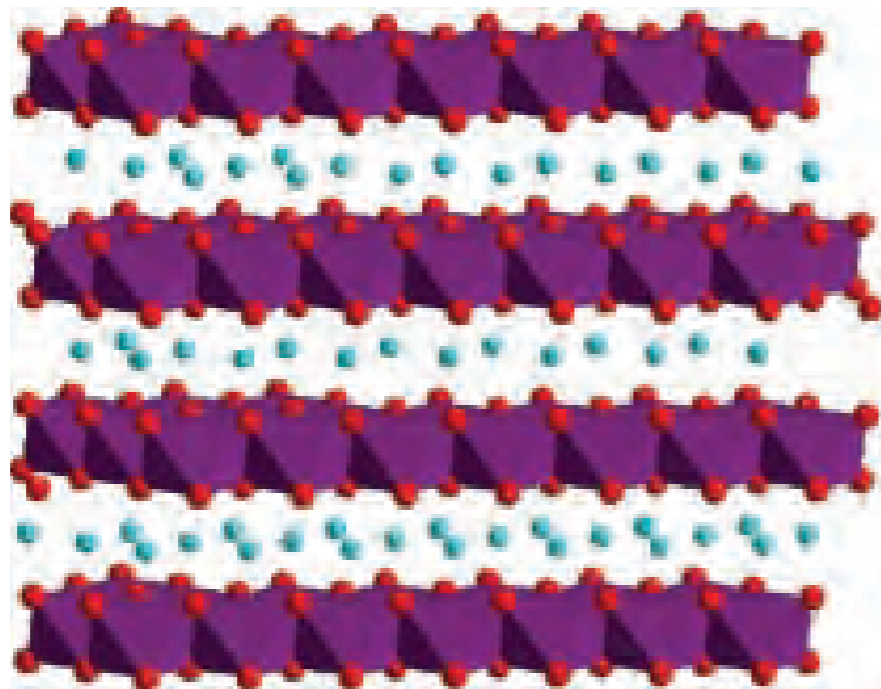


Skutterudite structure: filling voids with heavy atoms

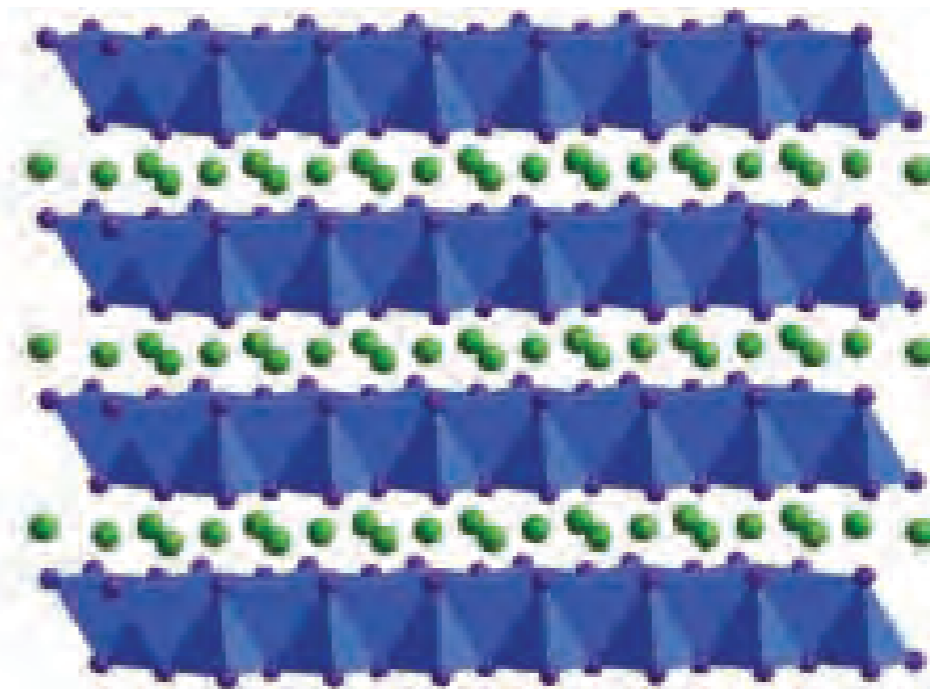


p-Yb₁₄MnSb₁₁ – ZT ~ 1 @ 900 °C

- Principle: trying to copy “High T_c ” superconductor structures
- Heavy ion / atom layers for phonon scattering
- High mobility electron layers for high electrical conductivity

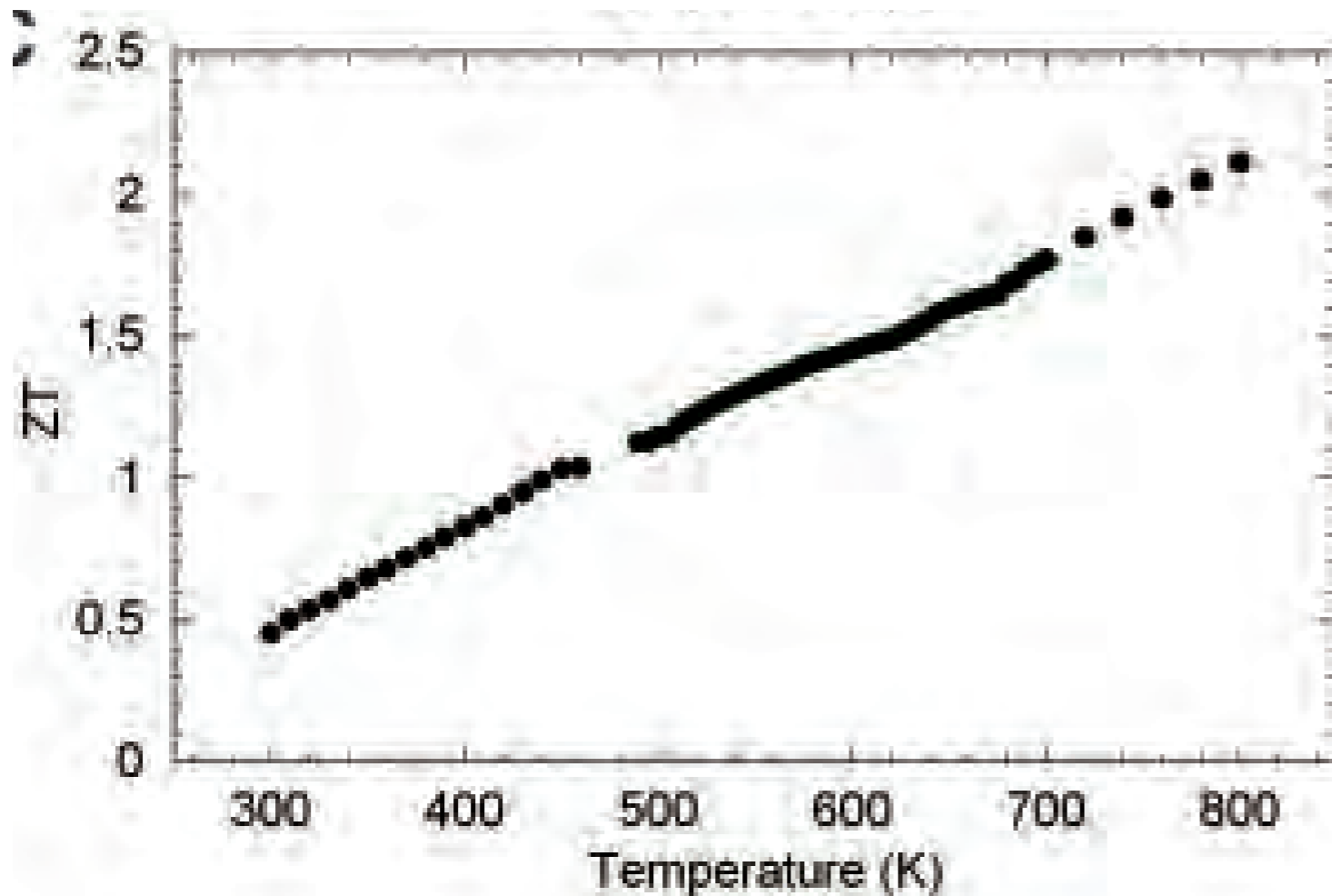
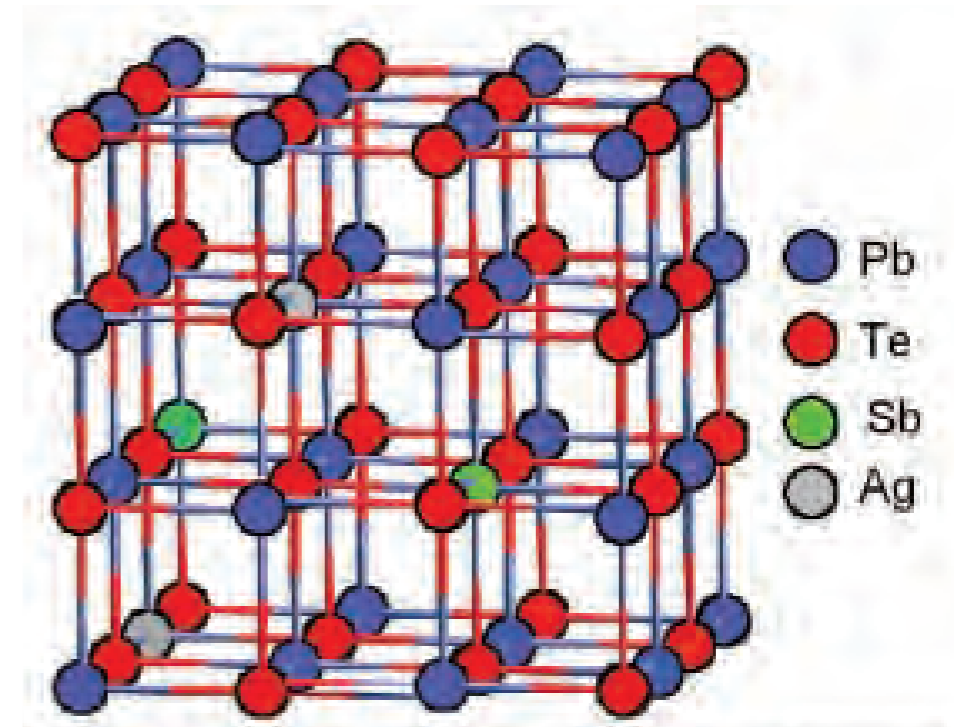
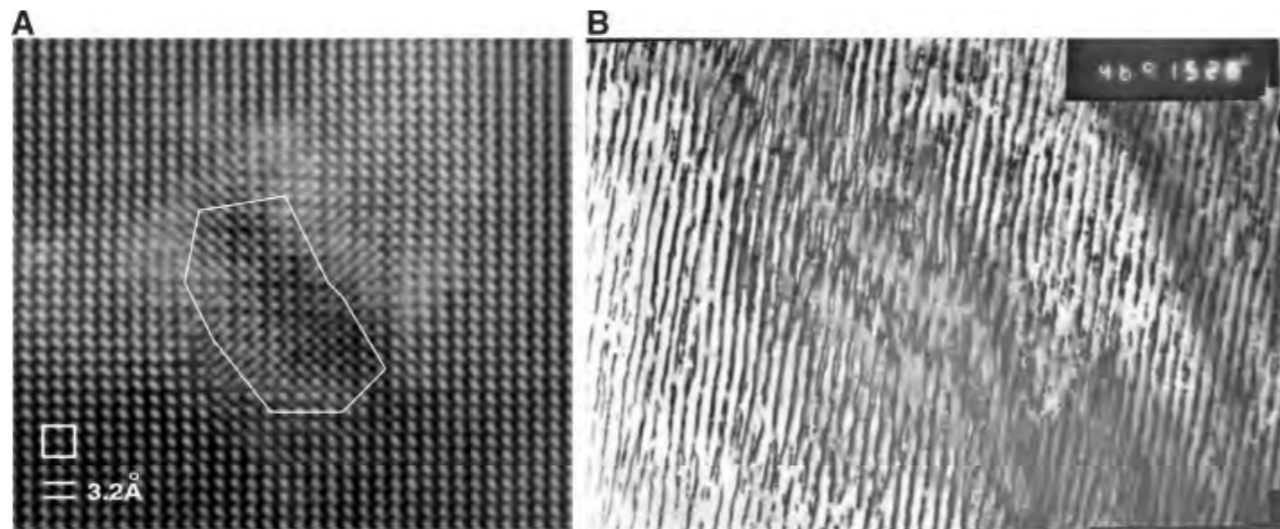


Na_xCoO_2



$\text{Ca}_x\text{Yb}_{1-x}\text{Zn}_2\text{Sb}_2$

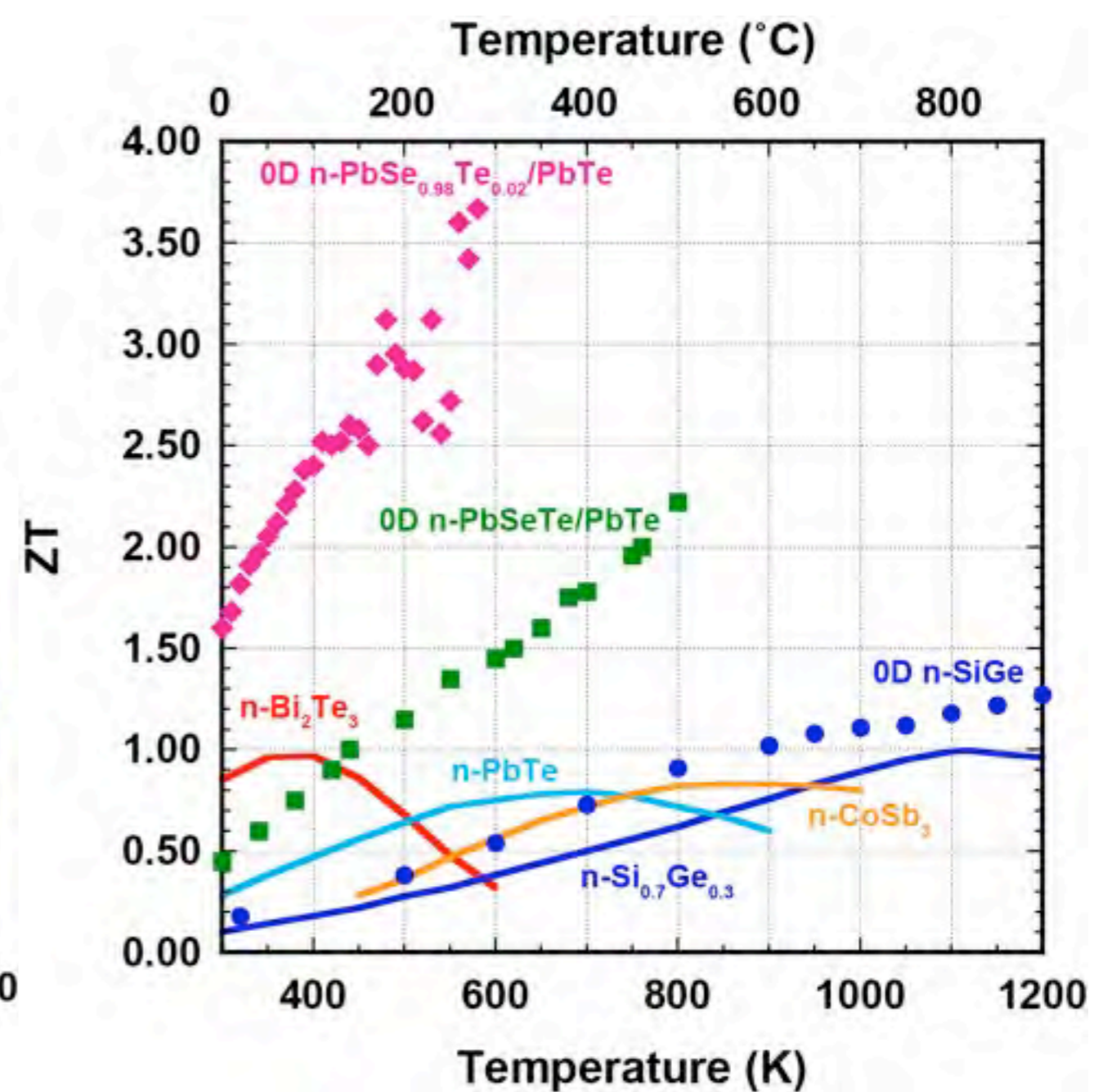
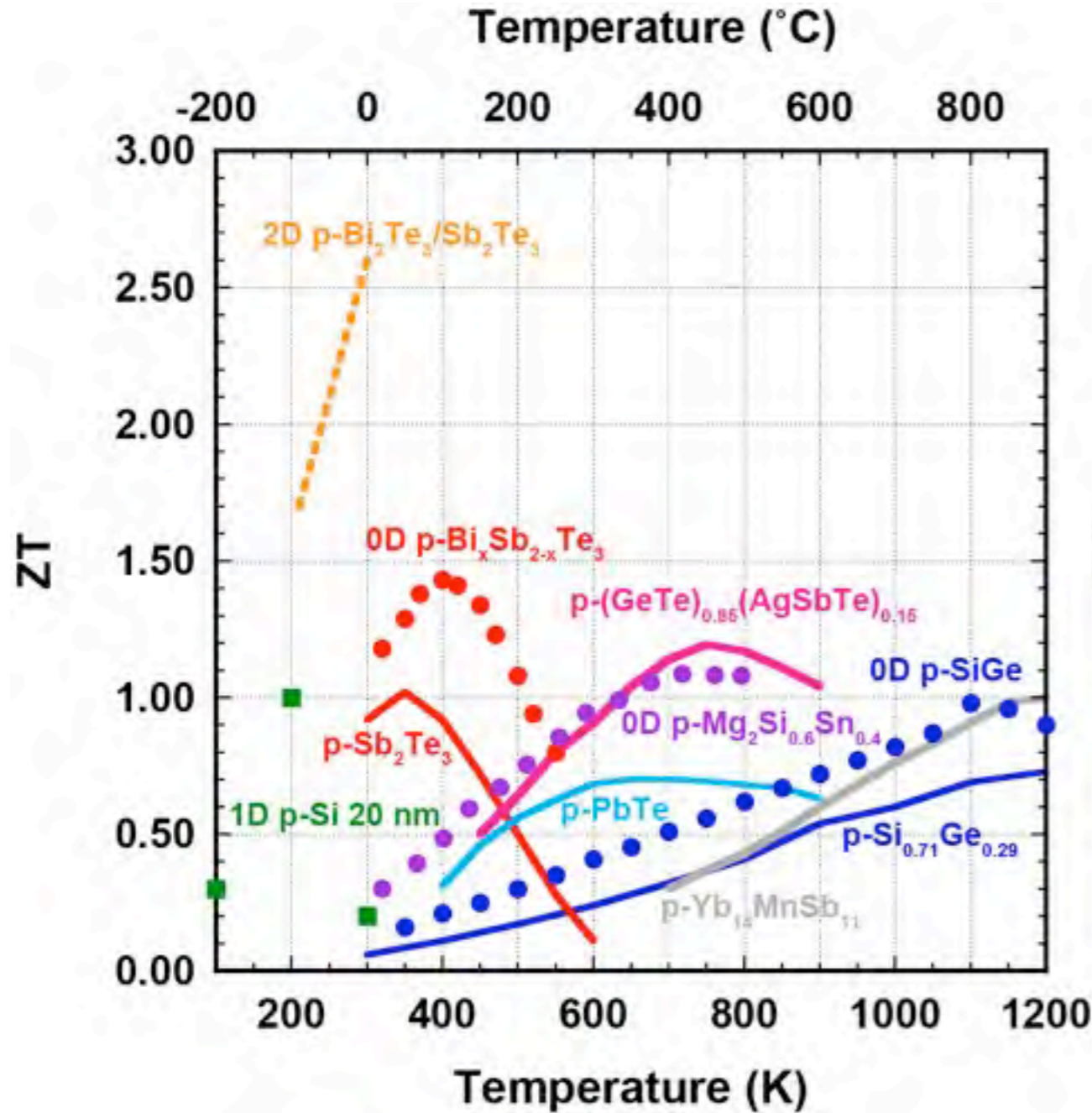
- Only small improvements to ZT observed



$\alpha = -335 \mu\text{VK}^{-1}$
 $\sigma = 30,000 \text{ S/m}$
 $\kappa = 1.1 \text{ Wm}^{-1}\text{K}^{-1}$
 at 700 K

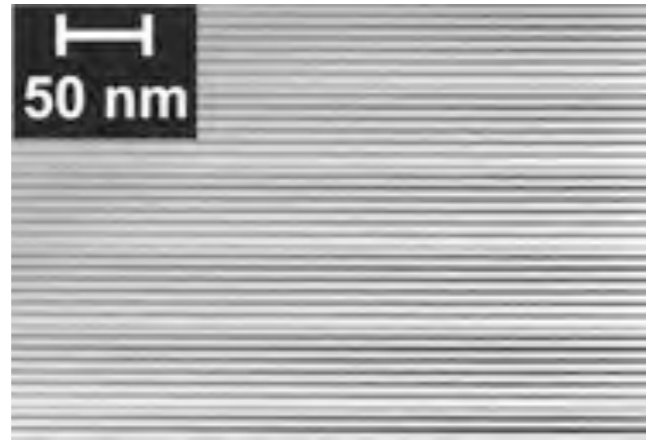
p-type

n-type

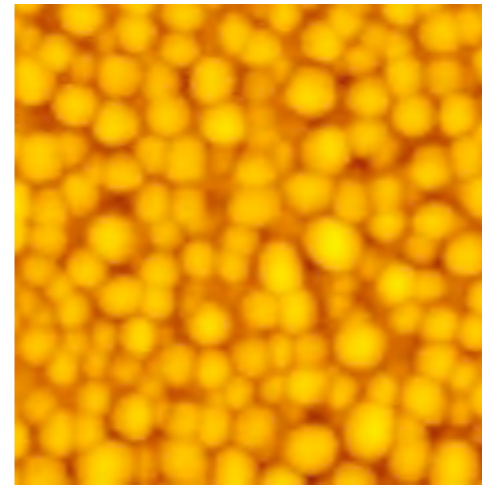


Nanostructures can improve Seebeck coefficient and/or decrease thermal conductivity

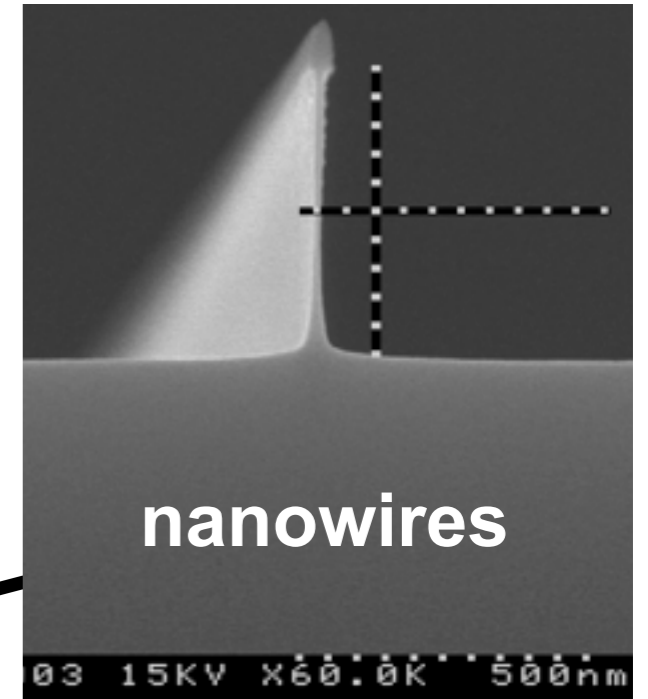
Low dimension technology



superlattices

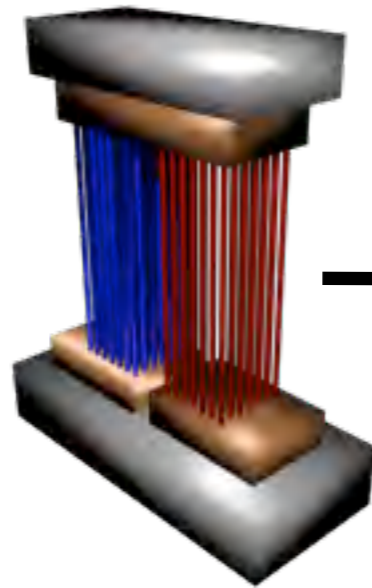


quantum dots

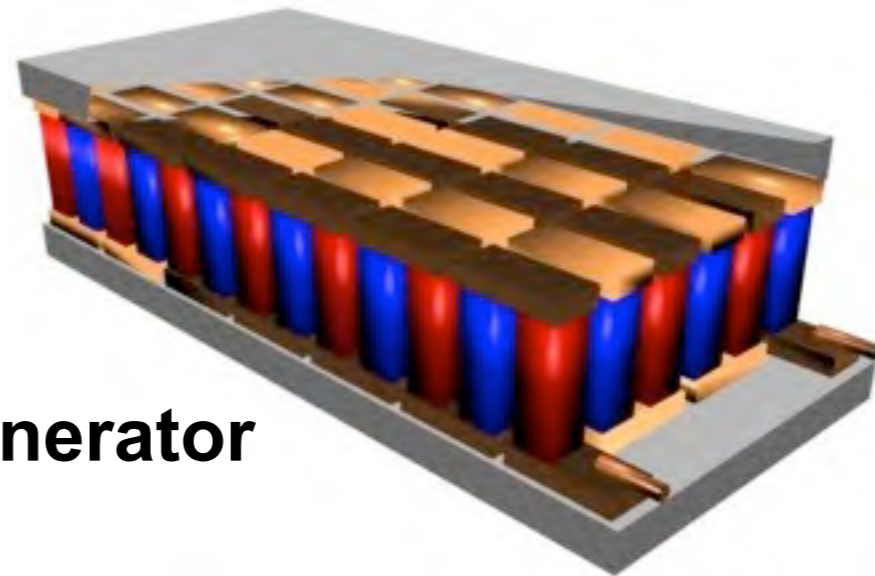


nanowires

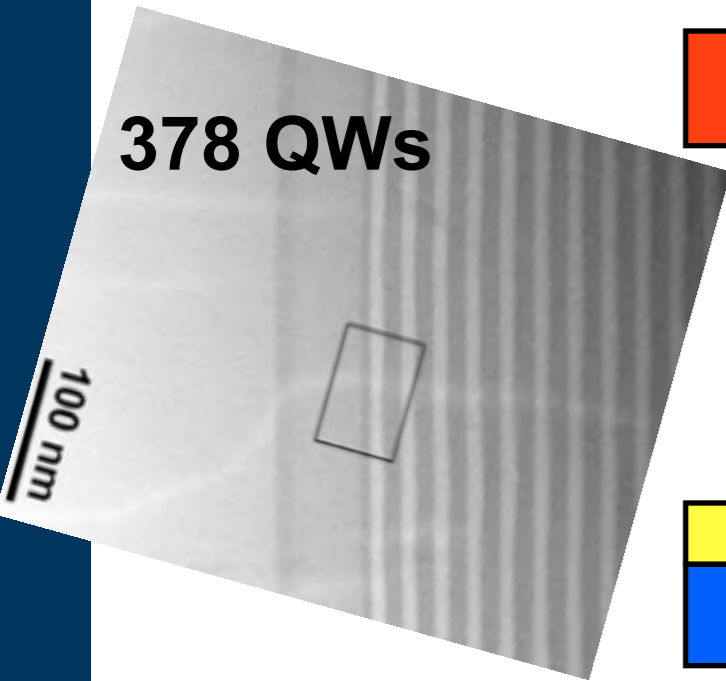
Module



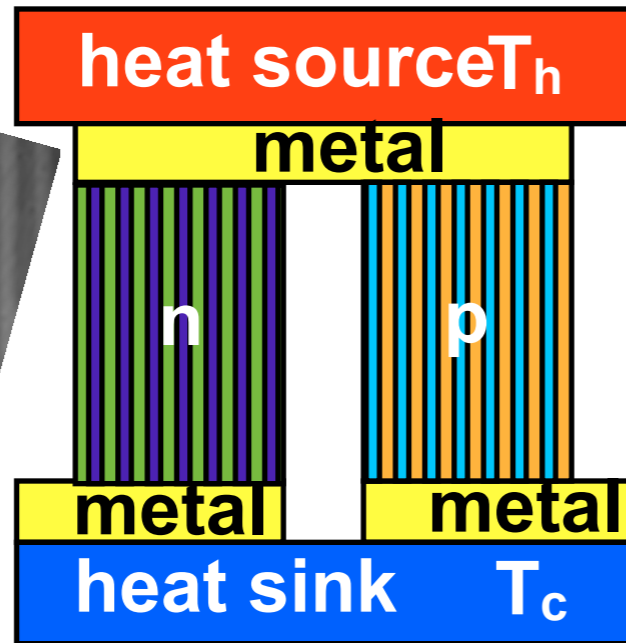
Generator



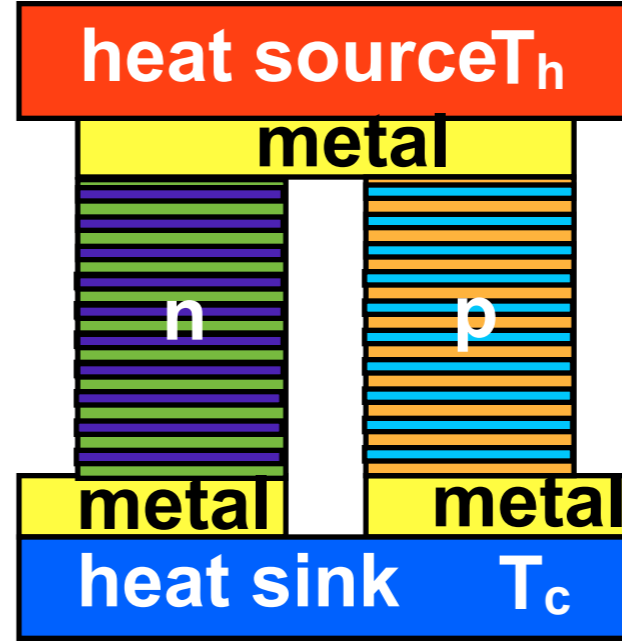
● **Si/SiGe technology → cheap and back end of line compatible**



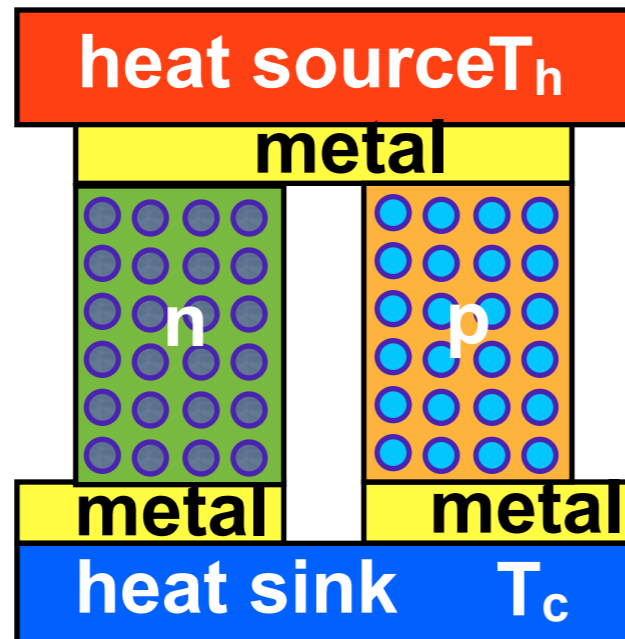
Lateral superlattice



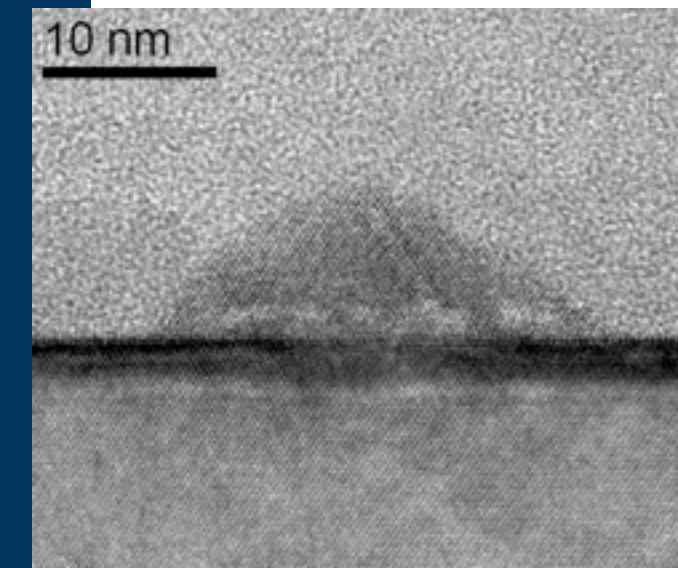
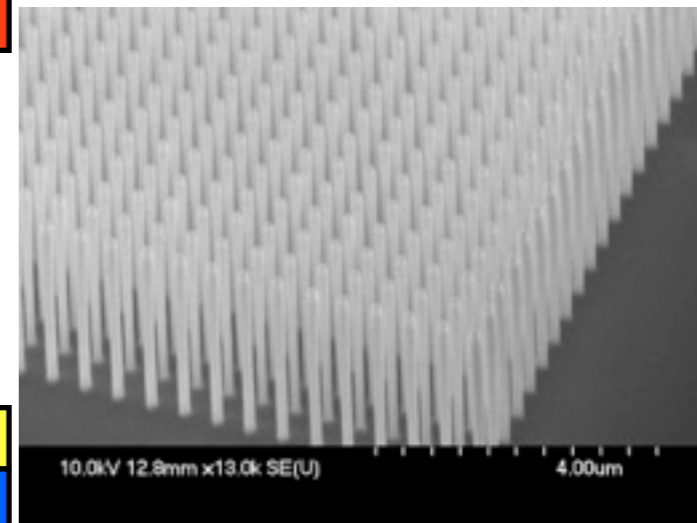
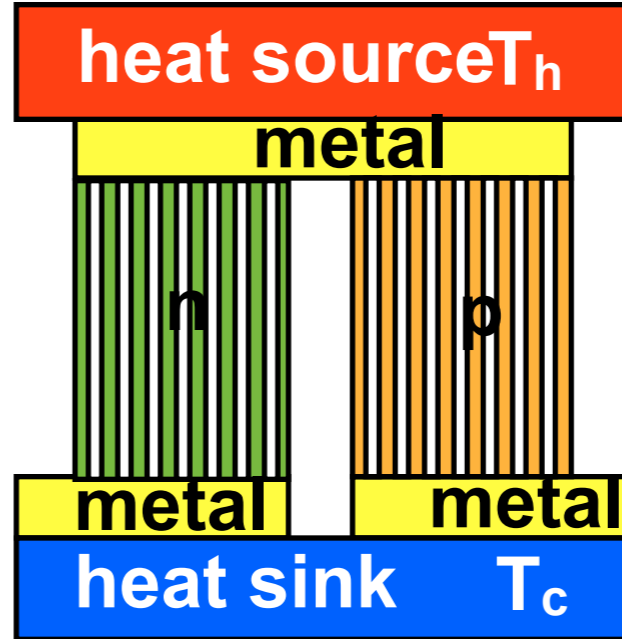
Vertical superlattice



Quantum Dots



Nanowires



- Use of transport perpendicular to superlattice quantum wells
- Higher α from the higher density of states
- Lower electron conductivity from tunnelling
- Lower κ_{ph} from phonon scattering at heterointerfaces
- Able to engineer lower κ_{ph} with phononic bandgaps
- Overall Z and ZT should increase

Vertical superlattice

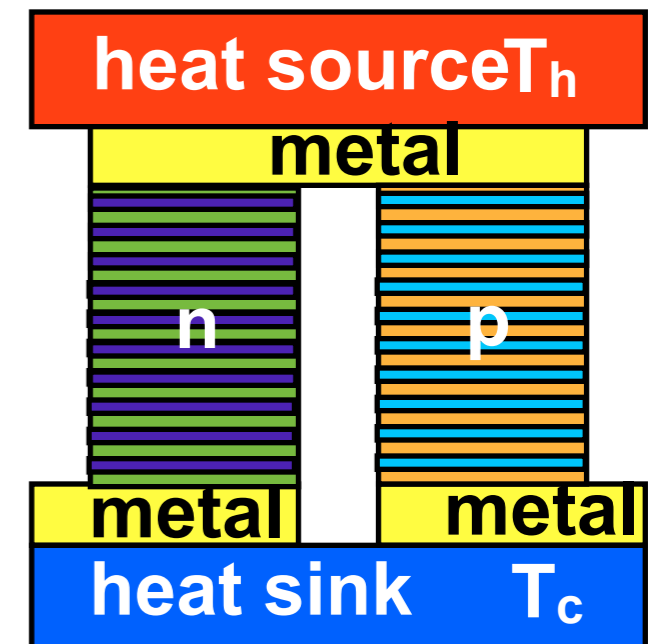


Figure of merit

$$ZT = \frac{\alpha^2 \sigma}{\kappa} T$$

SL1 to SL4: 922 x

2.85 ± 1.5 nm p-Ge QW

1.1 ± 0.6 nm p-Si_{0.5}Ge_{0.5}

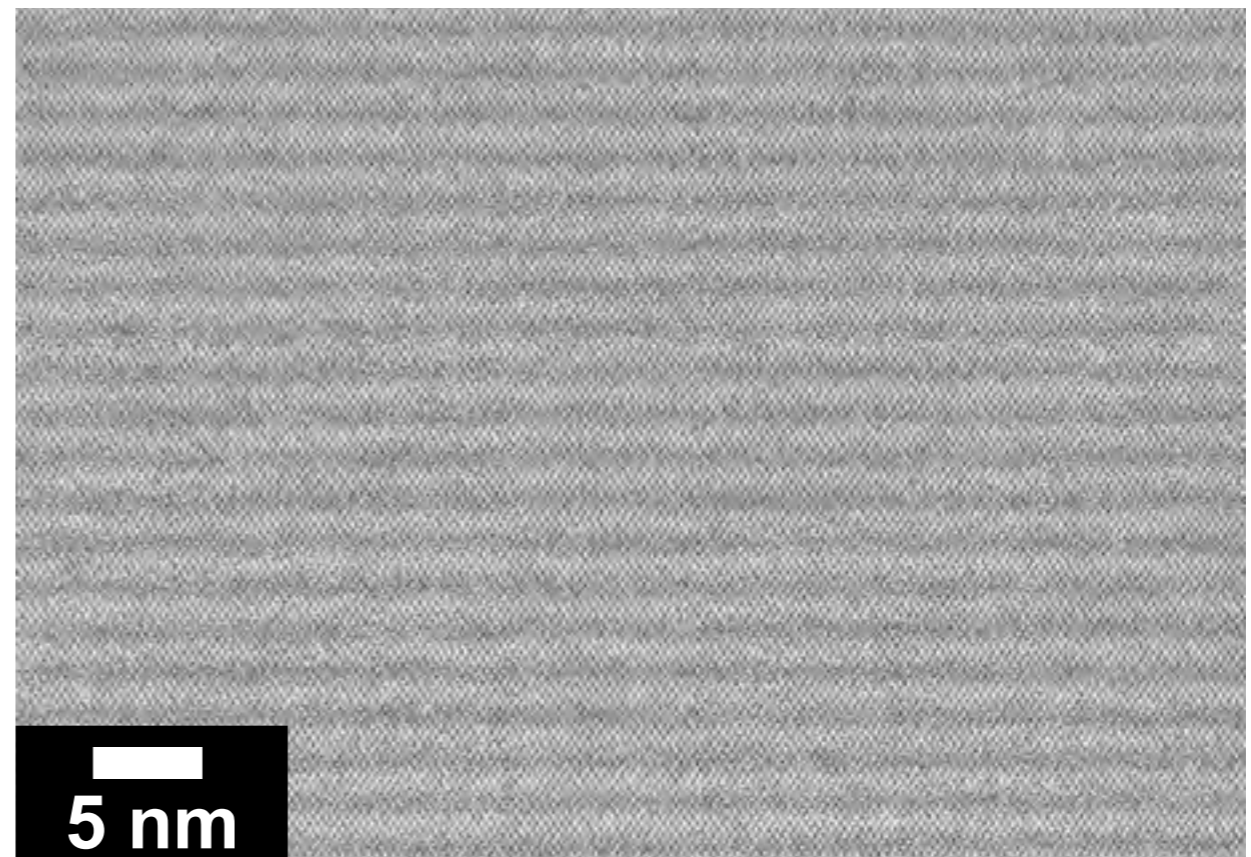
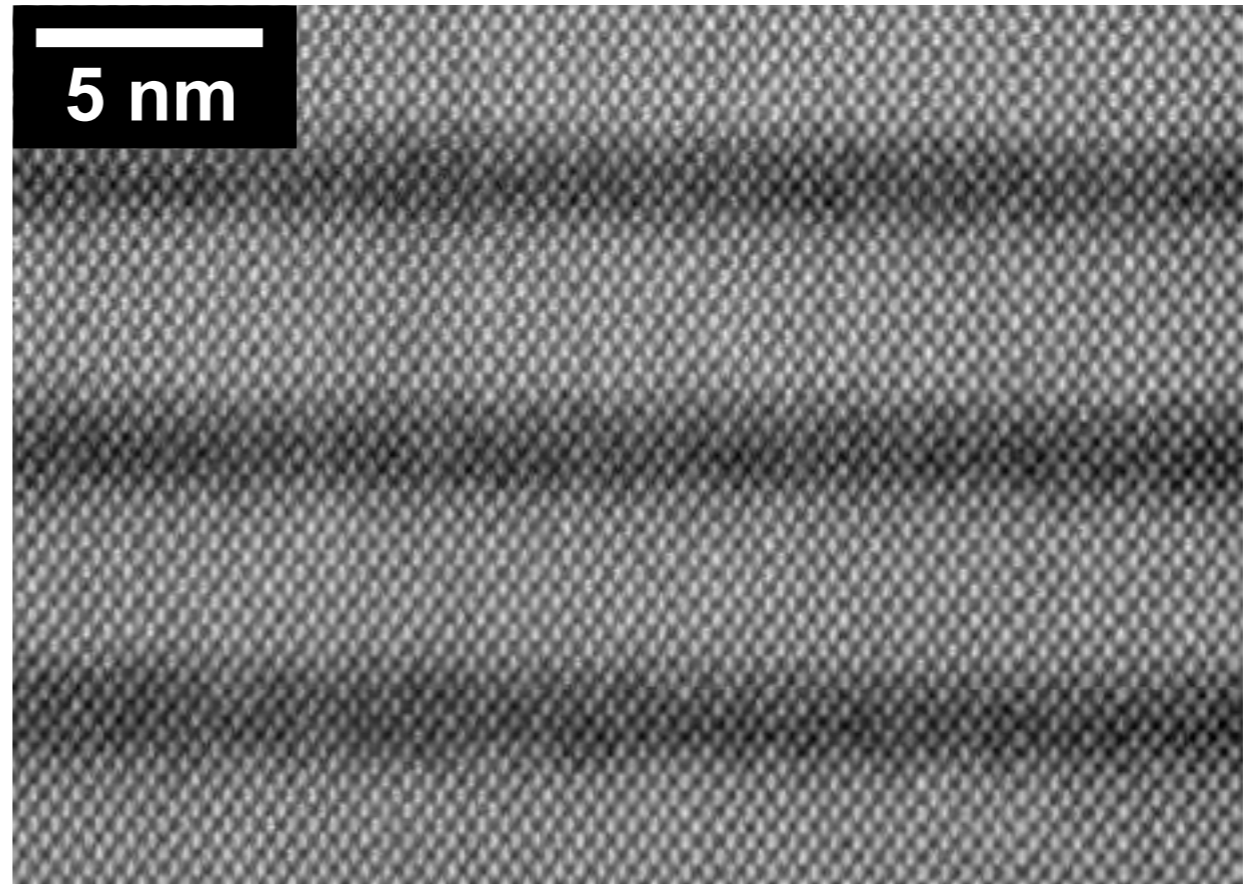
Si_{0.175}Ge_{0.825}

SL5: 2338 x

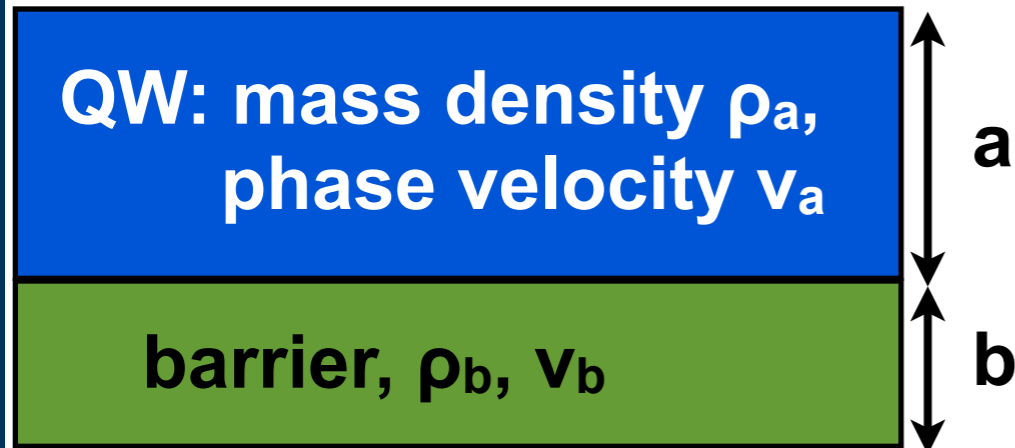
1.1 ± 0.2 nm p-Ge QW

0.5 ± 0.1 nm p-Si_{0.5}Ge_{0.5}

Si_{0.175}Ge_{0.825}



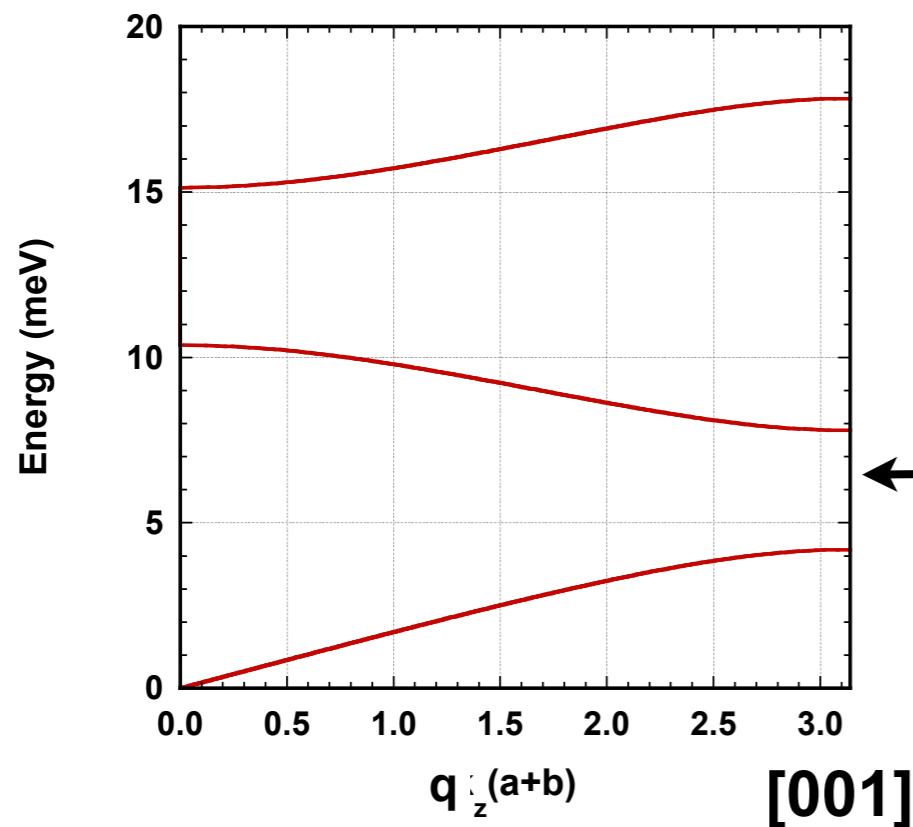
Superlattice $N \rightarrow \infty$



Acoustic mismatch: $\eta = \frac{\rho_b v_b}{\rho_a v_a}$

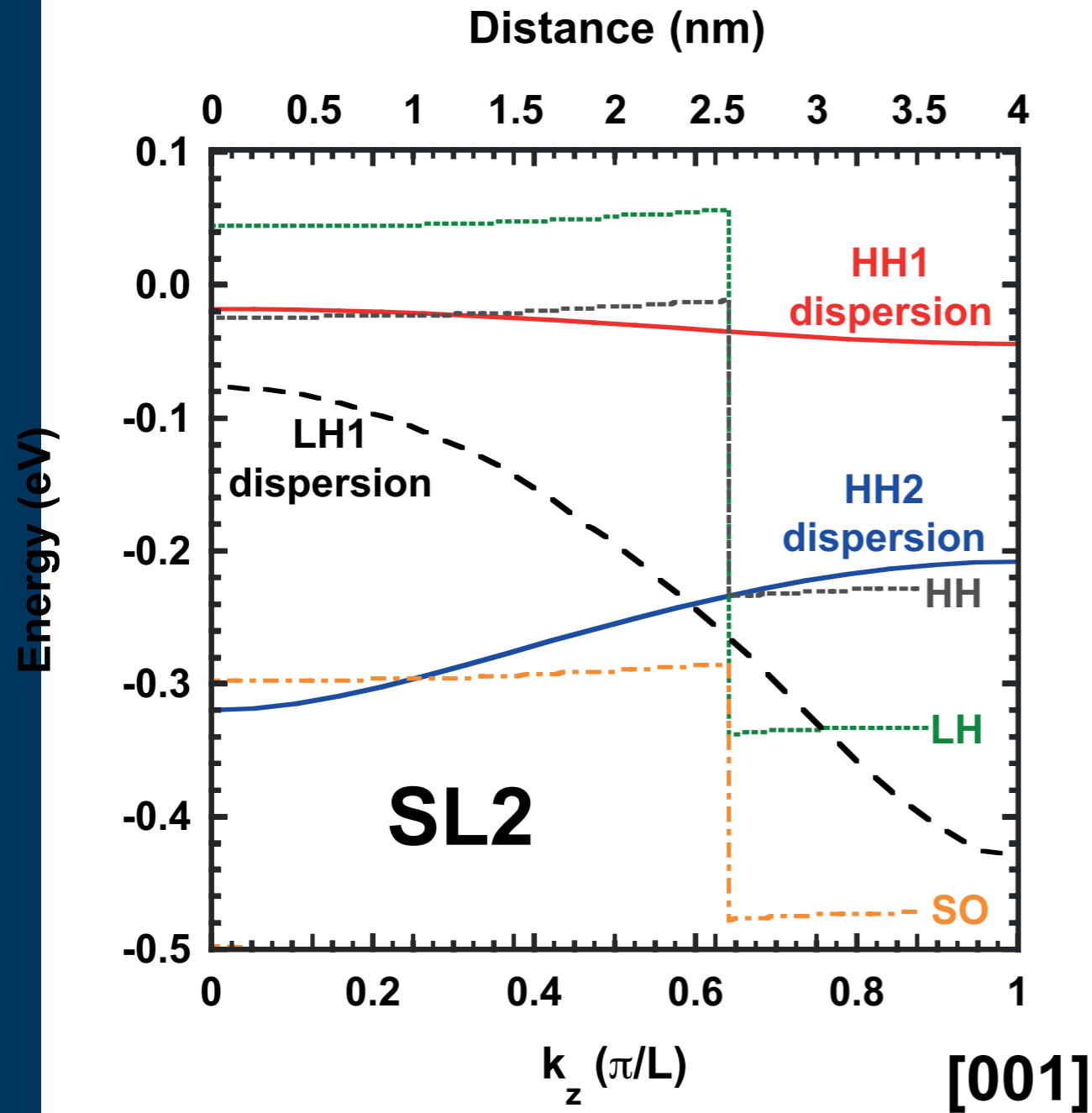
Superlattice zone boundaries: $q_z = \frac{n\pi}{a + b}$

$$\cos q_z (a + b) = \cos q_a a \cos q_b b - \left[\frac{1 + \eta^2}{2\eta} \right] \sin q_a a \sin q_b b$$

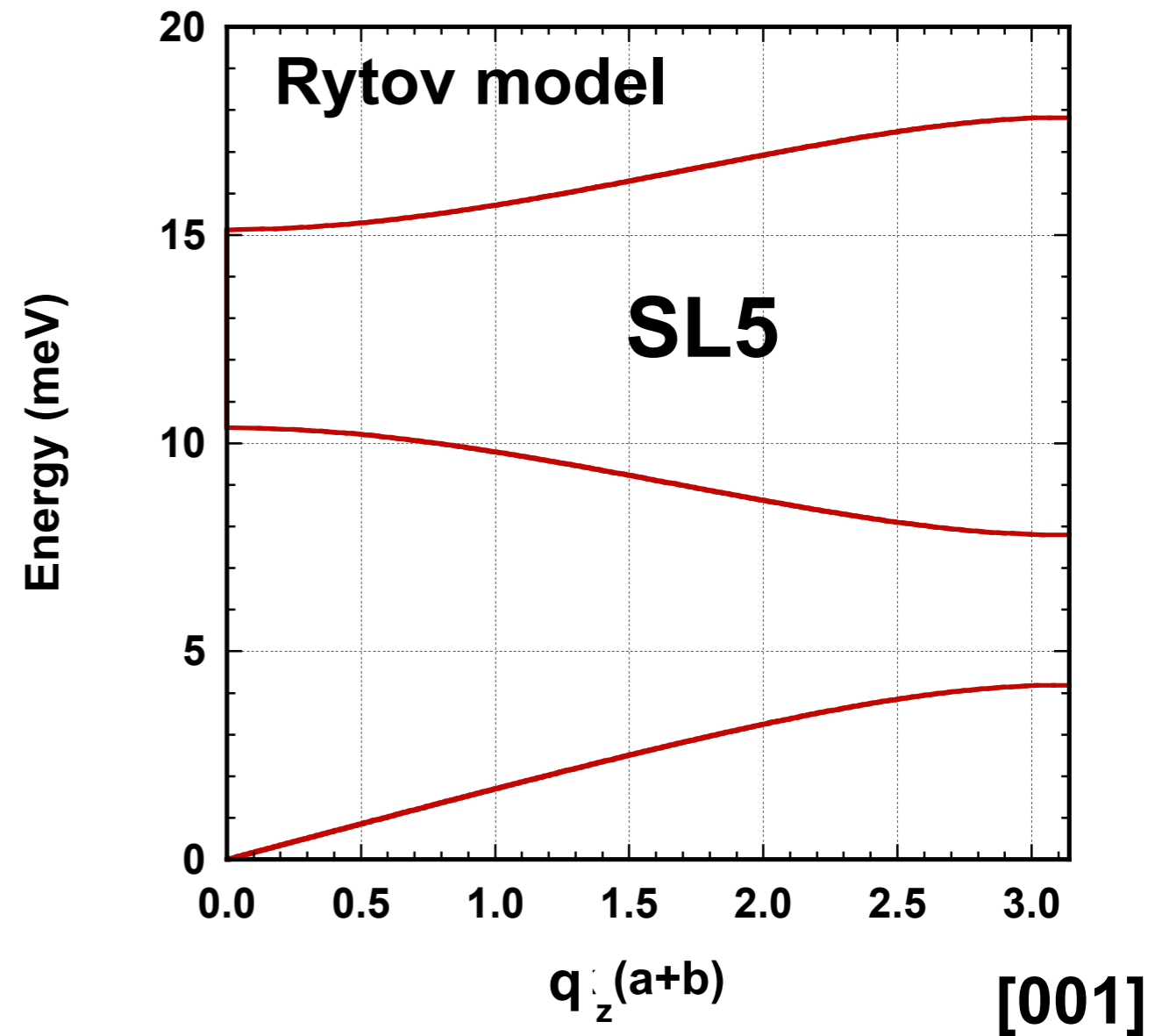


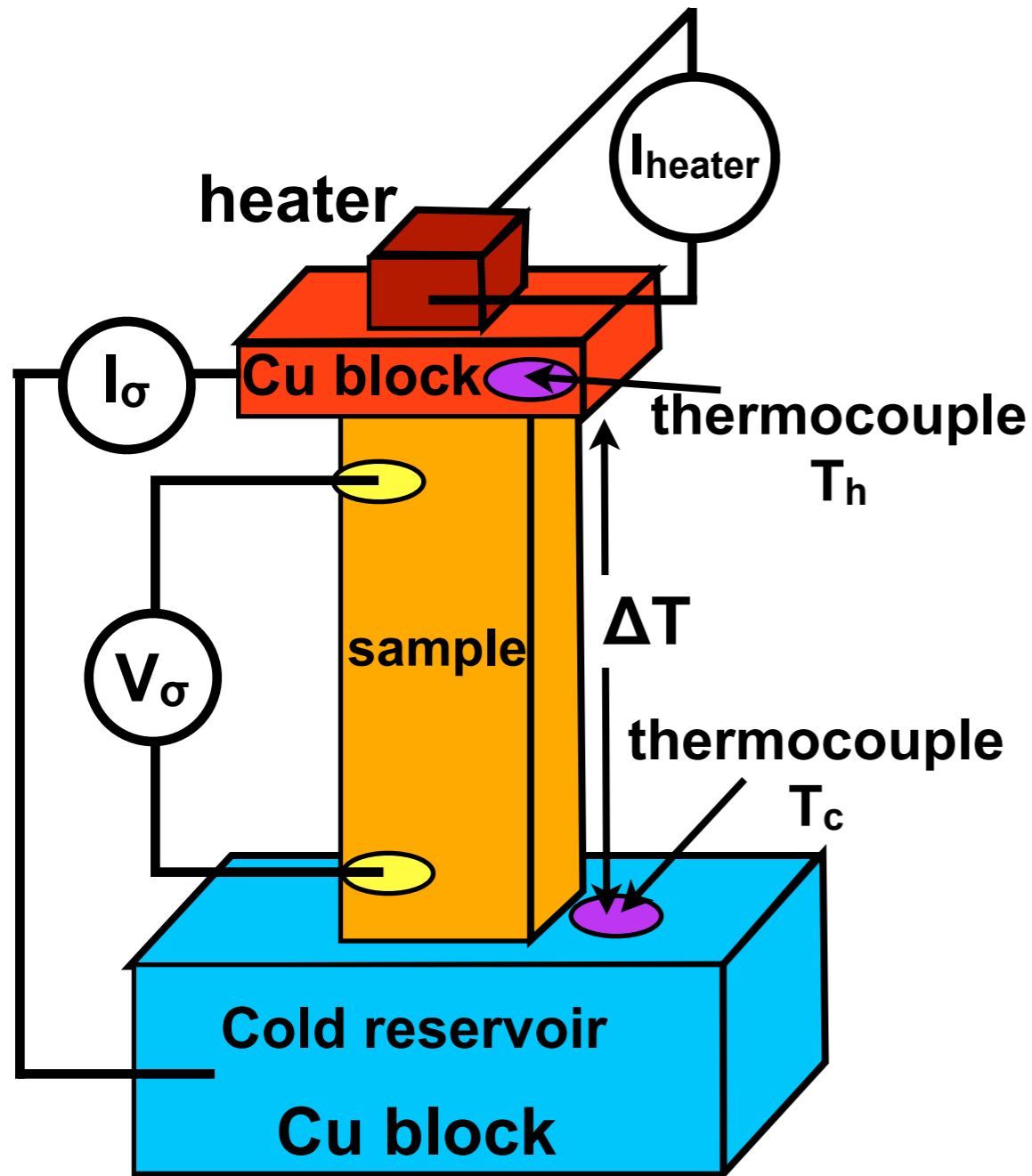
S.V. Rytov, Sov. Phys. Acoustics 2, 67 (1956)

Holes (Electronic Dispersion)

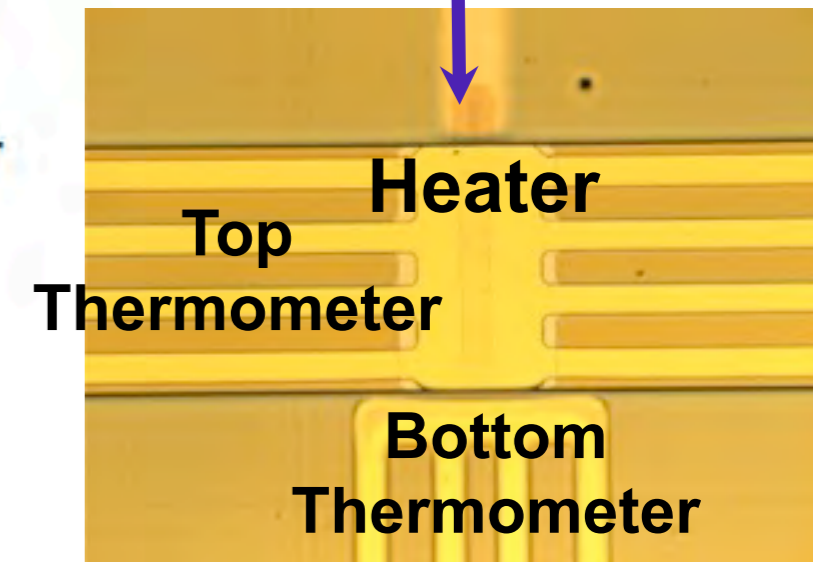
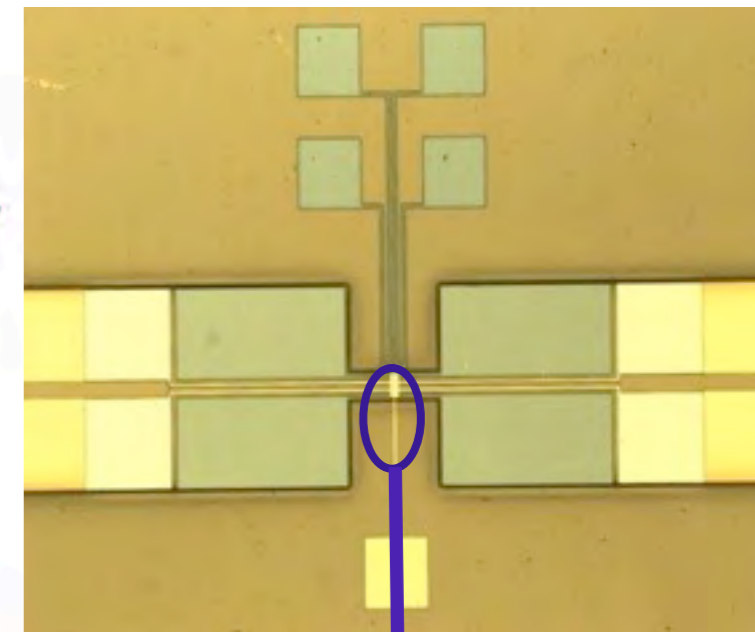
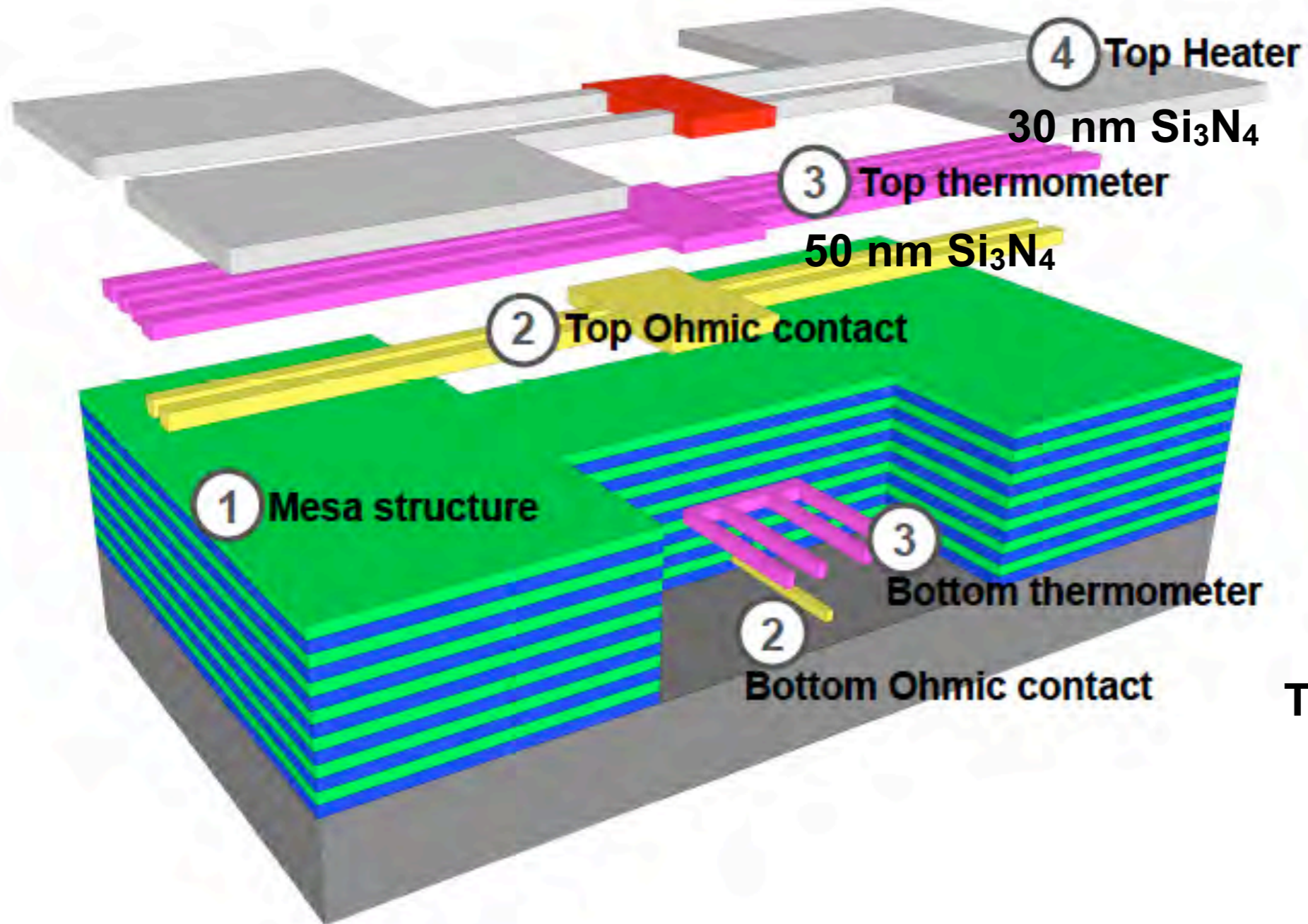


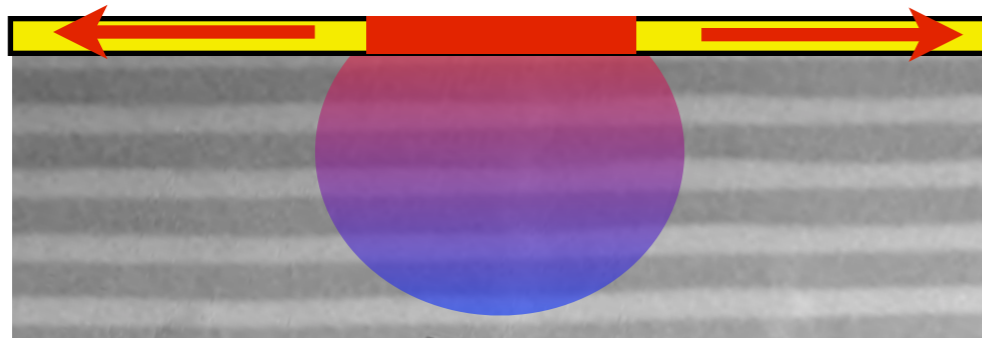
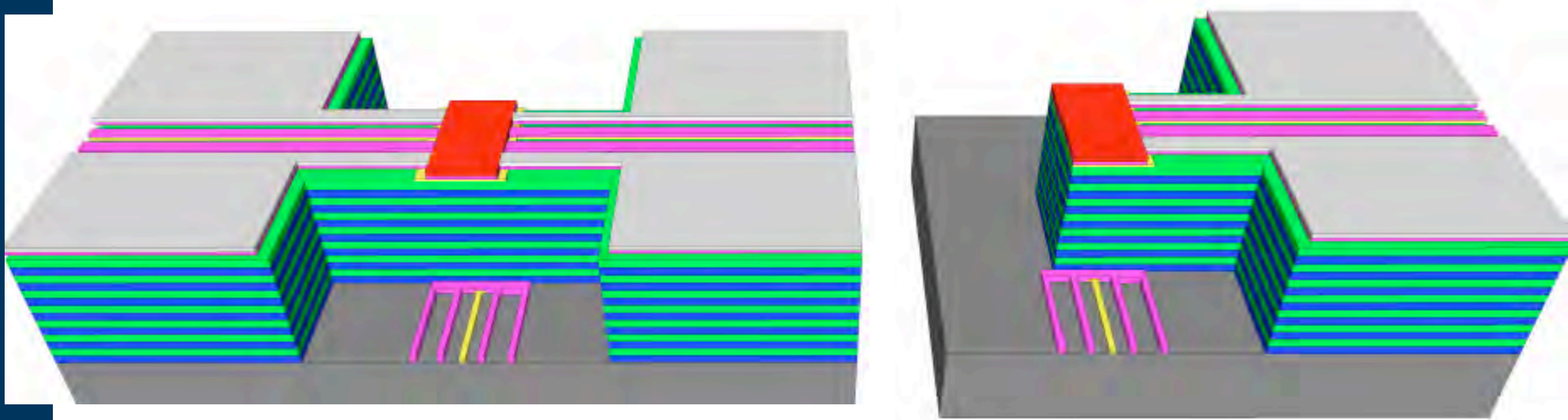
Phonon Dispersion



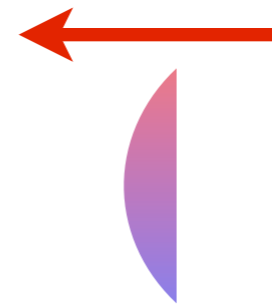


- Physically heat one side of sample
- Cold sink on other side of sample
- Thermocouples top and bottom to measure ΔT
- 4 terminal electrical measurements
- α and σ easy to measure
- Thermal conductivity, κ very difficult to measure

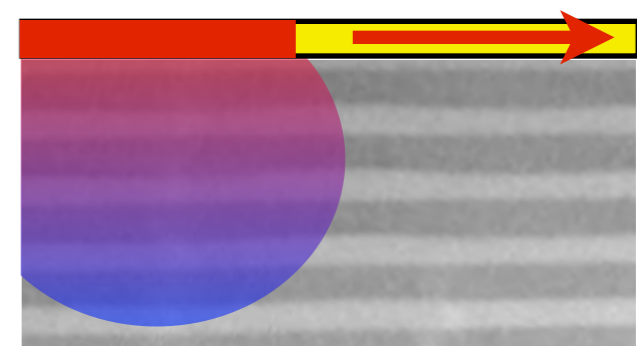




Isotropic structure



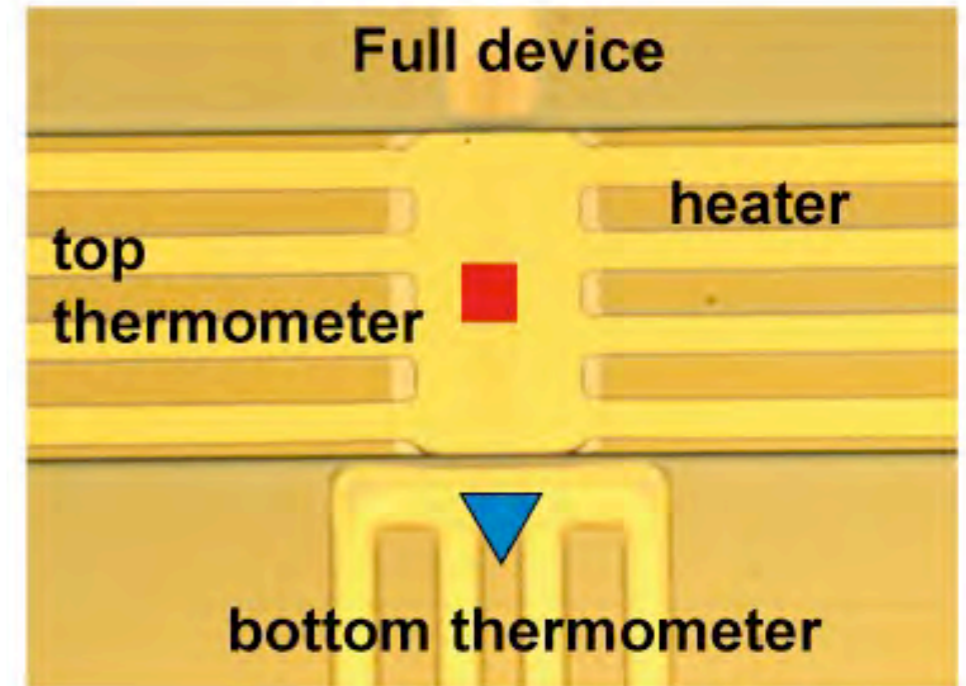
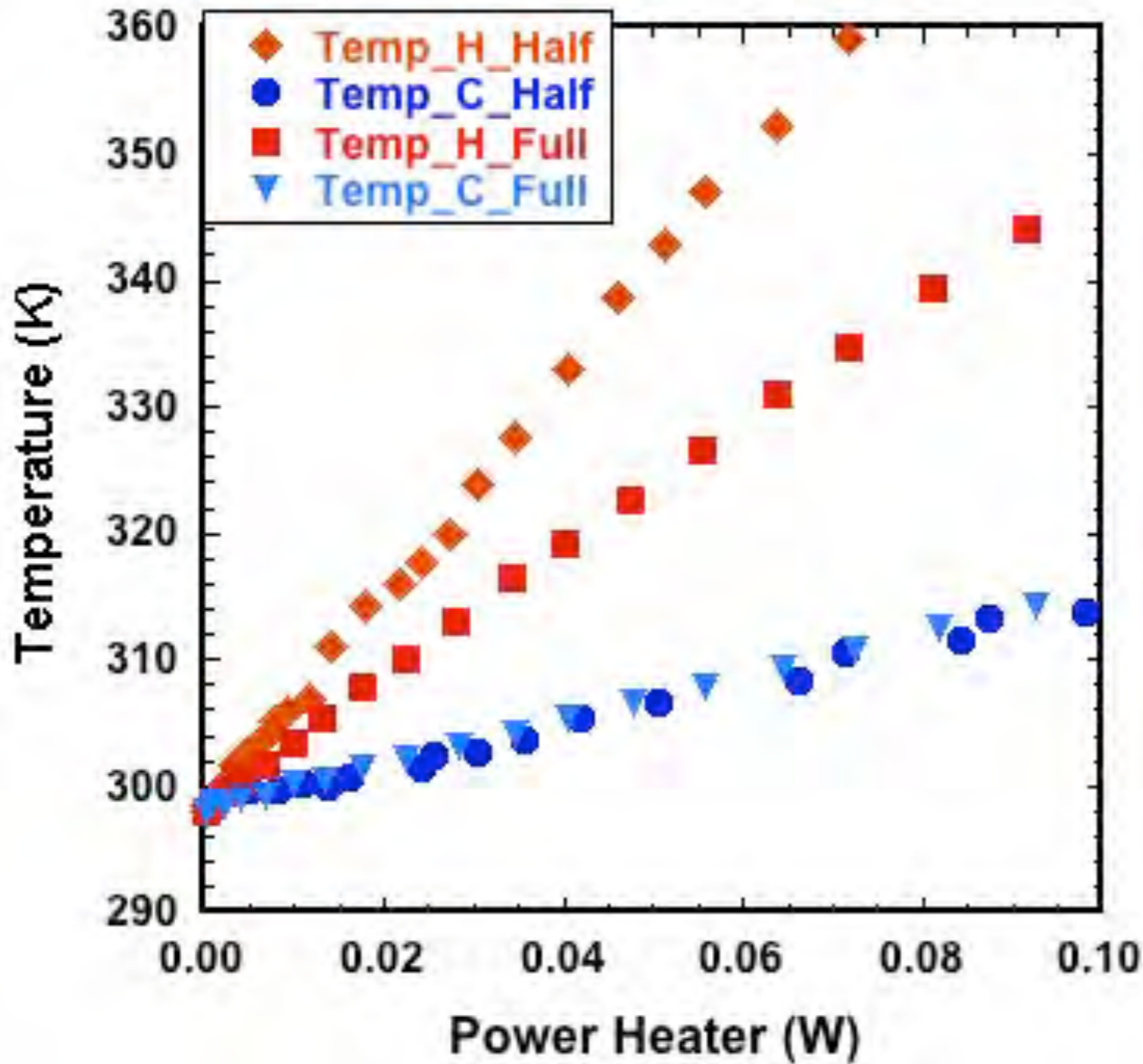
1/2 lateral
parasitic
contribution



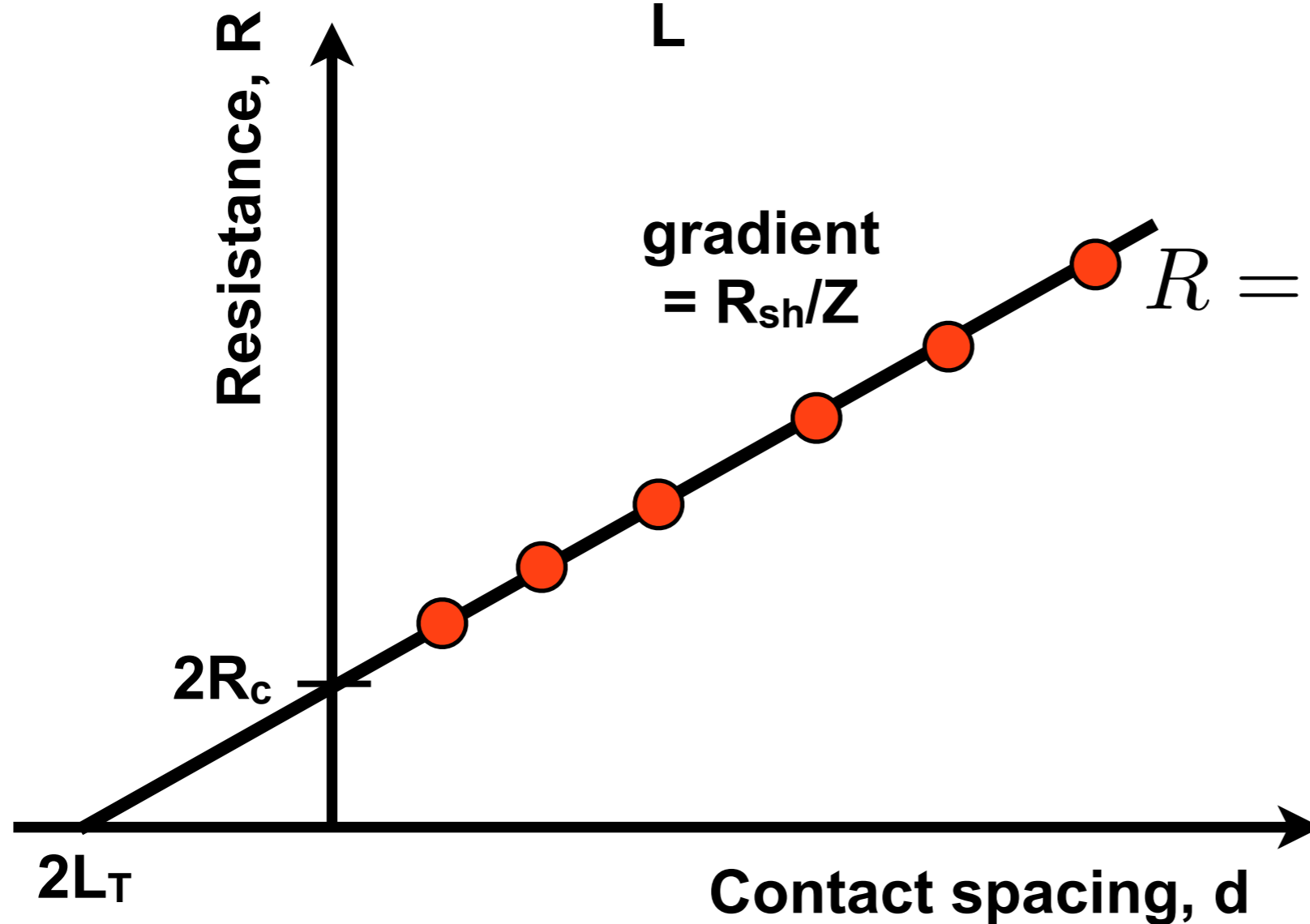
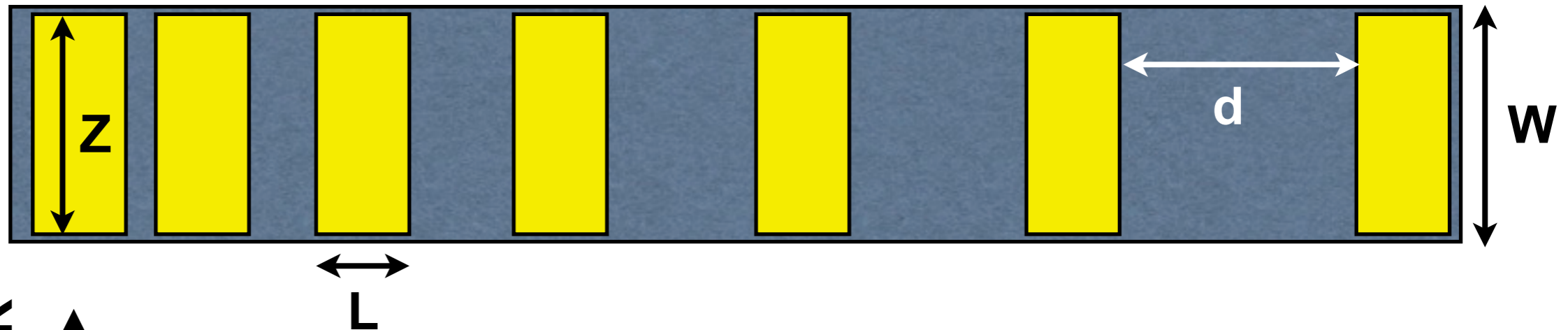
half structure



Half structure allows parasitics to be measured and removed for more accurate heat flux determination



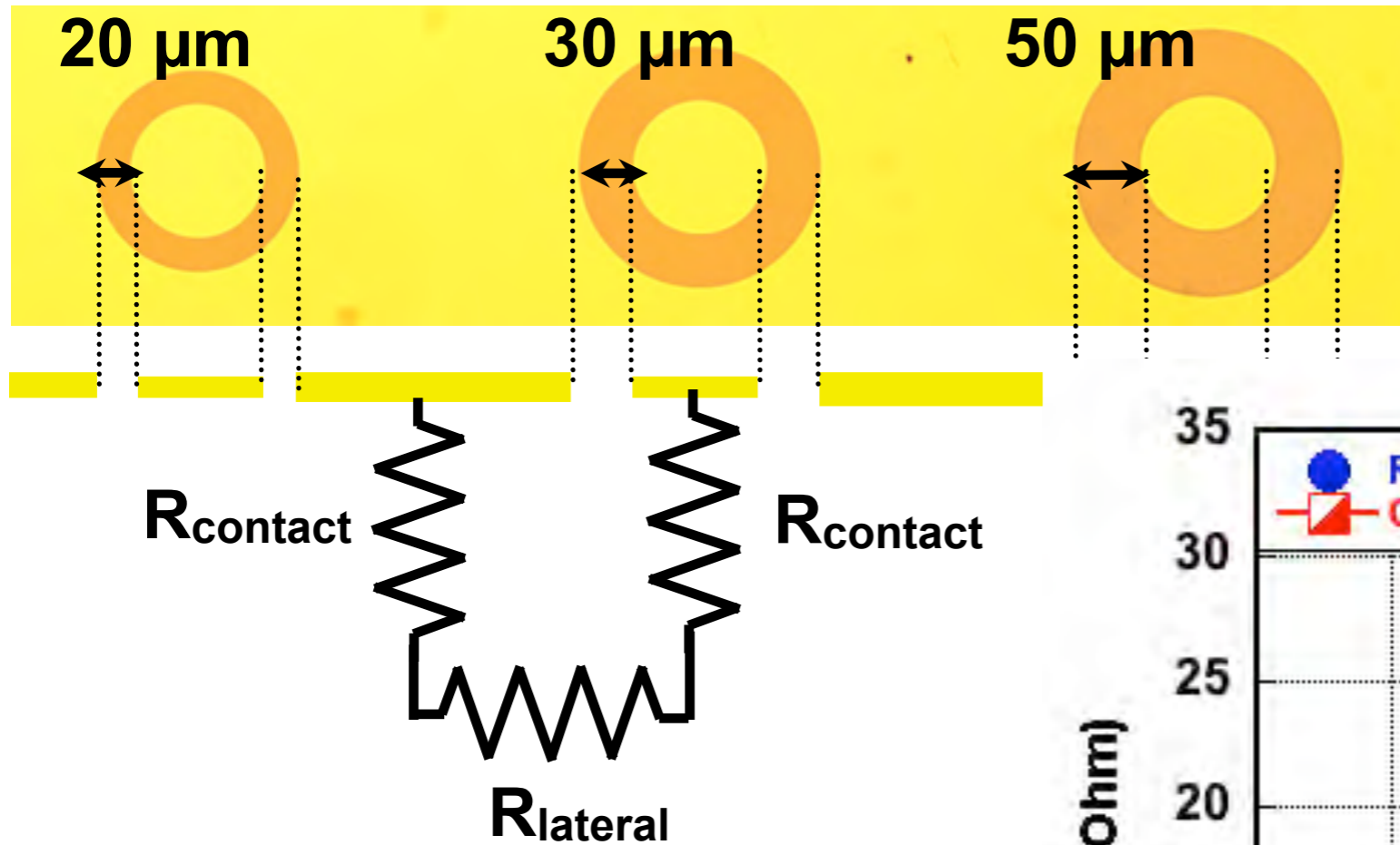
Measured 41% of heat in vertical transport



$$R = \frac{R_{sh}d}{Z} + 2R_c$$

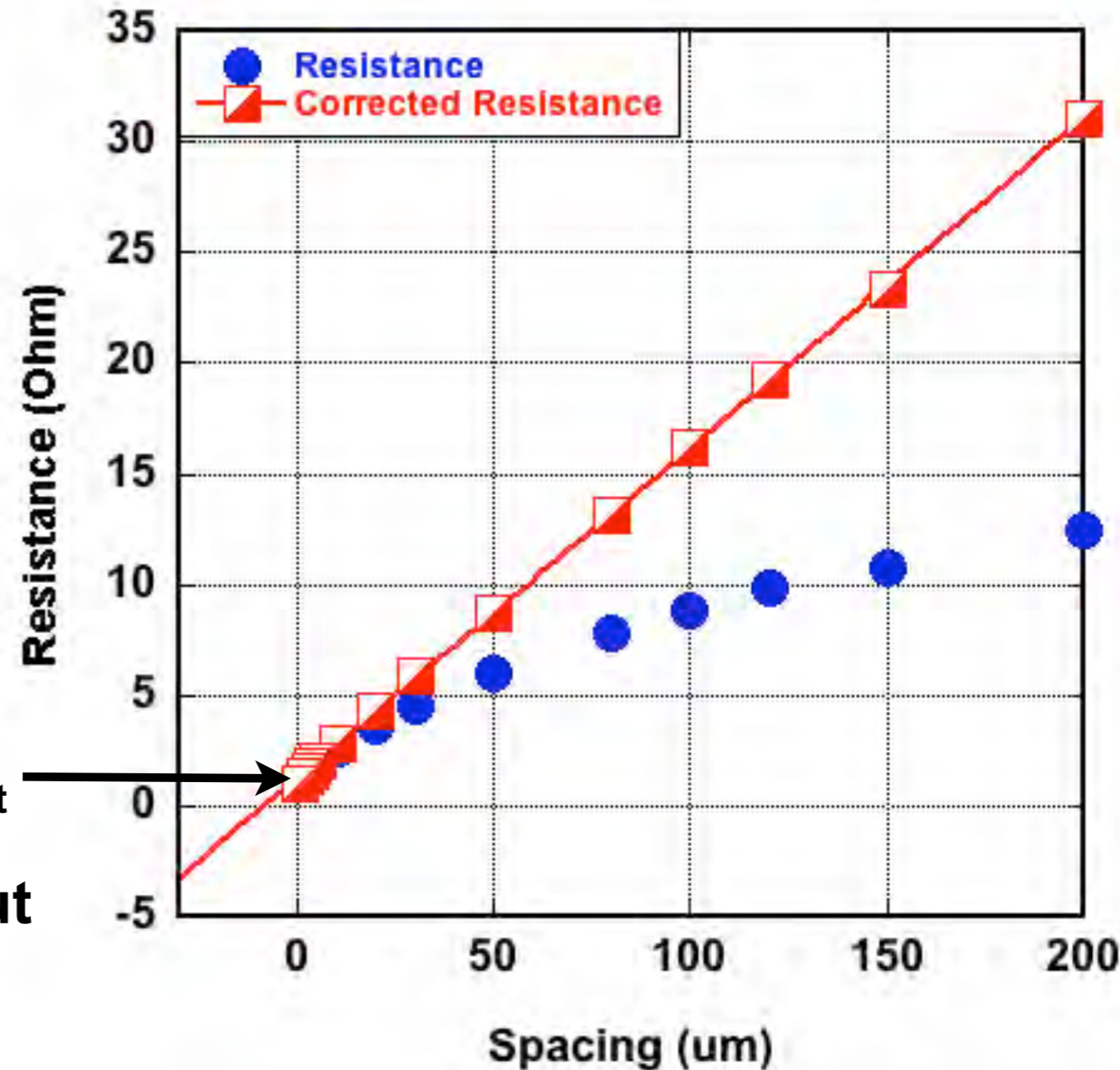
$$\rho_c = L_T^2 R_{sh}$$

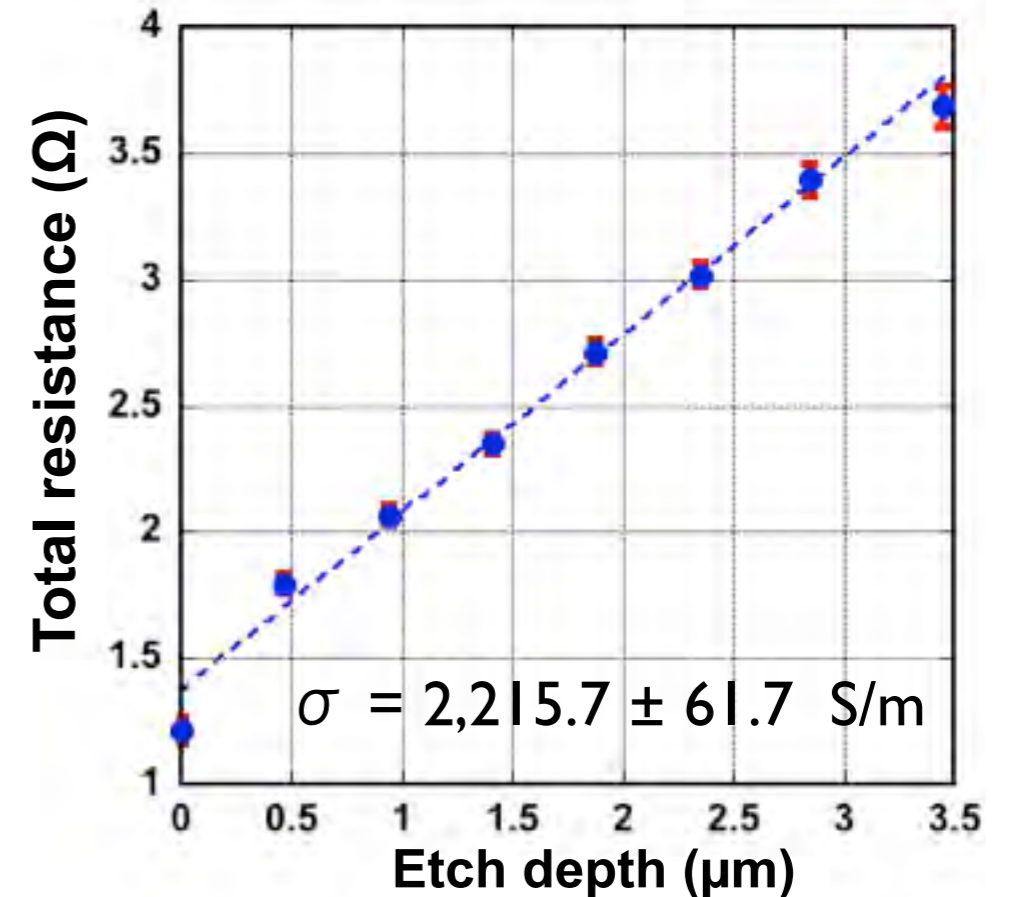
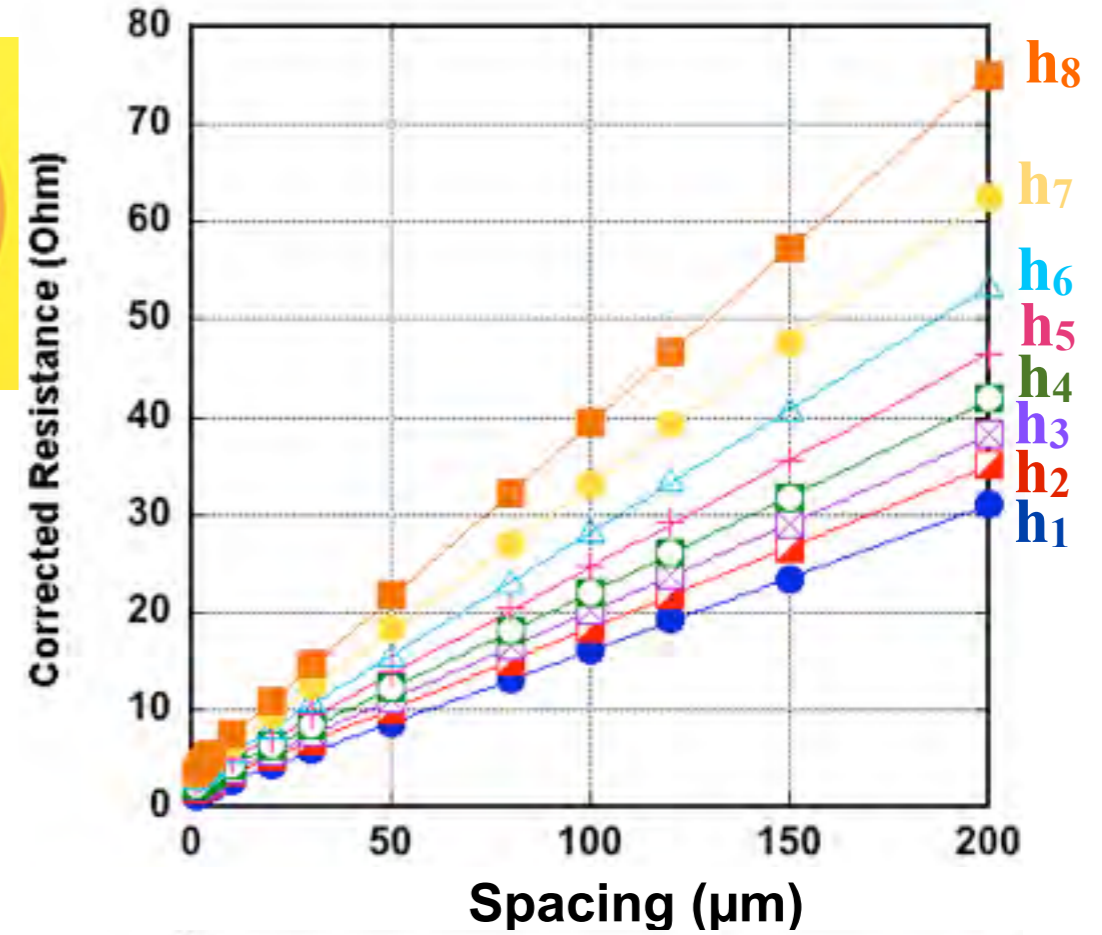
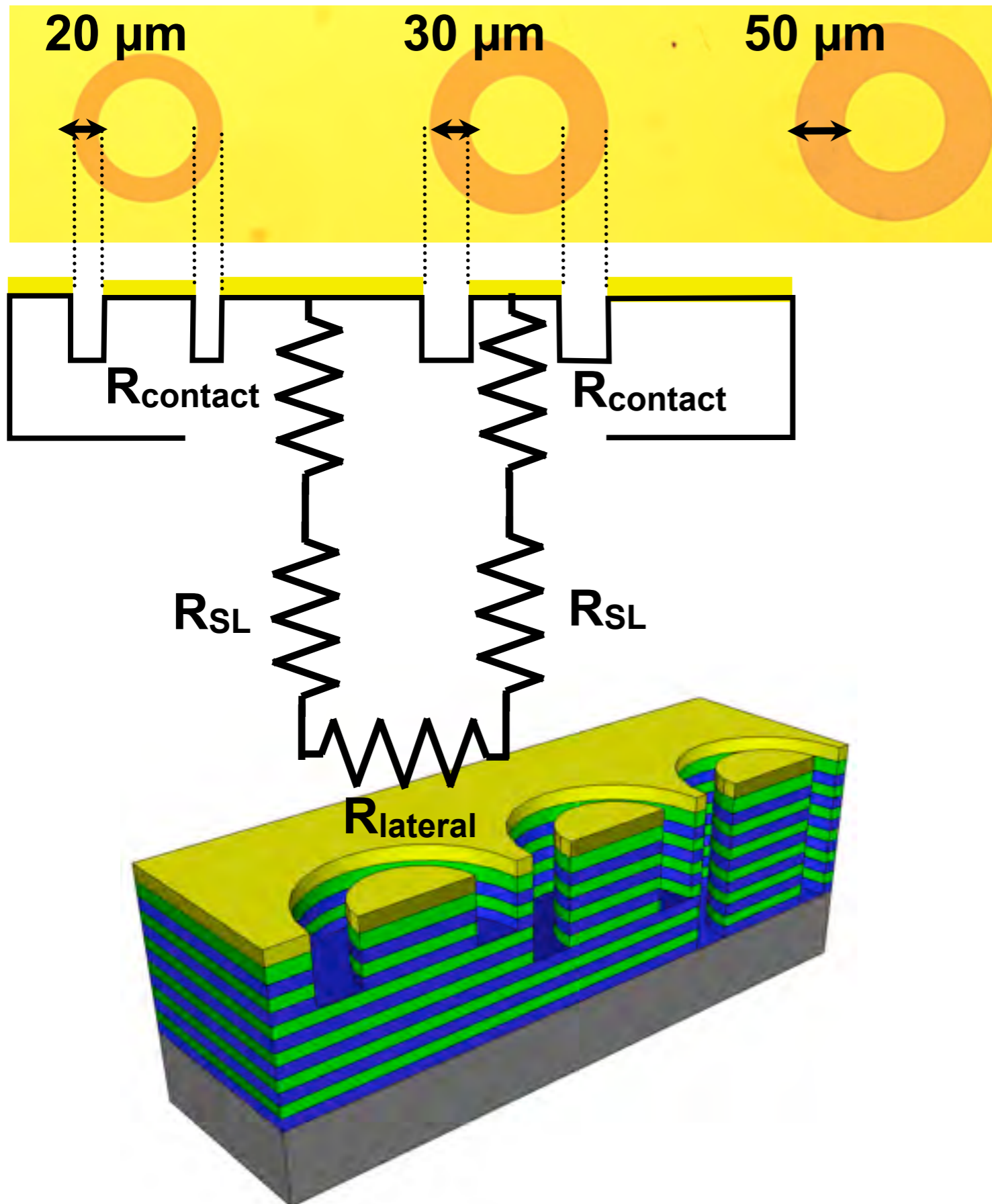
● Any misalignment or gaps results in errors → circular TLMs



● **Circular Transfer Line Method**

● **Higher accuracy than TLM but correction factor required**

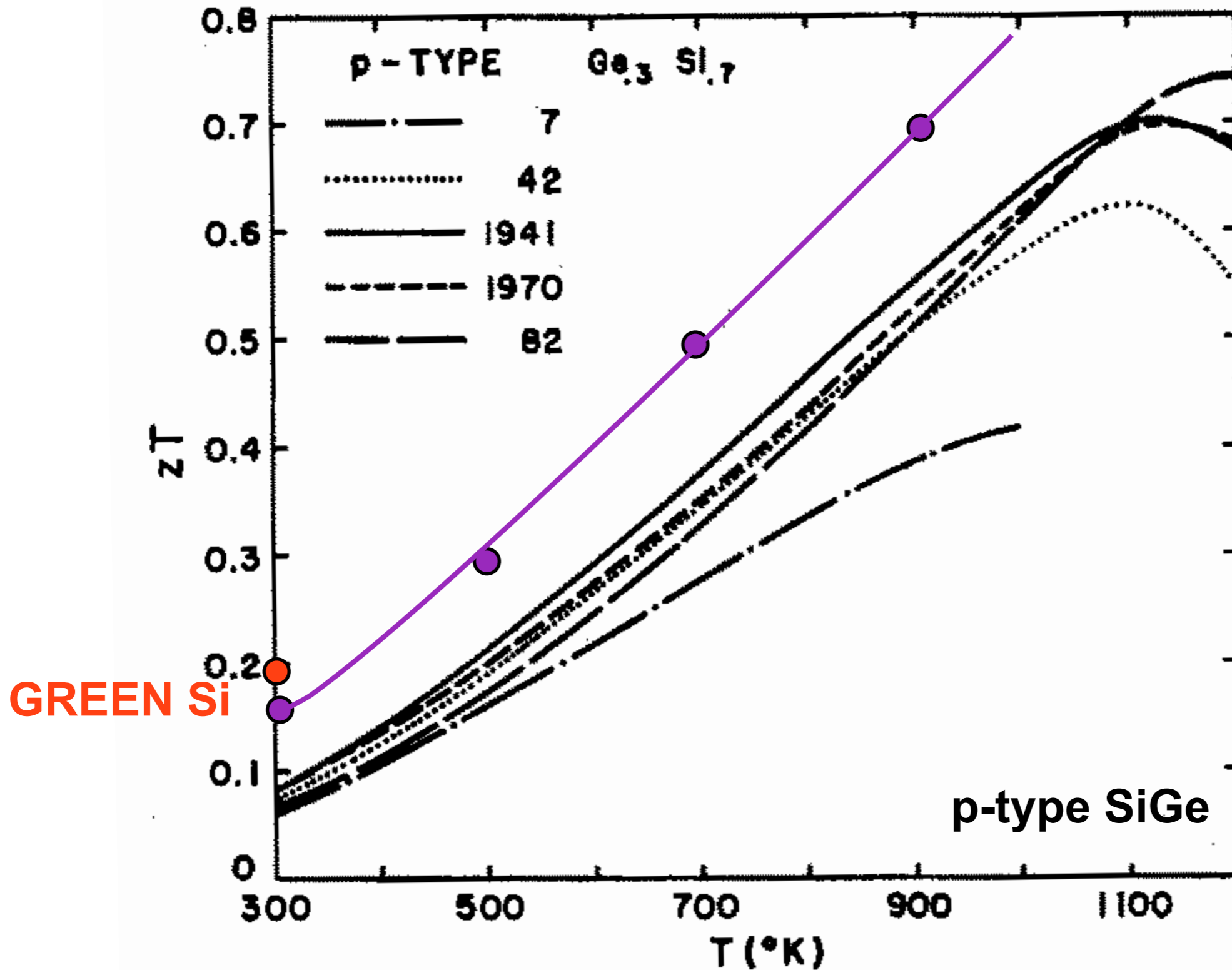




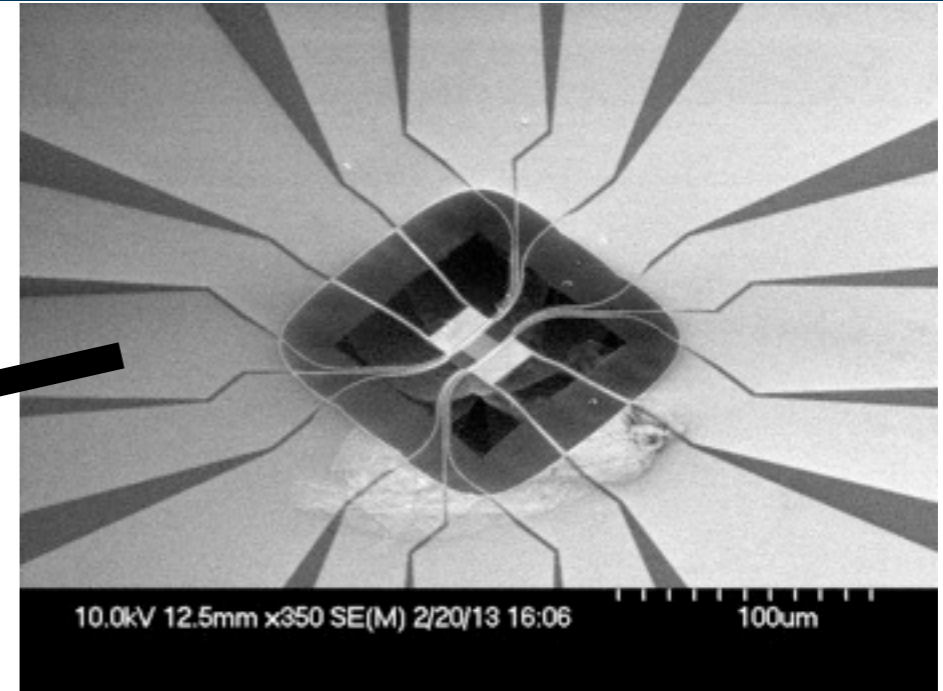
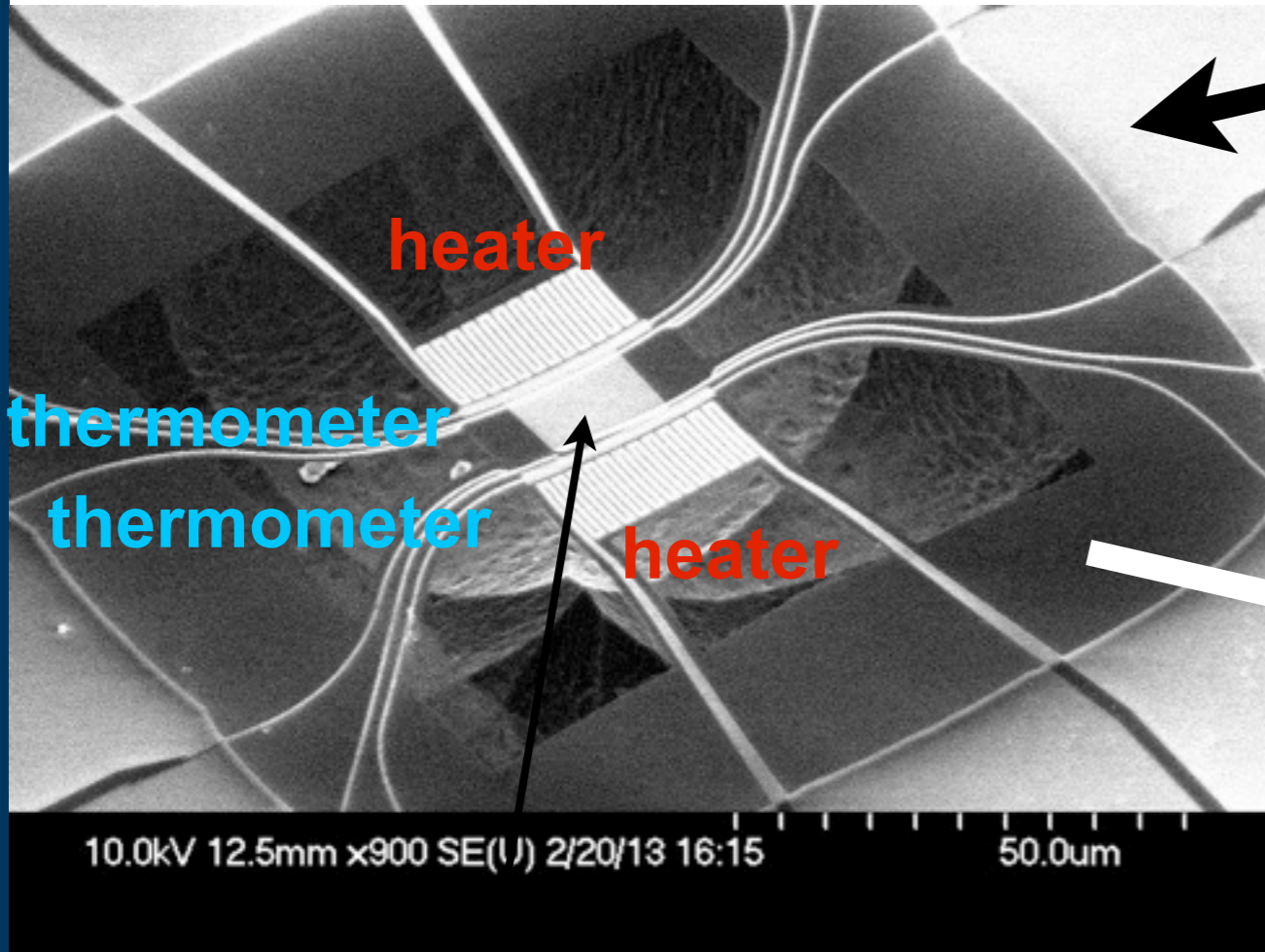
- **Many materials with $ZT > 1.5$ reported but few confirmed by others (!)**
- **No modules demonstrated with such high efficiencies**
- **Due to: measurement uncertainty & complexity of fabricating devices**
- $$\frac{\Delta(ZT)}{ZT} = 2 \frac{\Delta\alpha}{\alpha} + \frac{\Delta\sigma}{\sigma} + \frac{\Delta\kappa}{\kappa} + \frac{\Delta T}{T}$$

Δx = uncertainty in x = standard deviation in x
- **Measurements are conceptually simple but results vary considerably due to thermal gradients in the measurements → systematic inaccuracies**
- **Total ZT uncertainty can be between 25% to 50%**

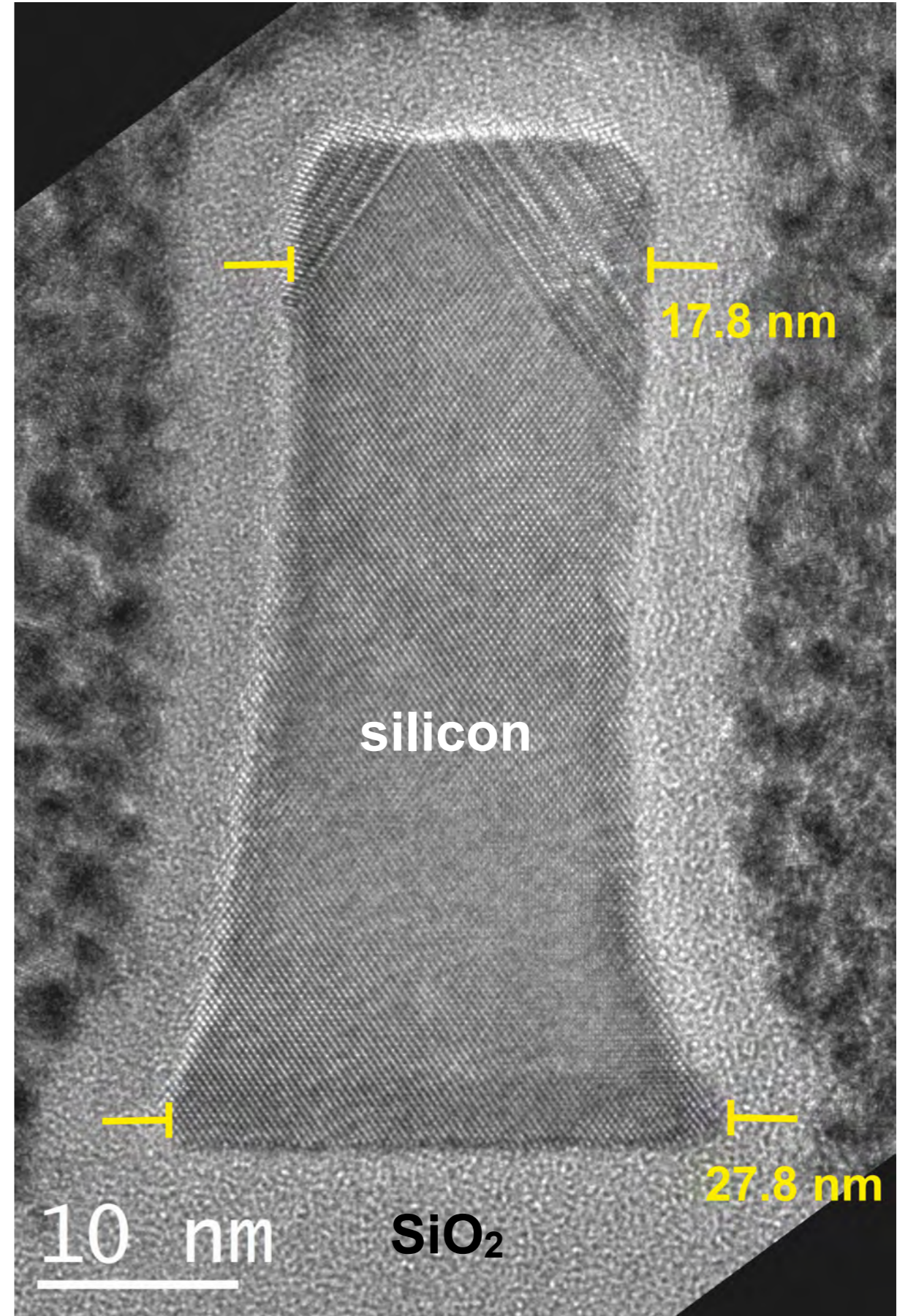
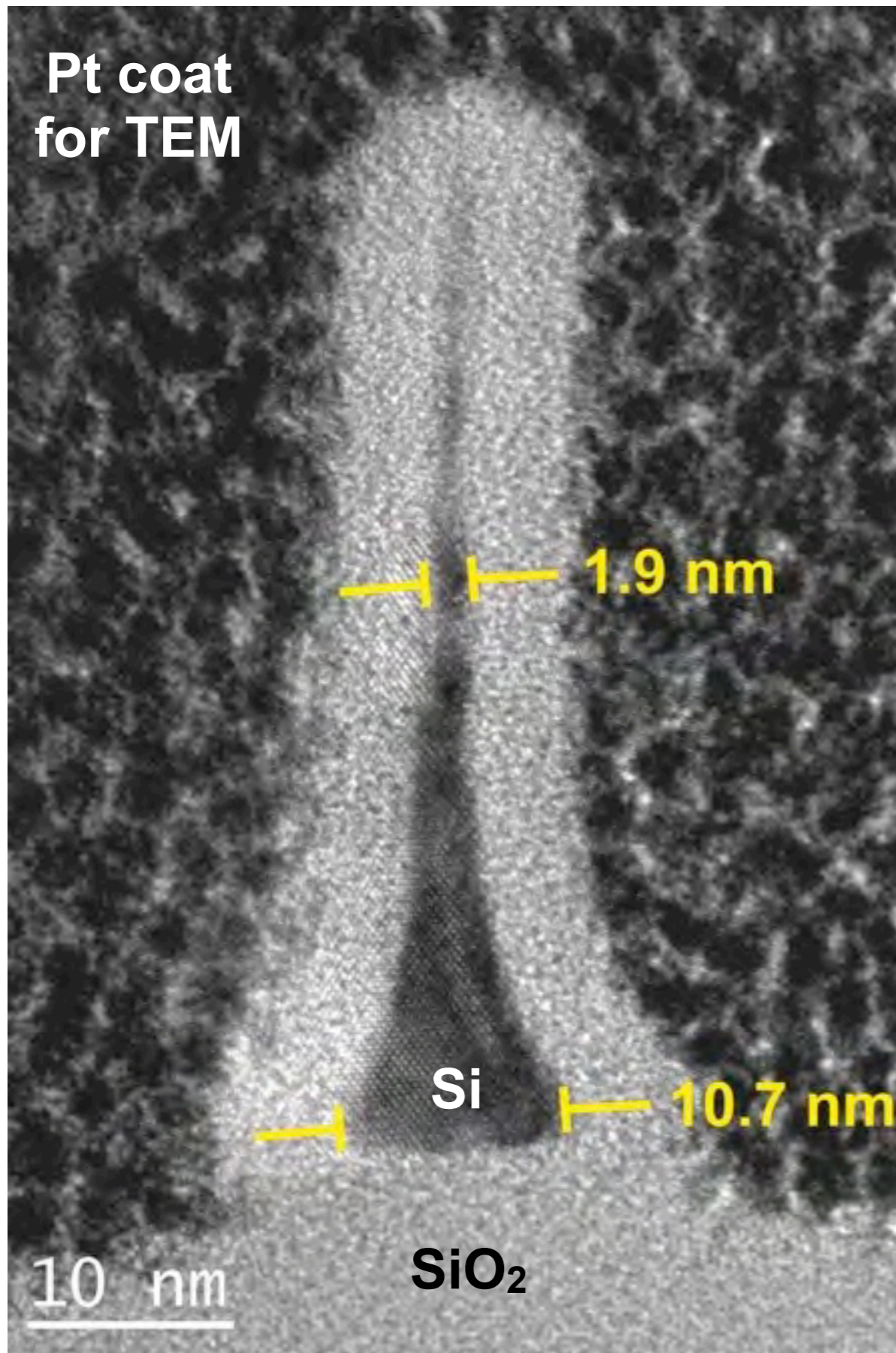
MIT, Nano Lett. 8, 4670 (2008)

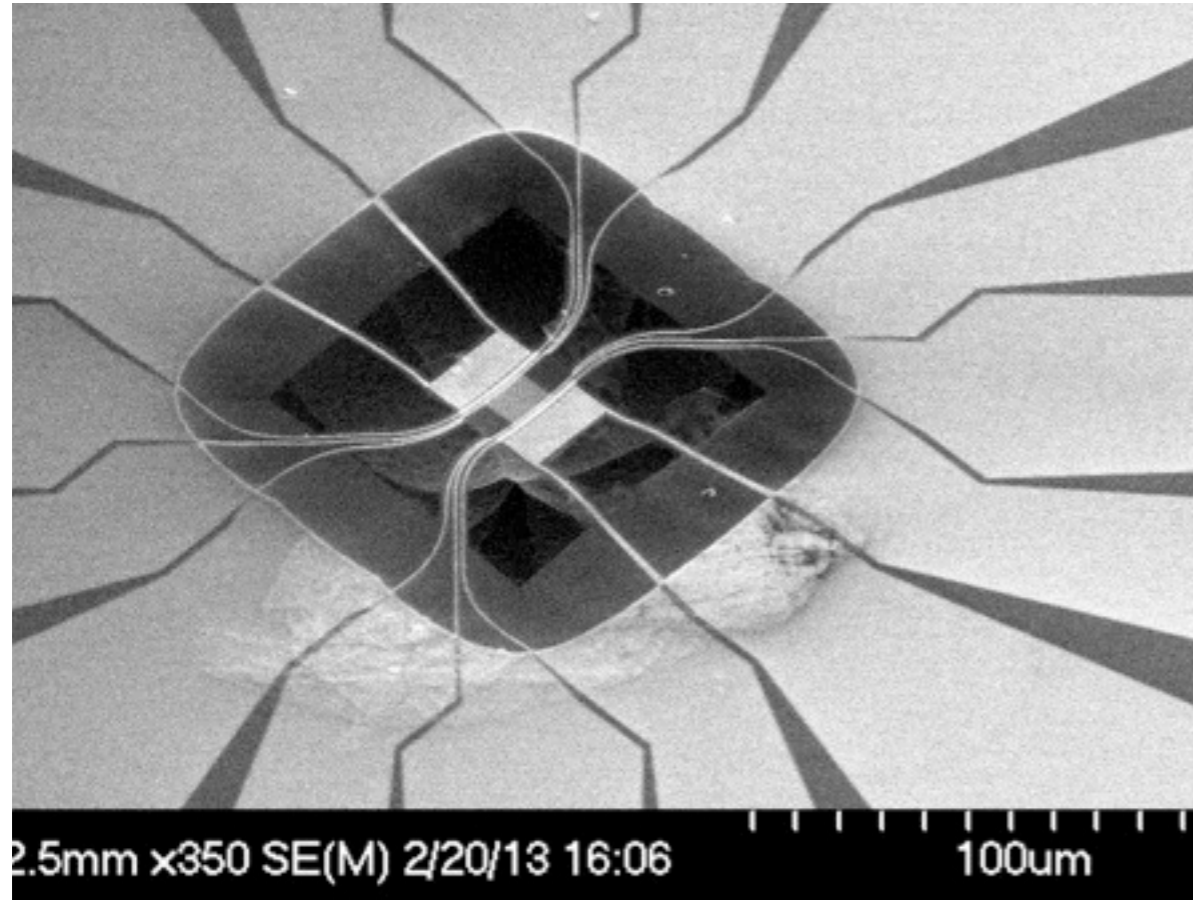


J.P. Dismukes et al., J. Appl. Phys. 35, 2899 (1964)

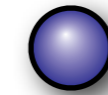


 **100 x 45 nm wide Si nanowires with integrated heaters, thermometers and electrical probes**

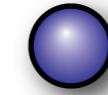




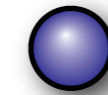
@ 300 K:



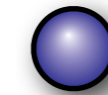
$\sigma = 20,300 \text{ S/m}$
4 terminal



$\kappa = 7.78 \text{ W/mK}$



$\alpha = -271 \mu\text{V/K}$



$ZT = 0.057$



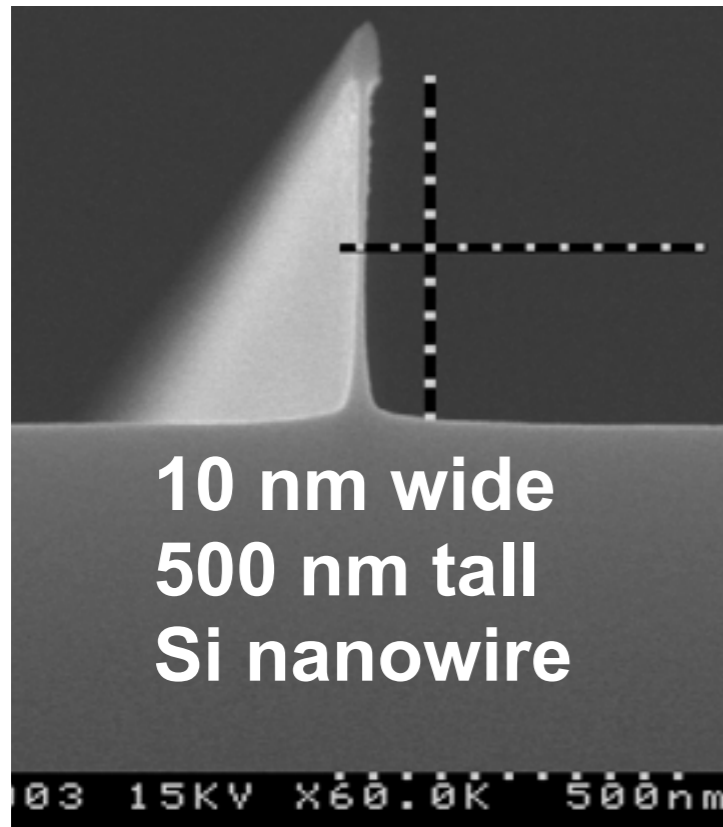
ZT enhanced by x117



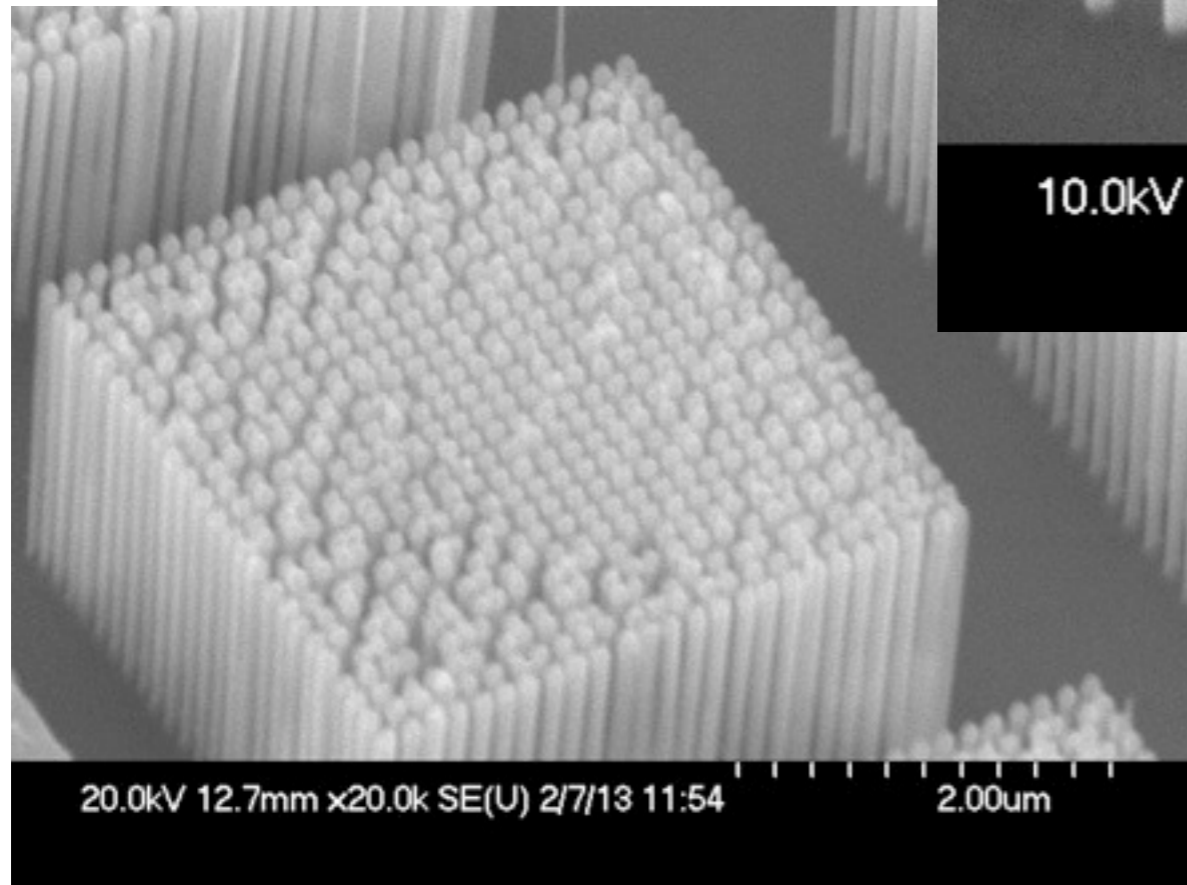
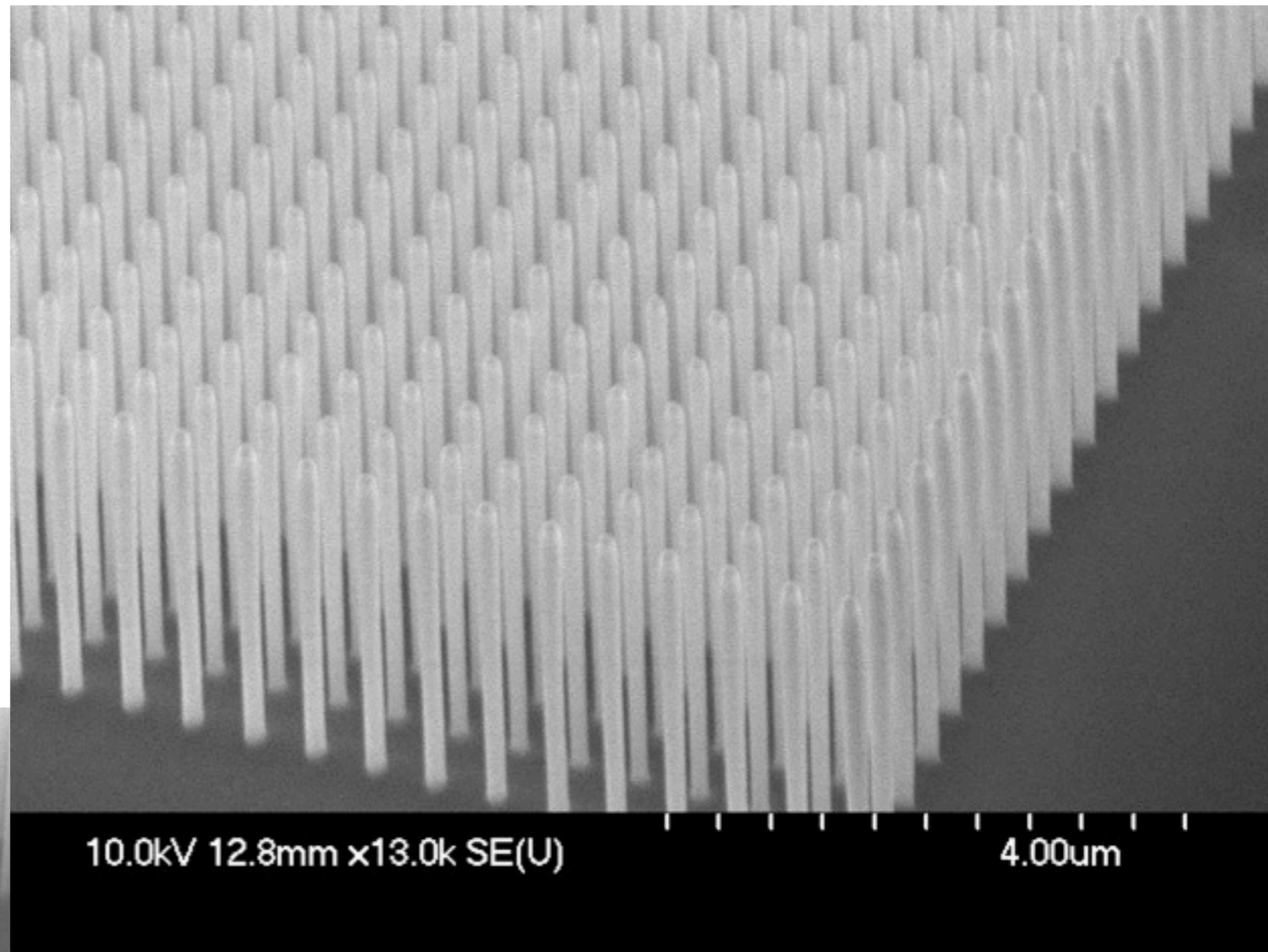
$\alpha^2\sigma = 1.49 \text{ mW m}^{-1}\text{K}^{-2}$



**What enhancements
with SiGe ?**



Si etch



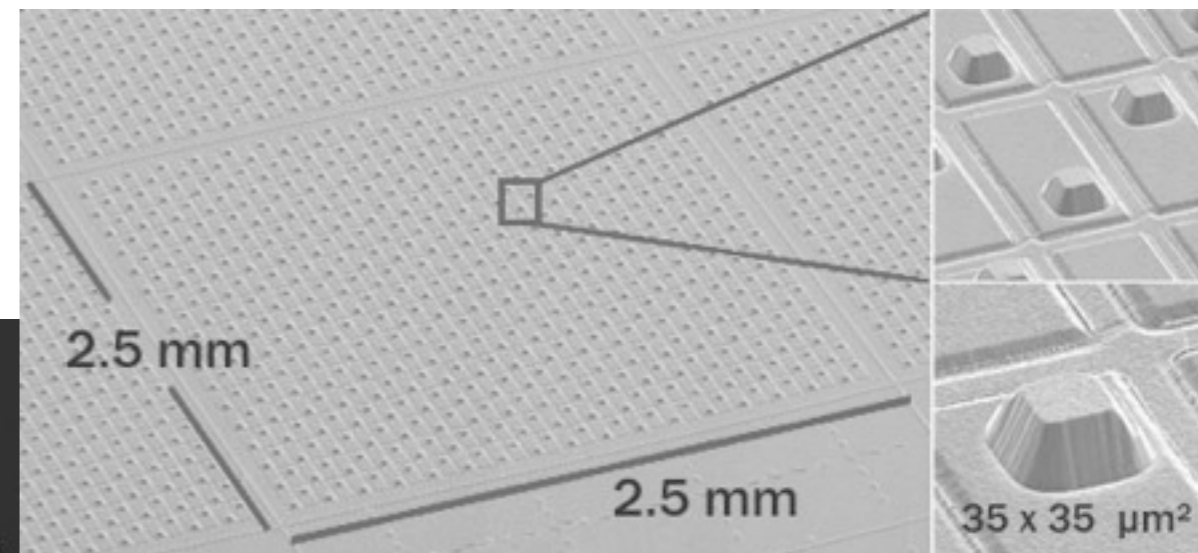
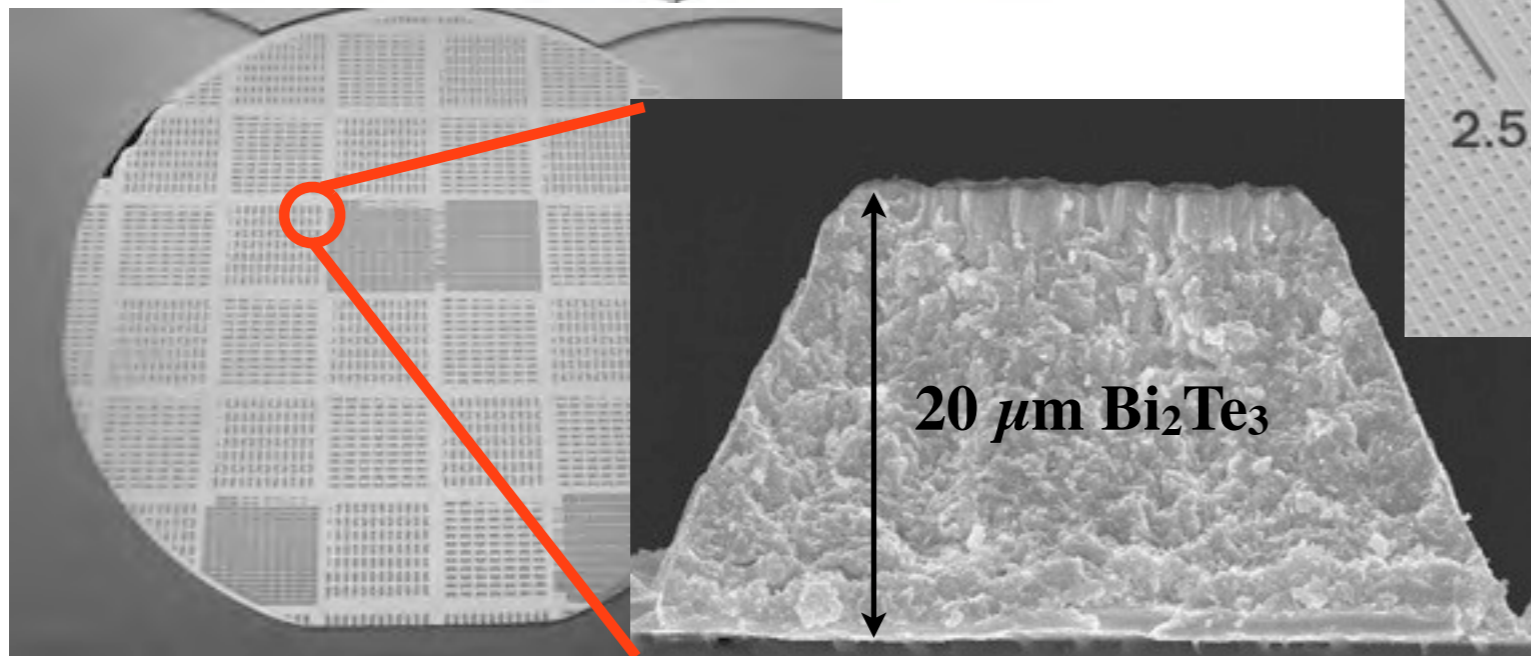
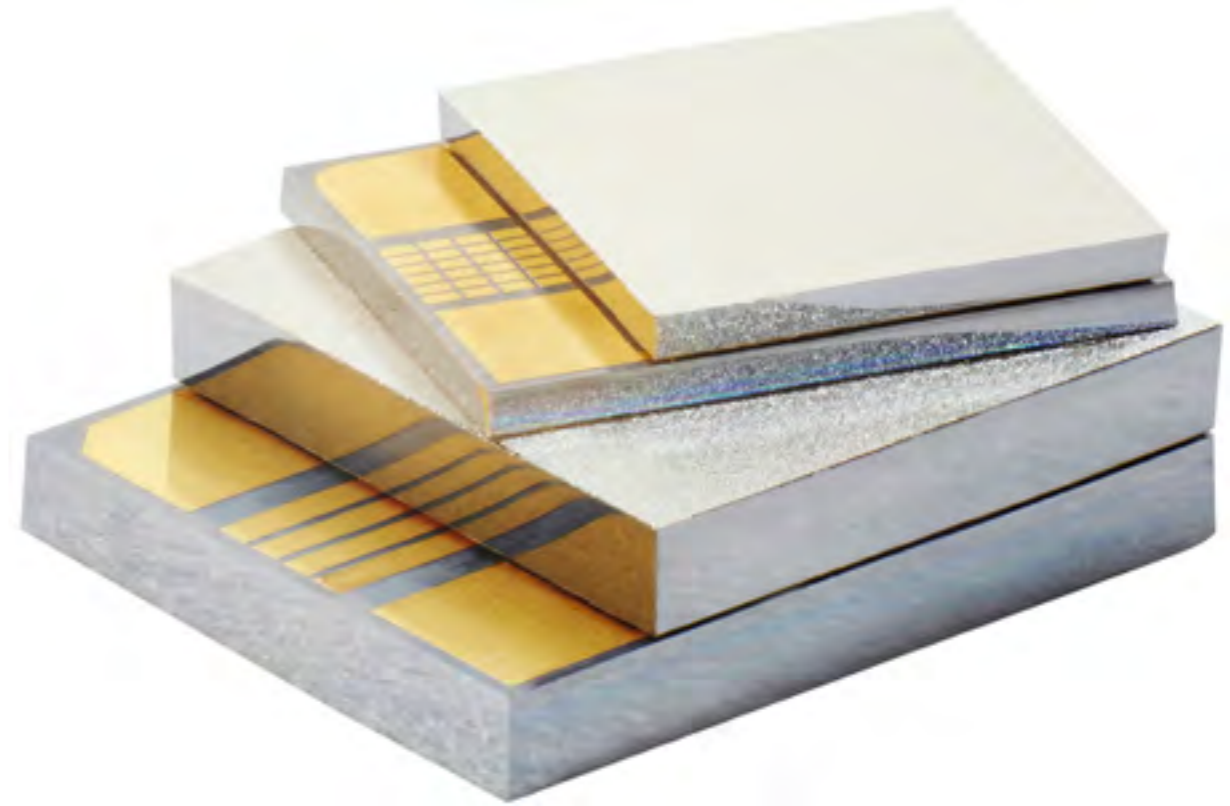
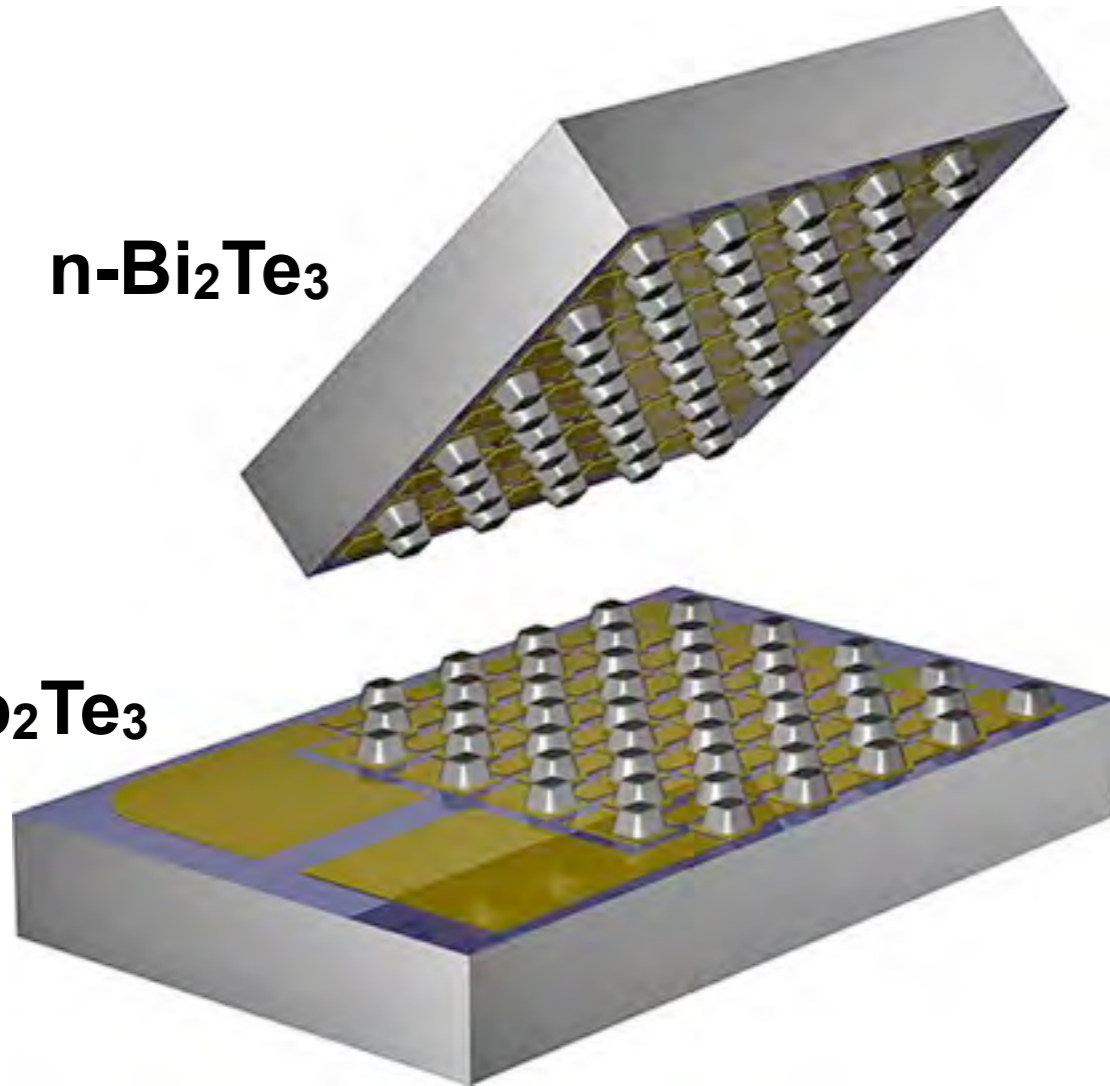
High density nanowires

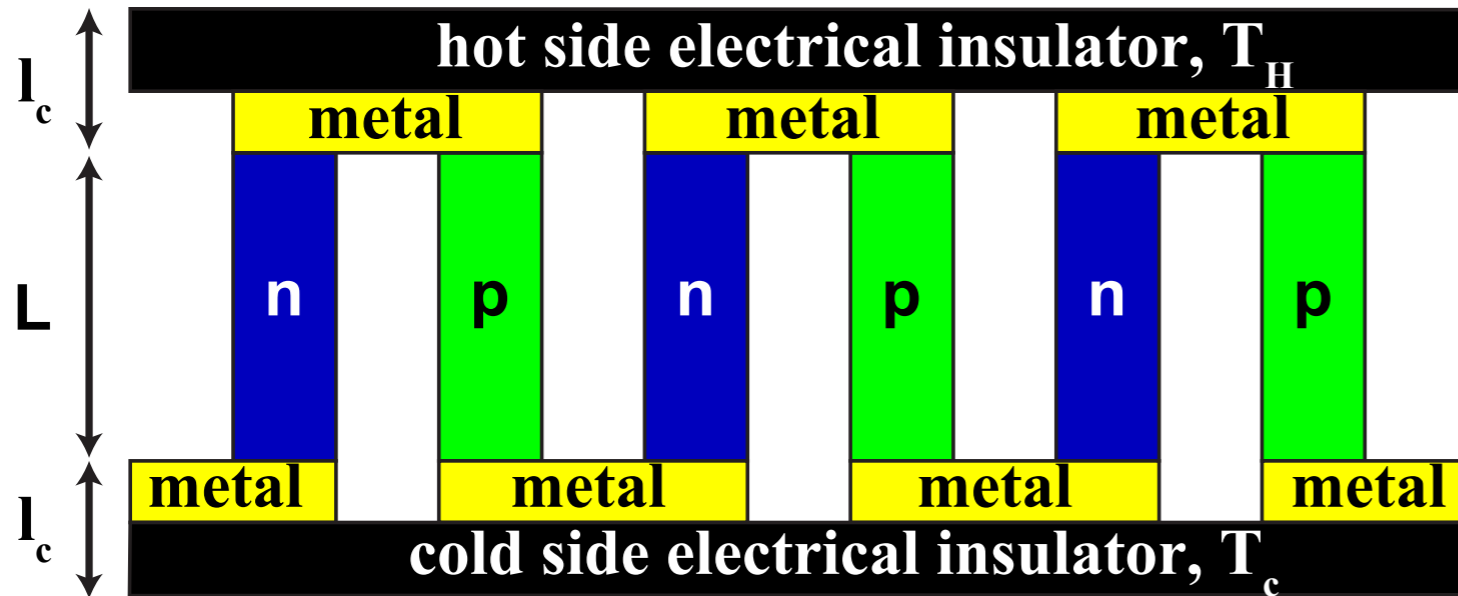
50 nm Ge/SiGe nanowires

4 μm deep etched

n-Bi₂Te₃

p-Sb₂Te₃





A = module leg area

L = module leg length

N = number of modules

κ_c = thermal contact conductivity

ρ_c = electrical contact resistivity

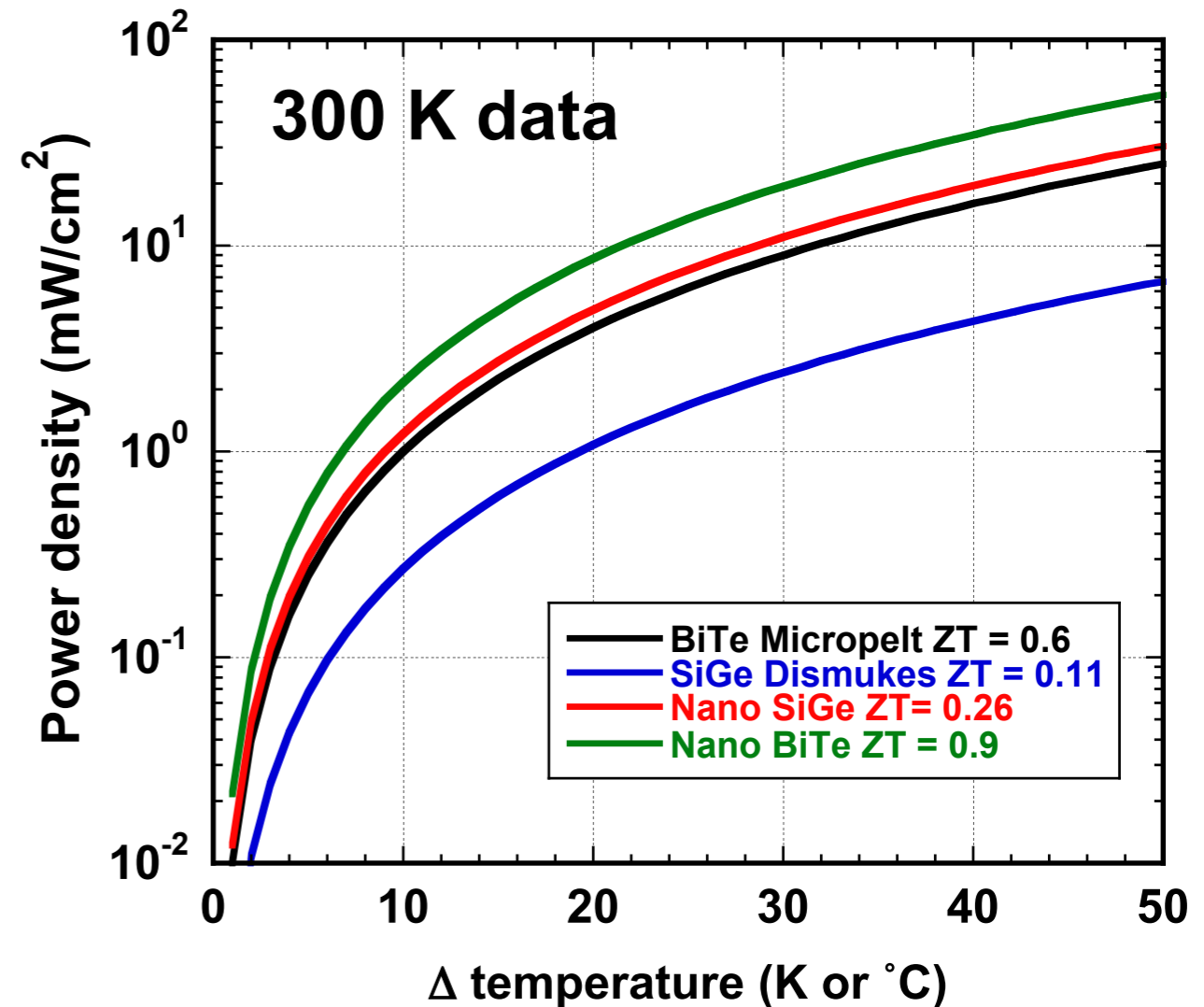
$$P = \frac{\alpha^2 \sigma AN \Delta T^2}{2(\rho_c \sigma + L) \left(1 + 2 \frac{\kappa l_c}{\kappa_c L}\right)^2}$$

D.M. Rowe & M. Gao, IEE Proc. Sci. Meas. Technol. 143, 351 (1996)

● System: power in BiTe alloys limited by Ohmic contacts

● $\rho_c (\text{Bi}_2\text{Te}_3) \cong 1 \times 10^{-7} \Omega\text{-cm}^2$

● $\rho_c (\text{Si}_{1-x}\text{Ge}_x) = 1.2 \times 10^{-8} \Omega\text{-cm}^2$



- D.M. Rowe (Ed.), "*Thermoelectrics Handbook: Macro to Nano*"
CRC Taylor and Francis (2006) ISBN 0-8494-2264-2
- G.S. Nolas, J. Sharp and H.J. Goldsmid "*Thermoelectrics: Basic Principles and New Materials Development*" (2001) ISBN 3-540-41245-X
- M.S. Dresselhaus et al. "*New directions for low-dimensional thermoelectric materials*" Adv. Mat. 19, 1043 (2007)
- D.J. Paul, "*Thermoelectric Energy Harvesting*" Intech Open Access from
"ICT - Energy - Concepts Towards Zero - Power Information &
Communication Technology " (2014) - DOI: [10.5772/57347](https://doi.org/10.5772/57347)

**Contact: Prof Douglas Paul
Douglas.Paul@glasgow.ac.uk
Tel:- +44 141 330 5219**

<http://userweb.eng.gla.ac.uk/douglas.paul/index.html>

**Address: School of Engineering,
University of Glasgow,
Rankine Building,
Oakfield Avenue,
Glasgow,
G12 8LT,
U.K.**

<http://www.greensilicon.eu/GREENSilicon/index.html>